

# Exploring Plasma Dynamics with Laboratory Magnetospheres

Mike Mauel and  
LDX and CTX Experimental Teams  
Columbia University and PSFC, MIT

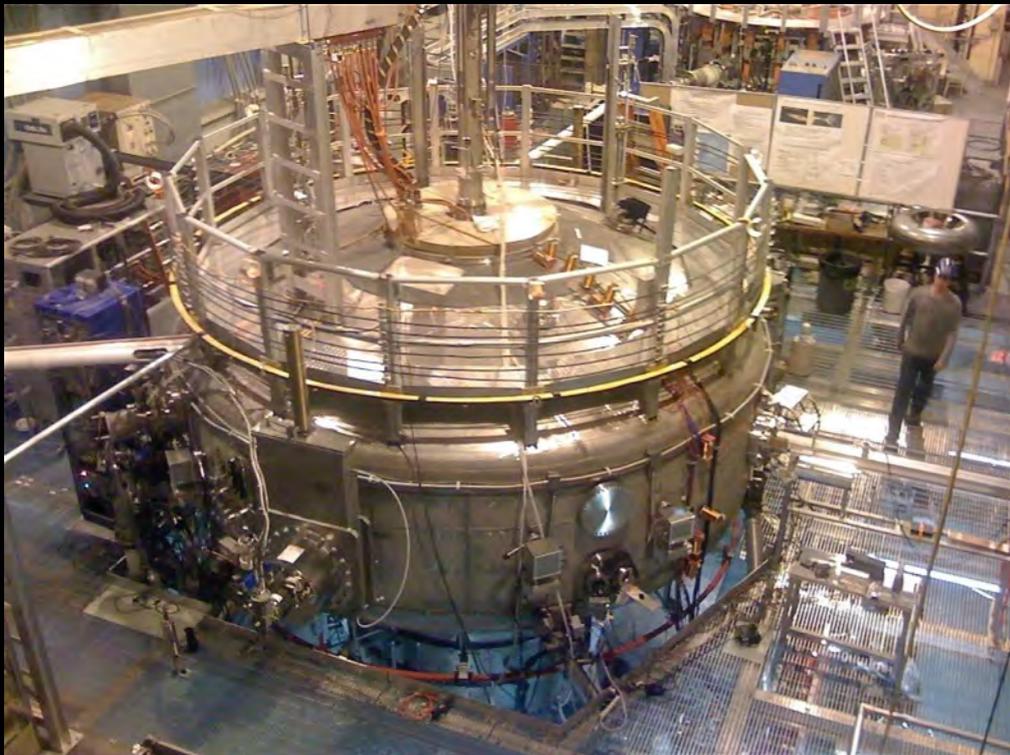
*Culham Science Centre, Abingdon, OX14 3DB, UK*  
February 2014



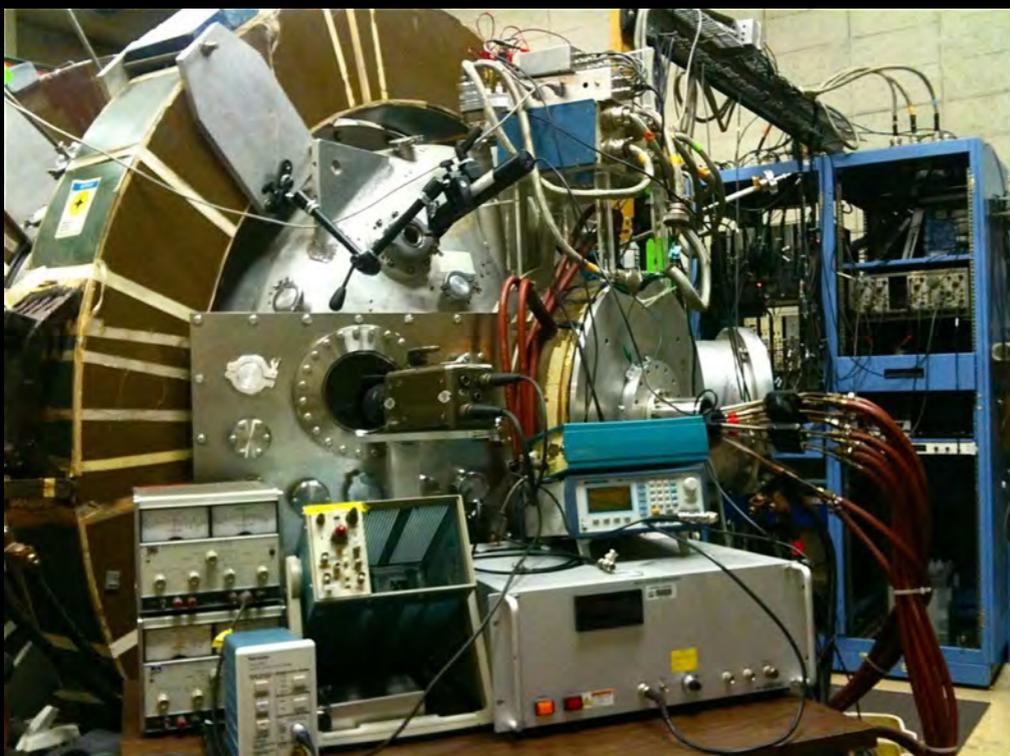
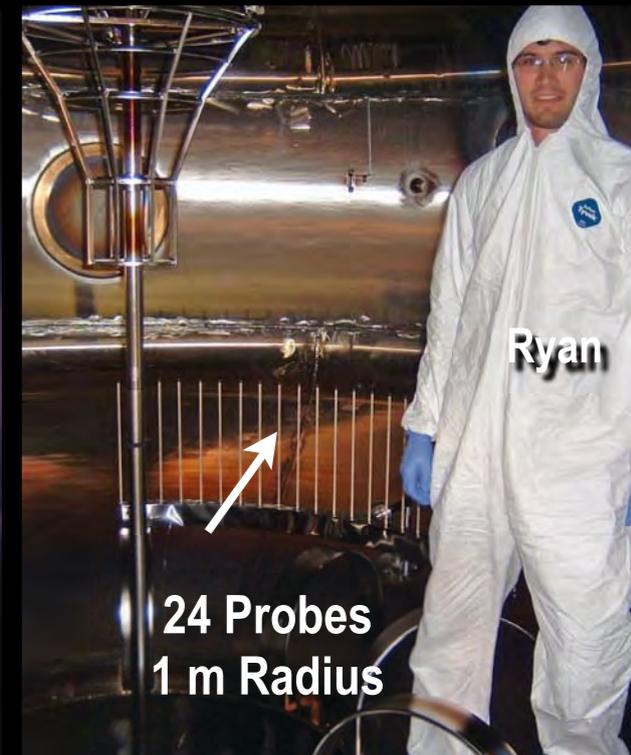
# Motivation

- **Can space weather physics be applied to the laboratory?**
  - Very high plasma pressure,  $\beta > 100\%$ , steady-state, without toroidal field
  - Collisionless and semi-collisional dynamics well-represented by bounce-averaged transport (*i.e.* particle number per unit flux with constant energy invariants)
  - Fluctuations drive plasma to “canonical” profiles: stationary, marginally stable states, having minimum entropy generation
- **Can laboratory studies facilitate the study of space physics and technology?**
  - Controlled experiments in relevant magnetic geometry
  - Very strong, but small, dipole magnet inside a very large vacuum chamber making possible very large plasma experiments at relatively low cost
  - “Whole plasma” access for unparalleled imaging and diagnostic measurement
  - Injection of waves (ECH, “chorus”, Alfvén, and ion-cyclotron waves), current, and particle/plasmoid gives unprecedented control over plasma properties and behaviors

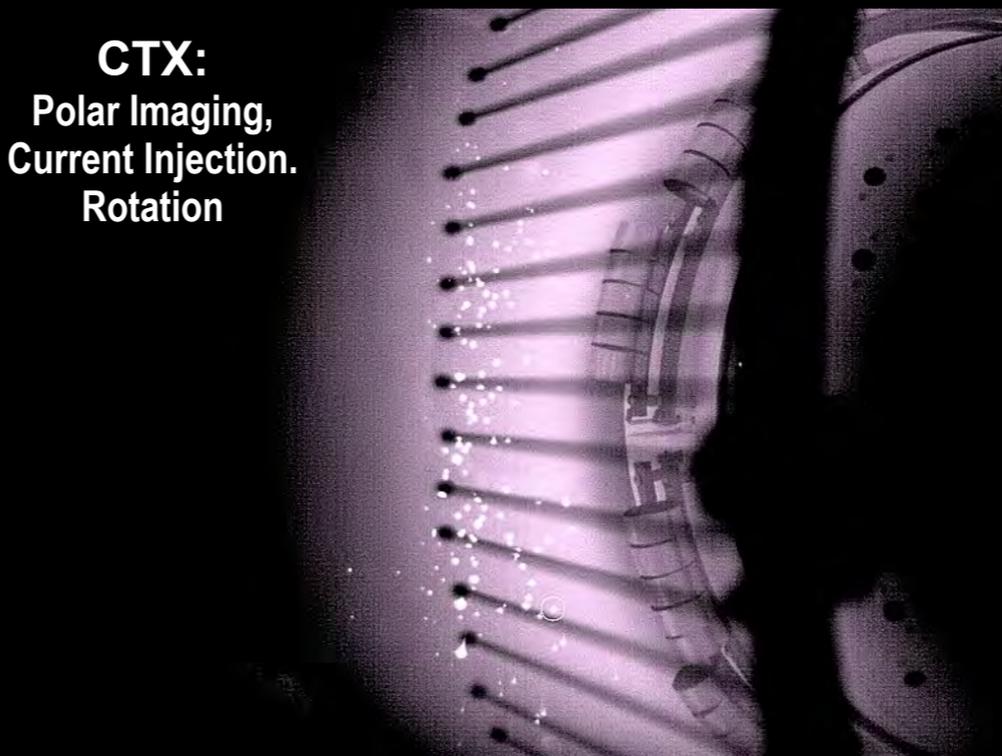
# Laboratory Magnetospheres: Facilities for Controlled Space Physics Experiments



**LDX:**  
High Beta Levitation & Turbulent Pinch



**CTX:**  
Polar Imaging,  
Current Injection,  
Rotation



# Outline

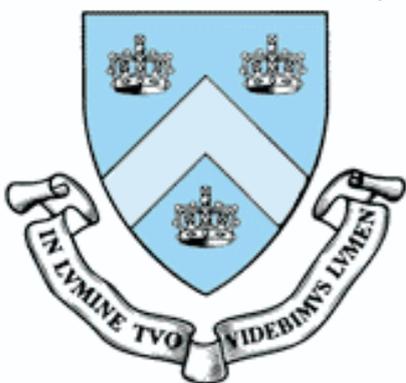
- How does a laboratory magnetosphere work?
- Interchange disturbances and magnetic drift resonances
  - ▶ **Low frequency interchange turbulence: steady “canonical” profiles and bounce-averaged (flux-tube averaged) gyrokinetics**
  - ▶ **Three interchange instabilities: Fast drift-kinetic, centrifugal interchange, semi-collisional entropy modes**
- **Examples:** exploring plasma dynamics by injection of heat, particles, current, and magnetic perturbations by decreasing ion inertial lengths

# LDX and CTX Team

*R. Bergmann, A. Boxer, D. Boyle, D. Brennan, M. Davis, G. Driscoll, R. Ellis, J. Ellsworth, S. Egorov, D. Garnier, B. Grierson, O. Grulke, C. Gung, A. Hansen, K.P. Hwang, V. Ivkin, J. Kahn, B. Kardon, I. Karim, J. Kesner, S. Kochan, V. Korsunsky, R. Lations, B. Levitt, S. Mahar, D. Maslovsky, M. Mael, P. Michael, E. Mimoun, J. Minervini, M. Morgan, R. Myatt, G. Naumovich, S. Nogami, E. Ortiz, M. Porkolab, S. Pourrahami, T. Pedersen, A. Radovinsky, A. Roach, M. Roberts, A. Rodin, G. Snitchler, D. Strahan, J. Schmidt, J. Schultz, B. Smith, P. Thomas, P. Wang, H. Warren, B. Wilson, M. Worstell, P. Woskov, B. Youngblood, A. Zhukovsky, S. Zweben*



Columbia University



National Science Foundation  
WHERE DISCOVERIES BEGIN

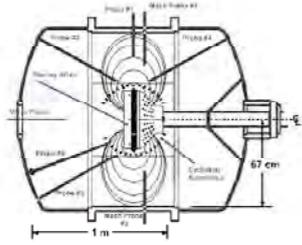




**Jay Kesner**

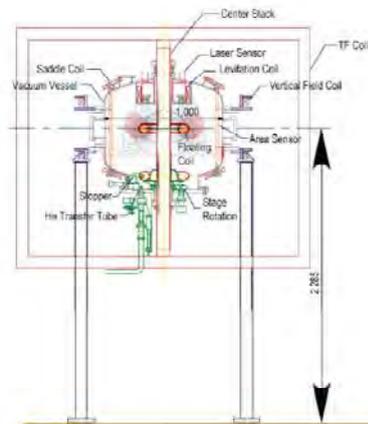
**Darren Garnier**

# Laboratory Dipole Experiments Around the World



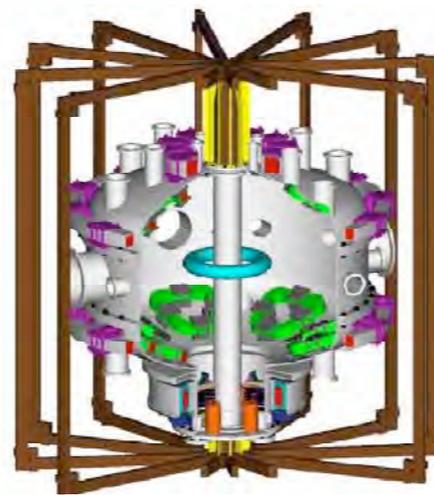
**CTX (Columbia)**

**150 kA turns  
(Not Levitated)  
0.15 m**



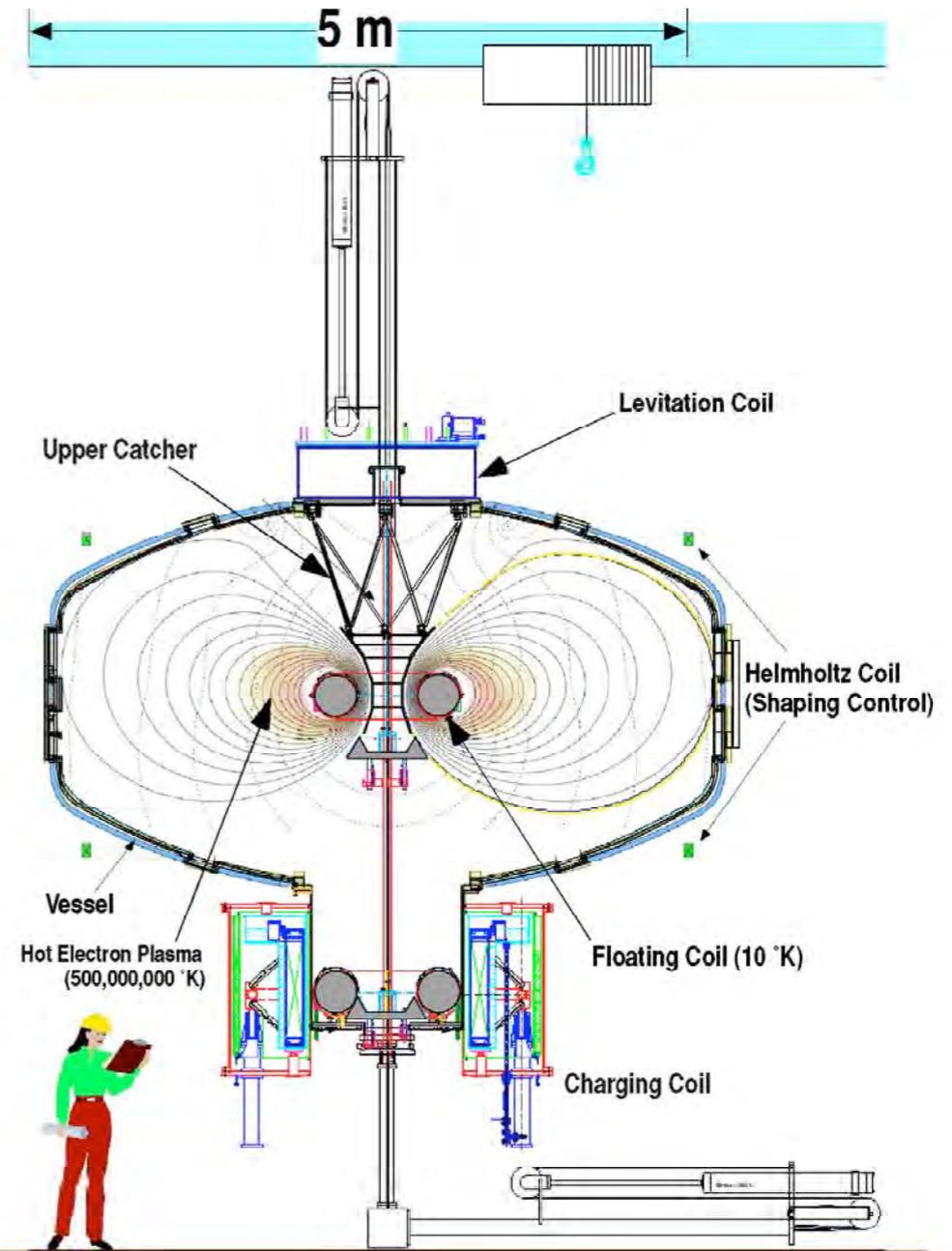
**Mini-RT (Univ. Tokyo)**

**50 kA turns  
17 kg  
0.15 m**



**RT-1 (Univ. Tokyo)**

**250 kA turns  
110 kg  
0.25 m**



**LDX (Columbia-MIT)**

**1200 kA turns  
565 kg  
0.34 m**

Hoist

Levitation Coil

**Launcher/Catcher**

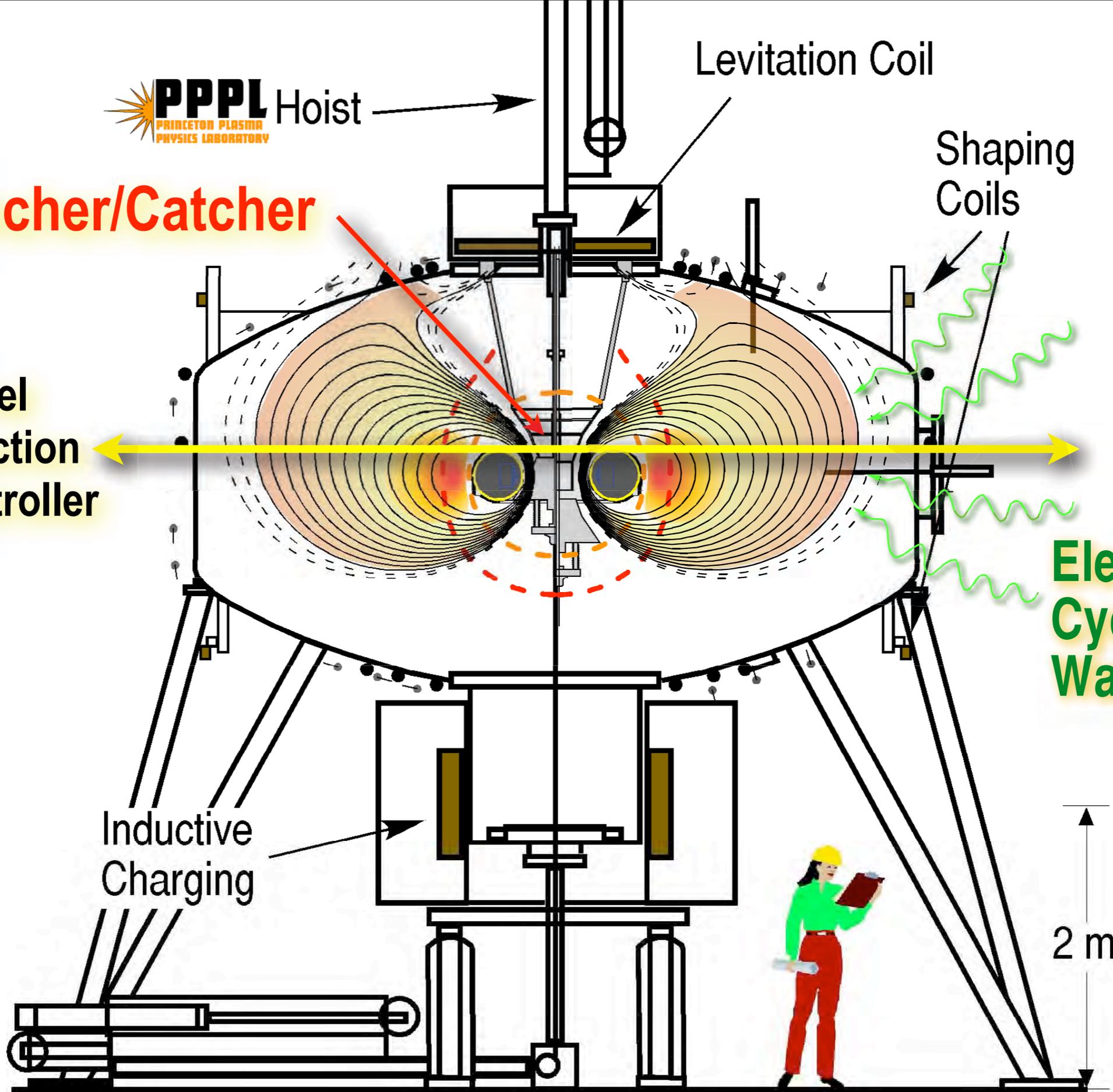
Shaping Coils

**8 Channel  
Laser Detection  
and RT Controller**

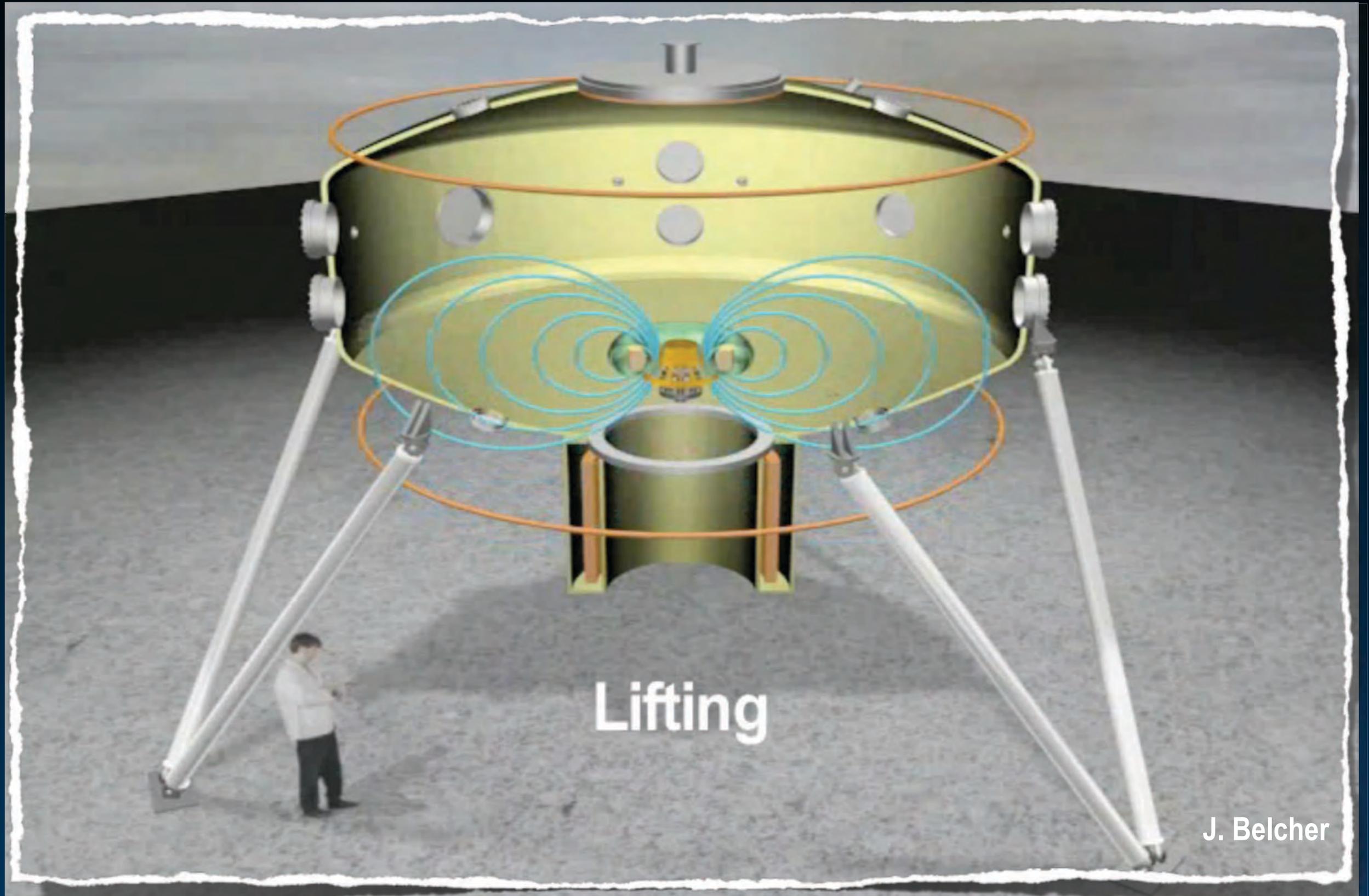
**Electron  
Cyclotron  
Waves**

Inductive  
Charging

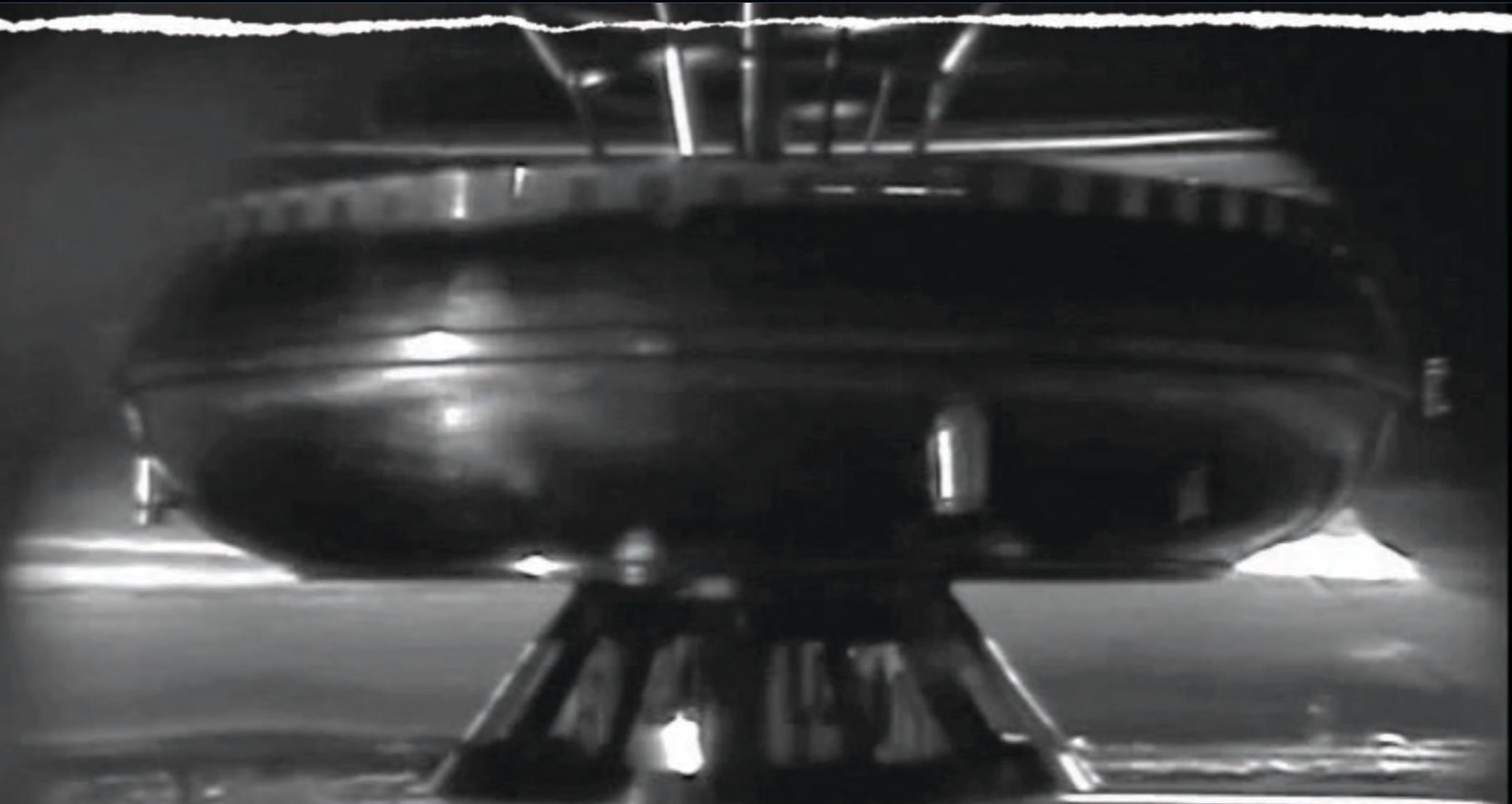
2 m



# Lifting, Launching, Levitation, Experiments, Catching

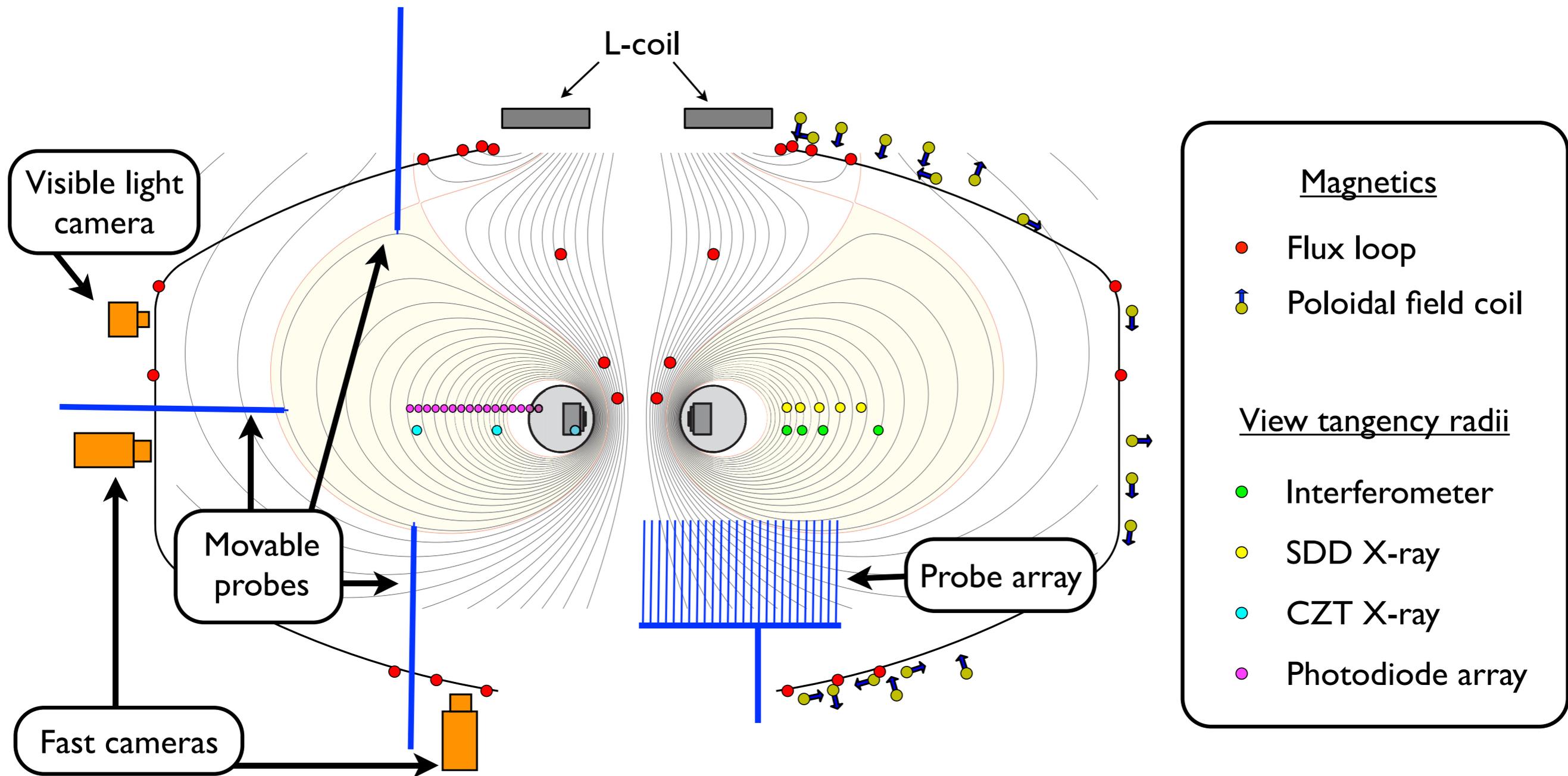


# First Levitated Dipole Plasma Experiment



**Floating  
(Up to 3 Hours)**

# Diagnosics

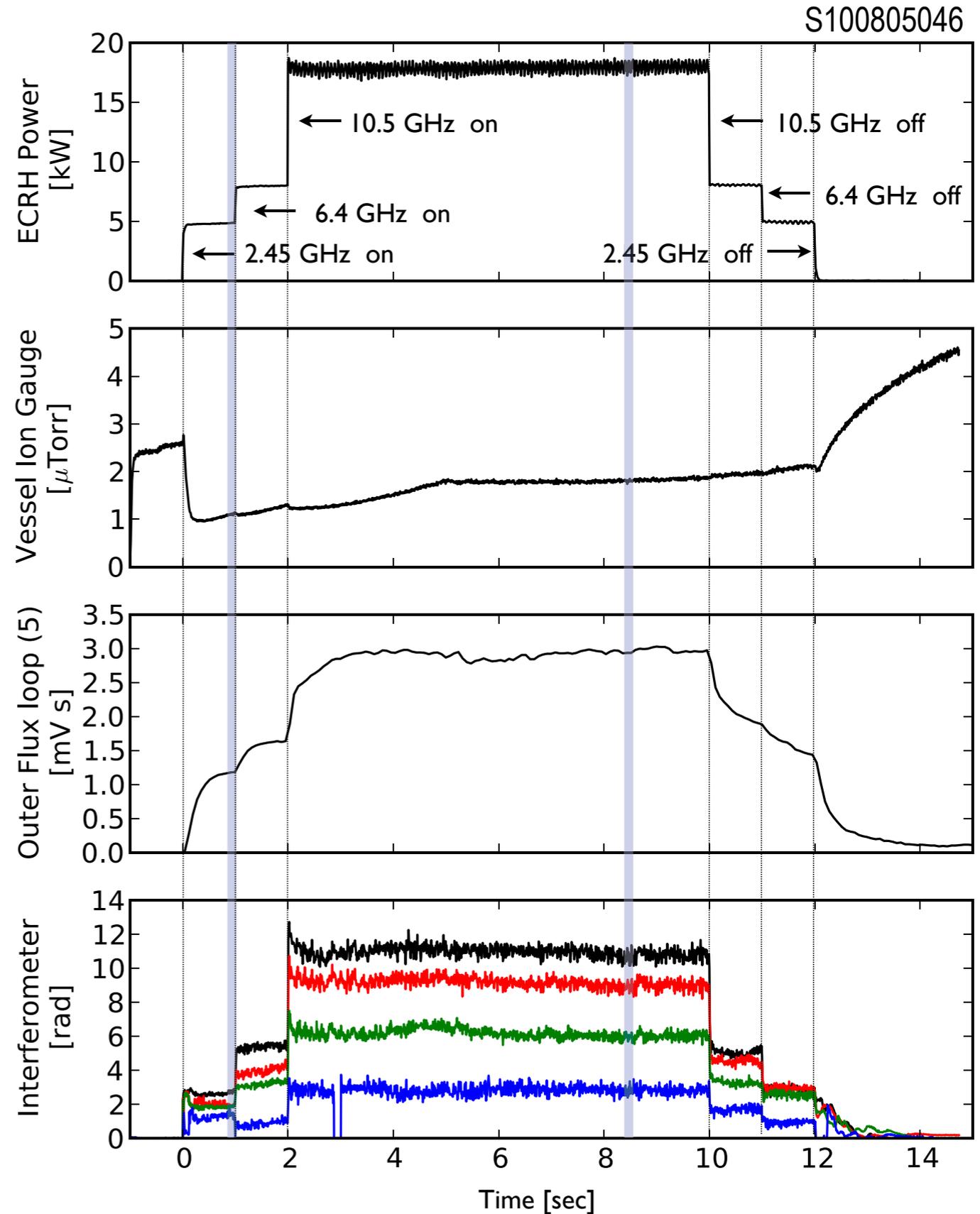


# Outline

- How does a laboratory magnetosphere work?
- Interchange disturbances and magnetic drift resonances
  - ▶ **Low frequency interchange turbulence: steady “canonical” profiles and bounce-averaged (flux-tube averaged) gyrokinetics**
  - ▶ **Three interchange instabilities: Fast drift-kinetic, centrifugal interchange, semi-collisional entropy modes**
- **Examples:** exploring plasma dynamics by injection of heat, particles, current, and magnetic perturbations by decreasing ion inertial lengths

# Example Plasma Experiment

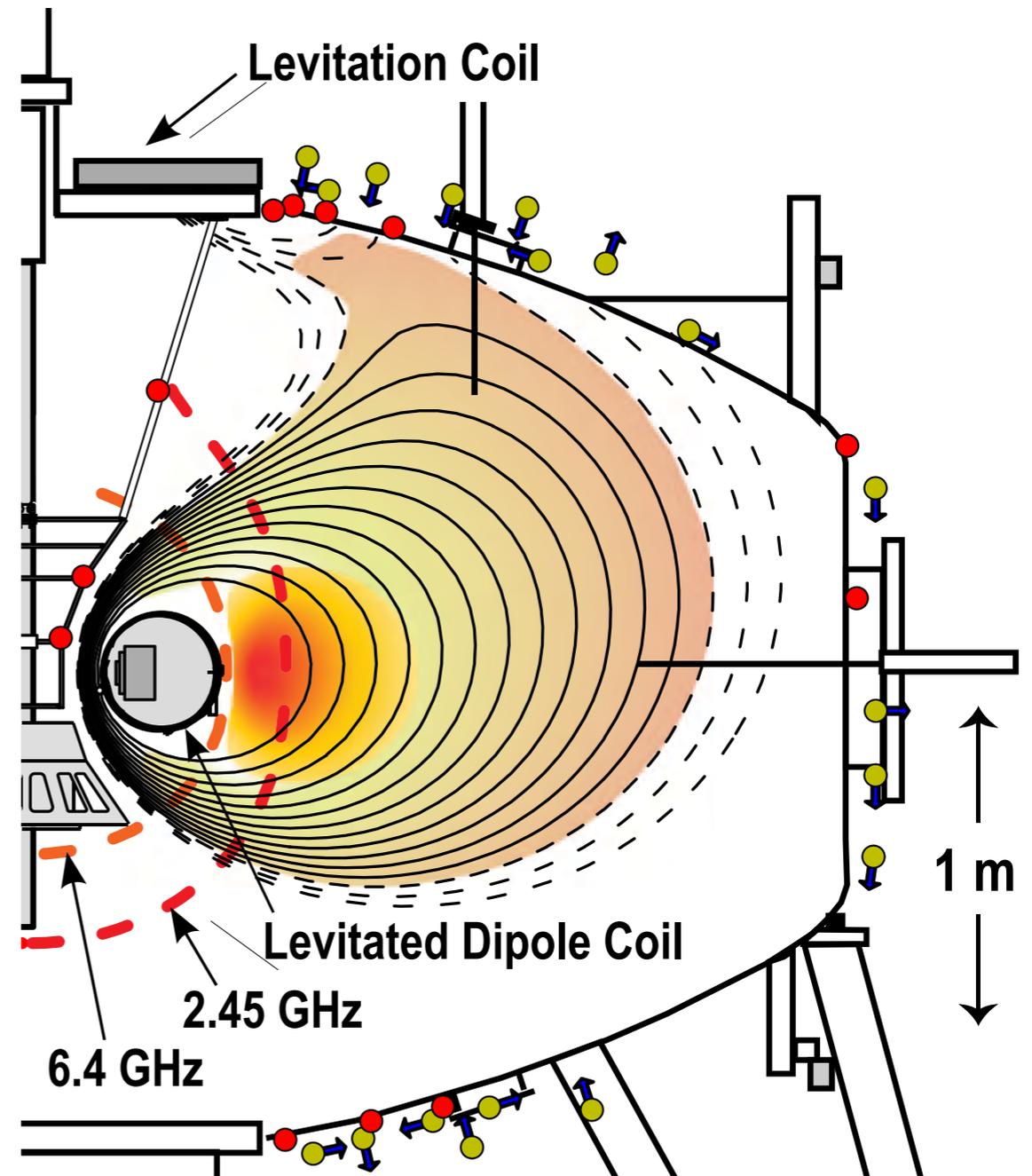
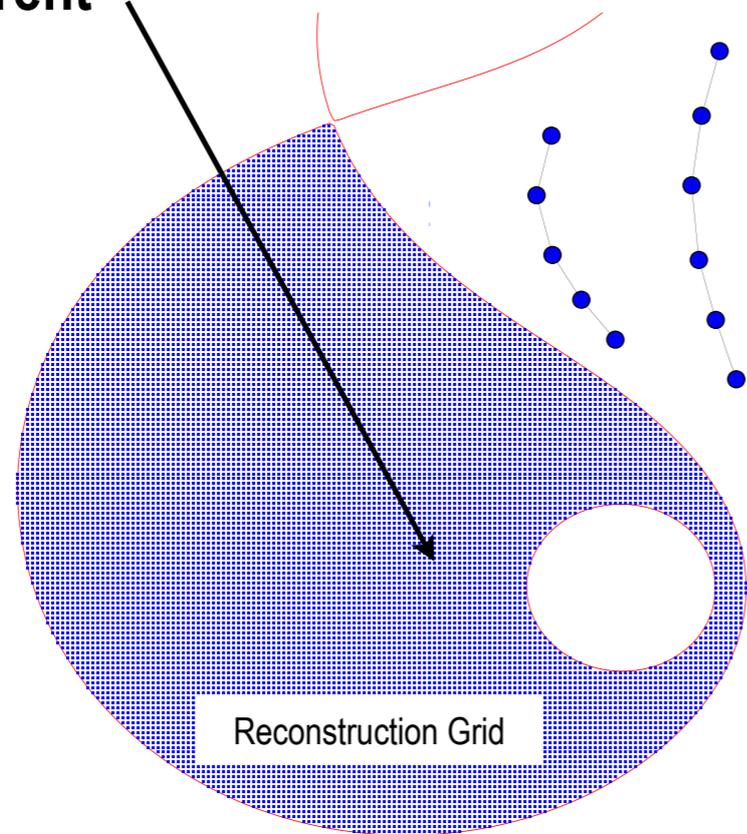
- 20 kW injected electron cyclotron waves
- Plasma energy 250 J (3 kA ring current)
- Peak  $\beta \sim 40\%$  (70% achieved in RT-1)
- Hydrogen gas density  $4 \times 10^{10} \text{ cm}^{-3}$
- Peak plasma density  $10^{12} \text{ cm}^{-3}$
- Energetic electrons  $\langle E \rangle \sim 54 \text{ keV}$
- Peak  $\langle T \rangle > 0.5 \text{ keV}$  (thermal)
- Density proportional to injected power
- Sustained, dynamic, “steady state”



# Measuring the Plasma Pressure from the Plasma Ring Current

$$\mathbf{J}_{\perp} = \frac{\mathbf{B} \times \nabla P_{\perp}}{B^2} + \frac{\mathbf{B} \times \kappa}{B^2} (P - P_{\perp})$$

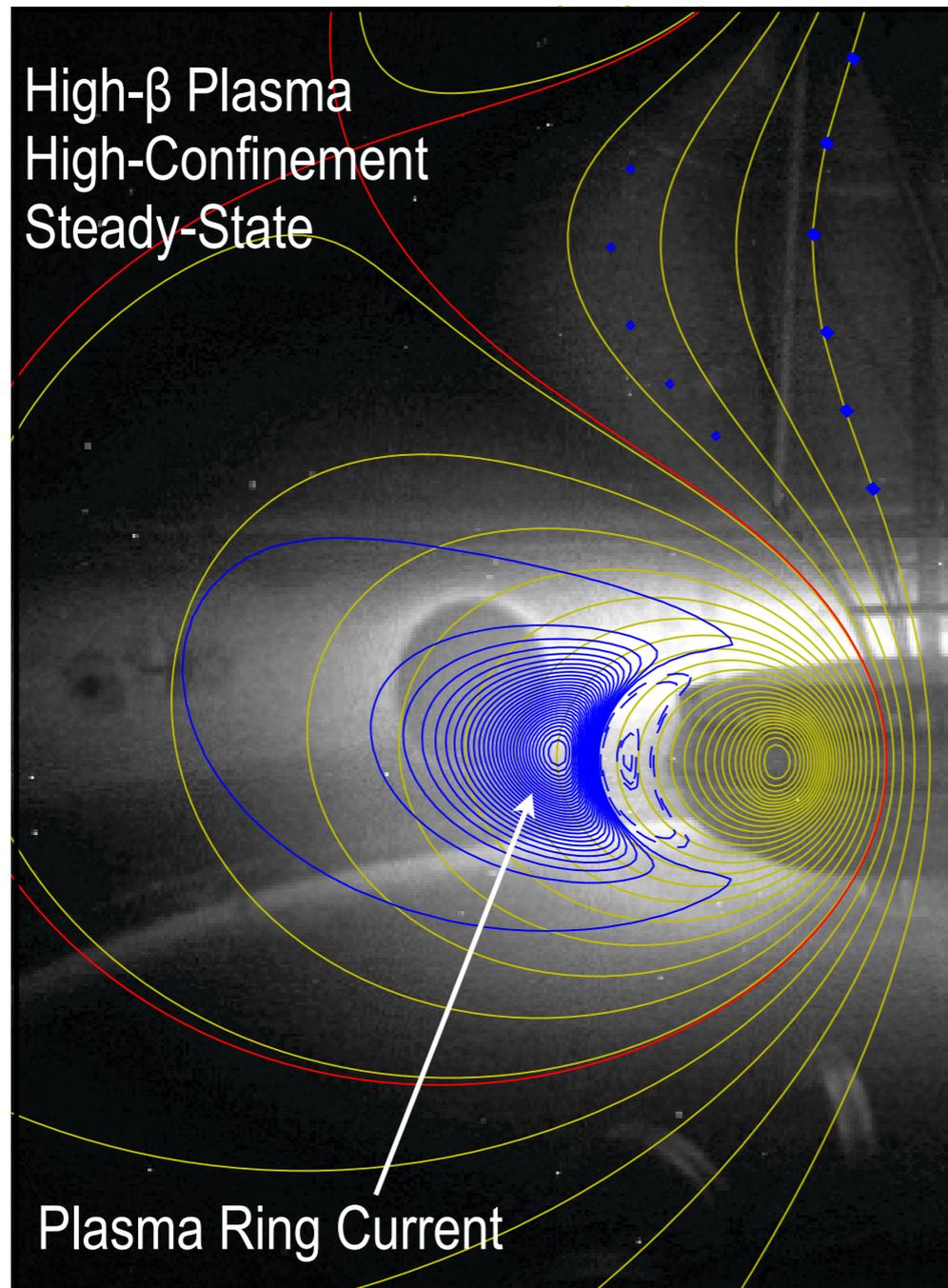
Plasma Ring Current



What is the plasma ring current distribution that fits magnetic sensor arrays?

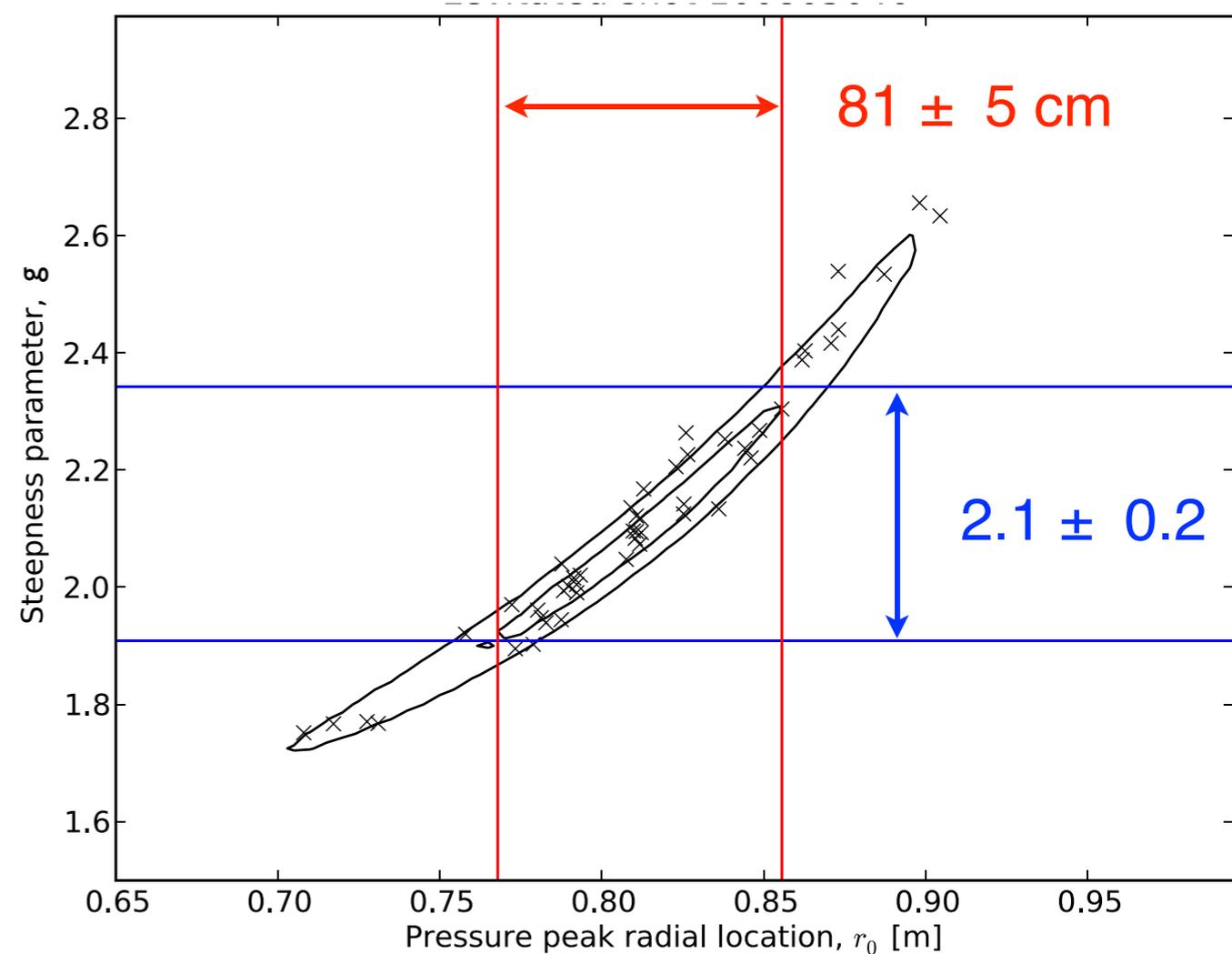
# Measuring the Plasma Pressure from the Plasma Ring Current

$$\mathbf{J}_{\perp} = \frac{\mathbf{B} \times \nabla P_{\perp}}{B^2} + \frac{\mathbf{B} \times \kappa}{B^2} (P - P_{\perp})$$



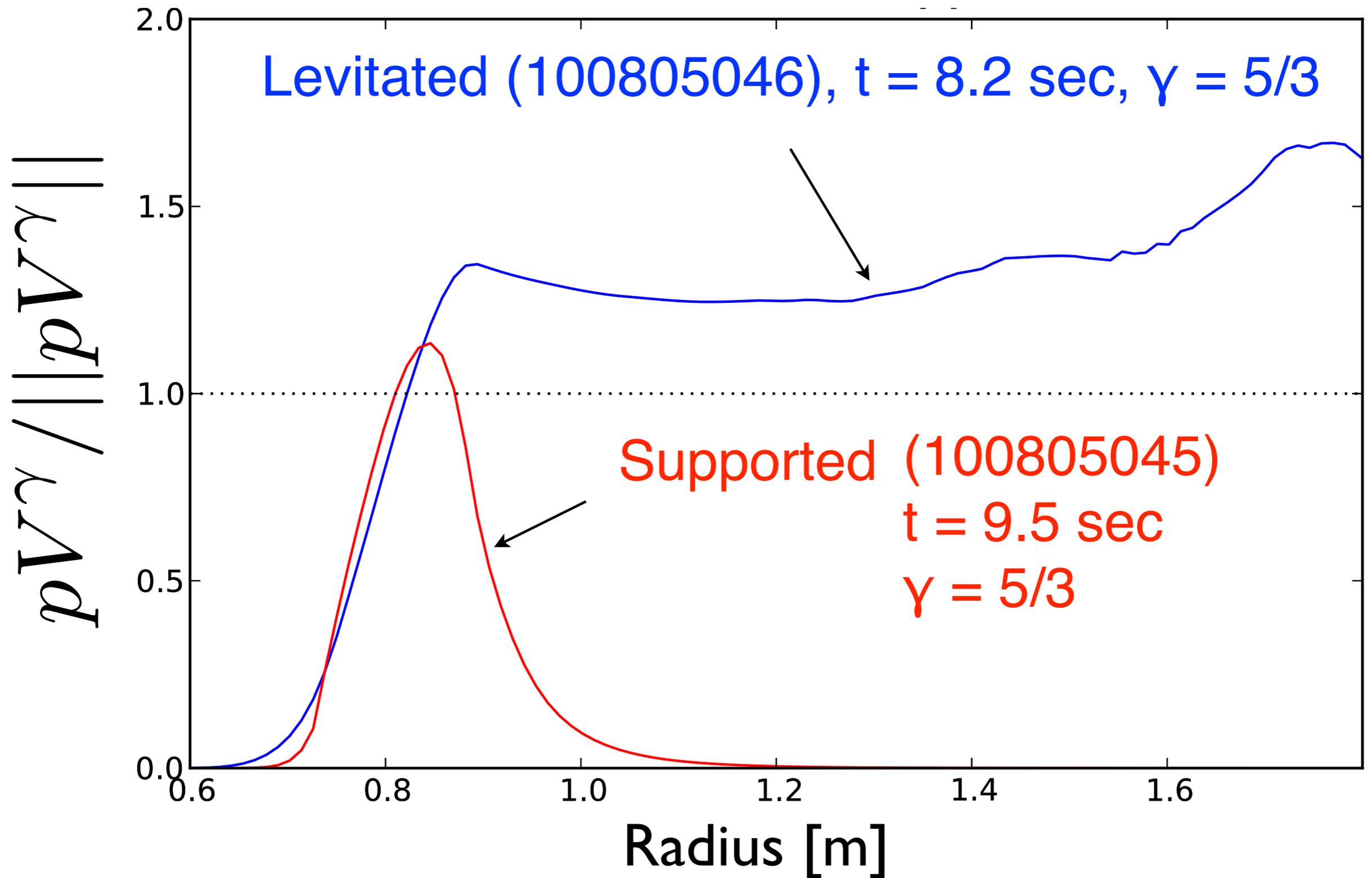
3 kA

## Reconstruction Results in Very Good Accuracy of Pressure Profile



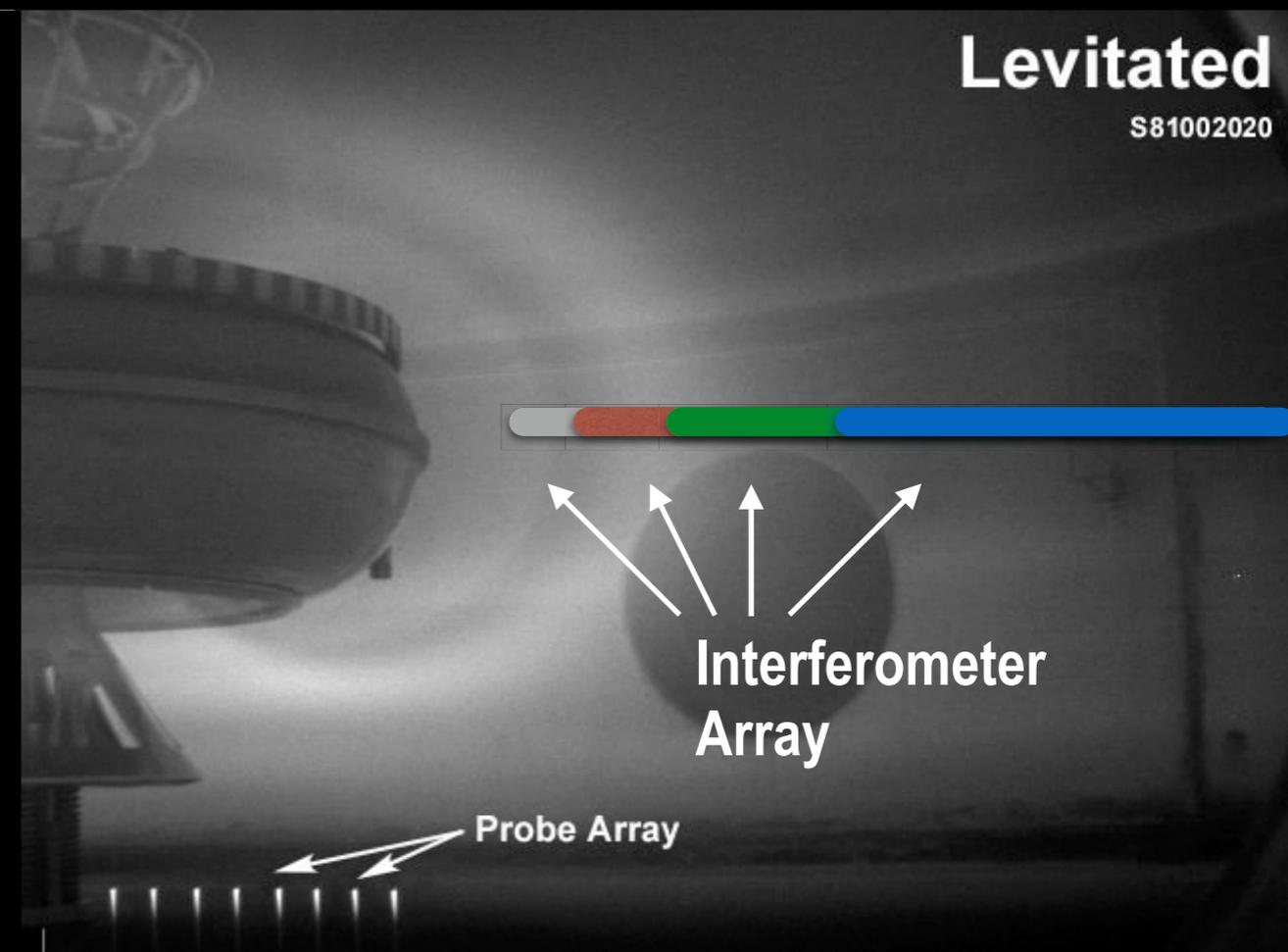
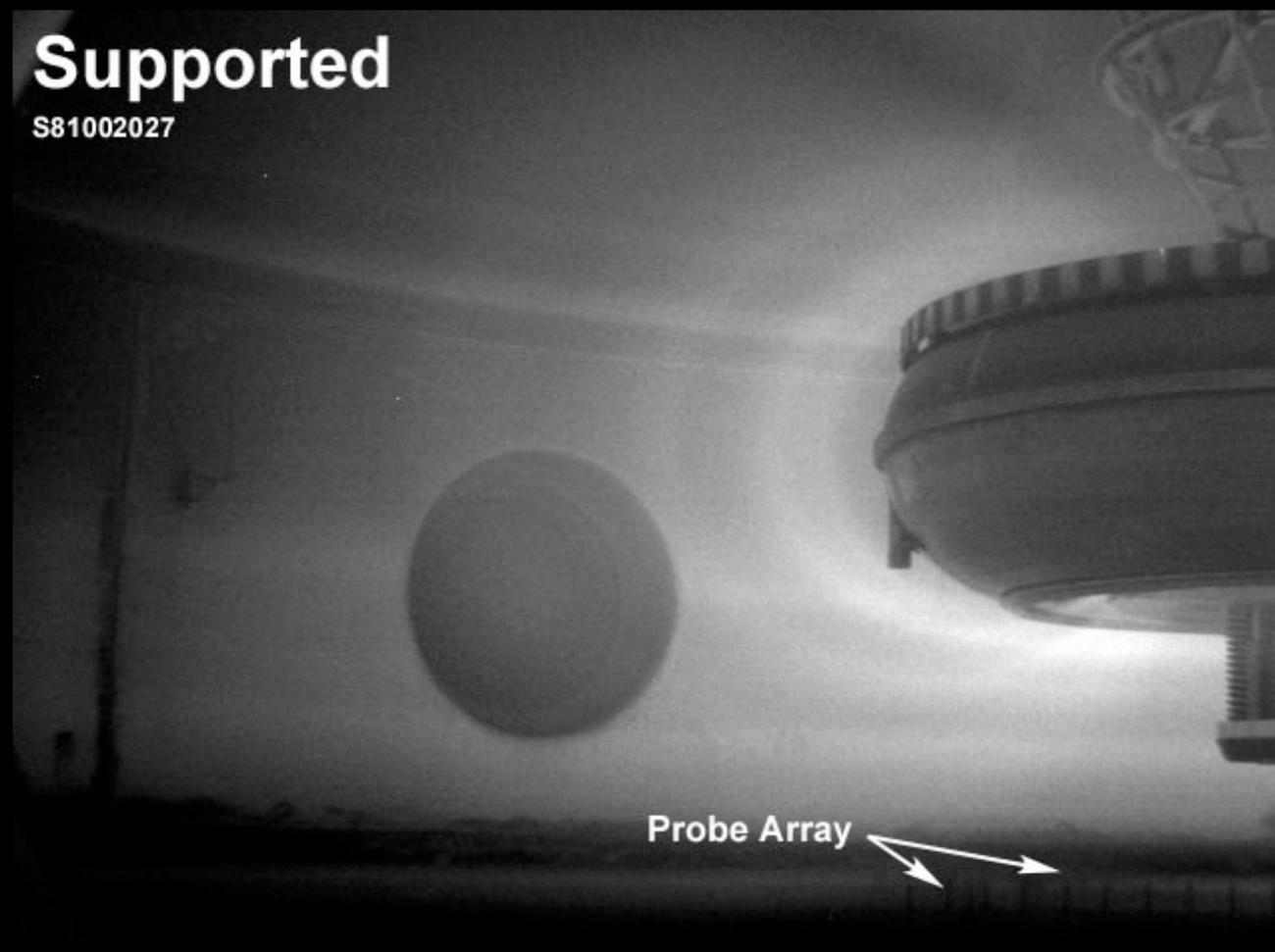
$$P_{||} \approx P_{\perp}$$

# “Canonical” Profile: $\delta(PV^\gamma) \approx 0$



# Measurement of Density Profile with Interferometry

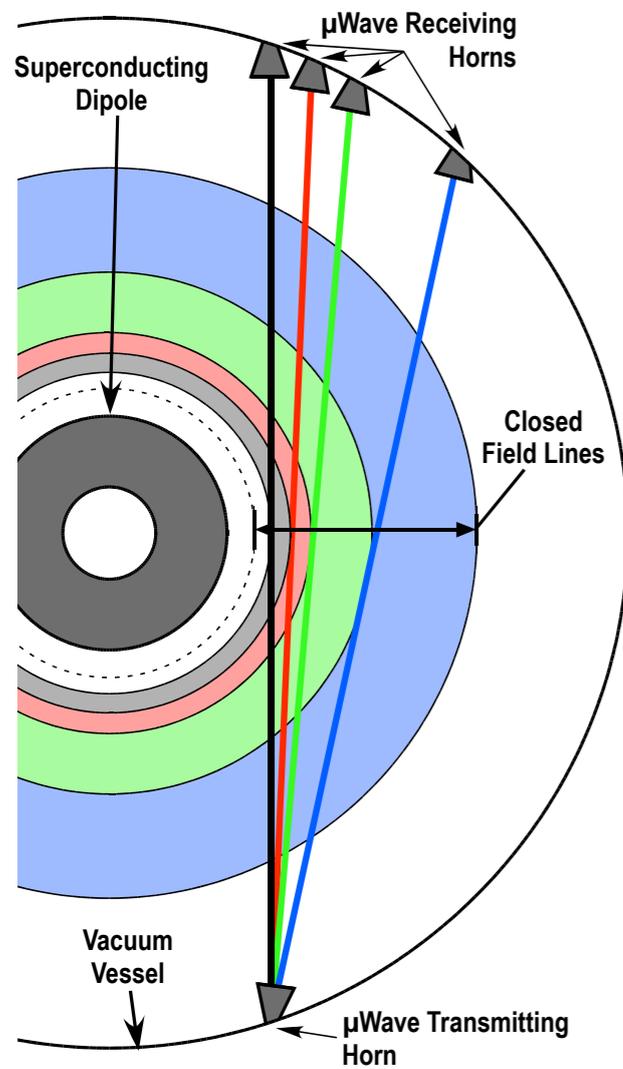
← 5 m →



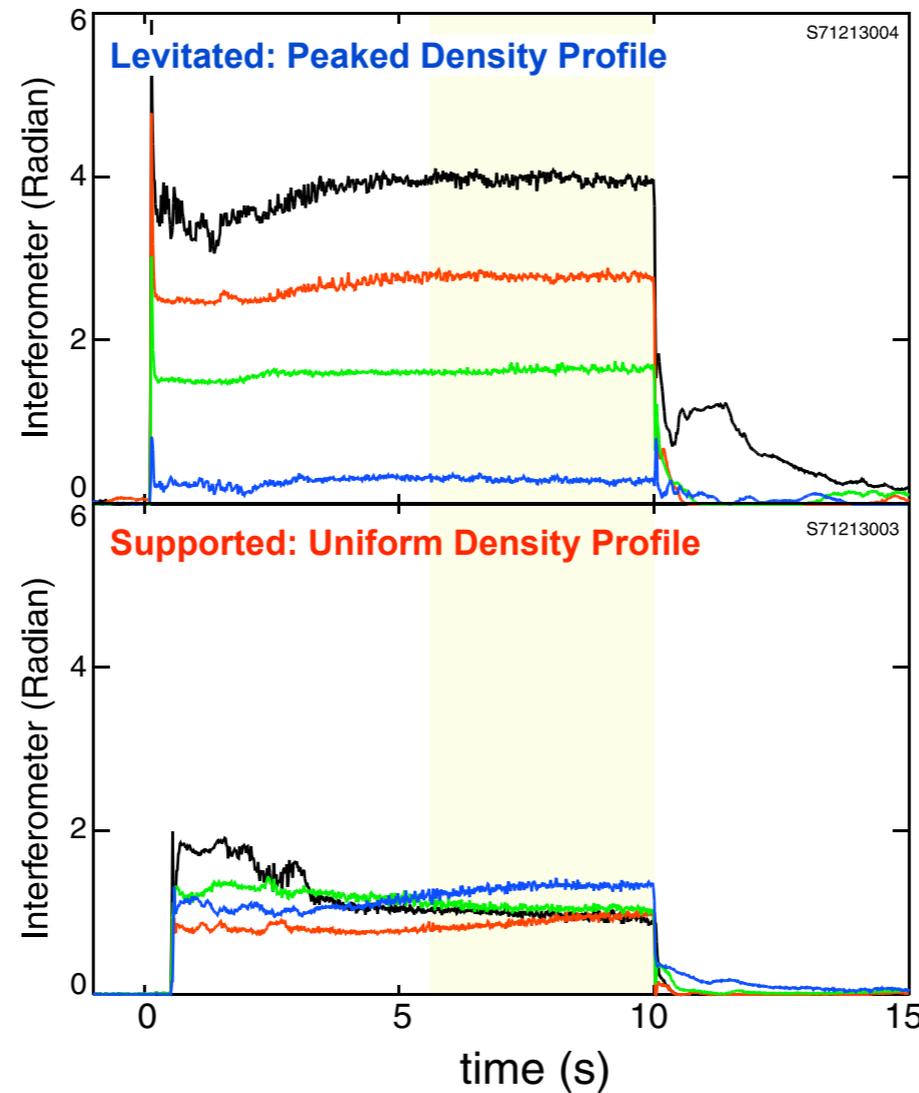
# Measurement of Density Profile with Interferometry

## Show Equal Particle Number per Unit Magnetic Flux

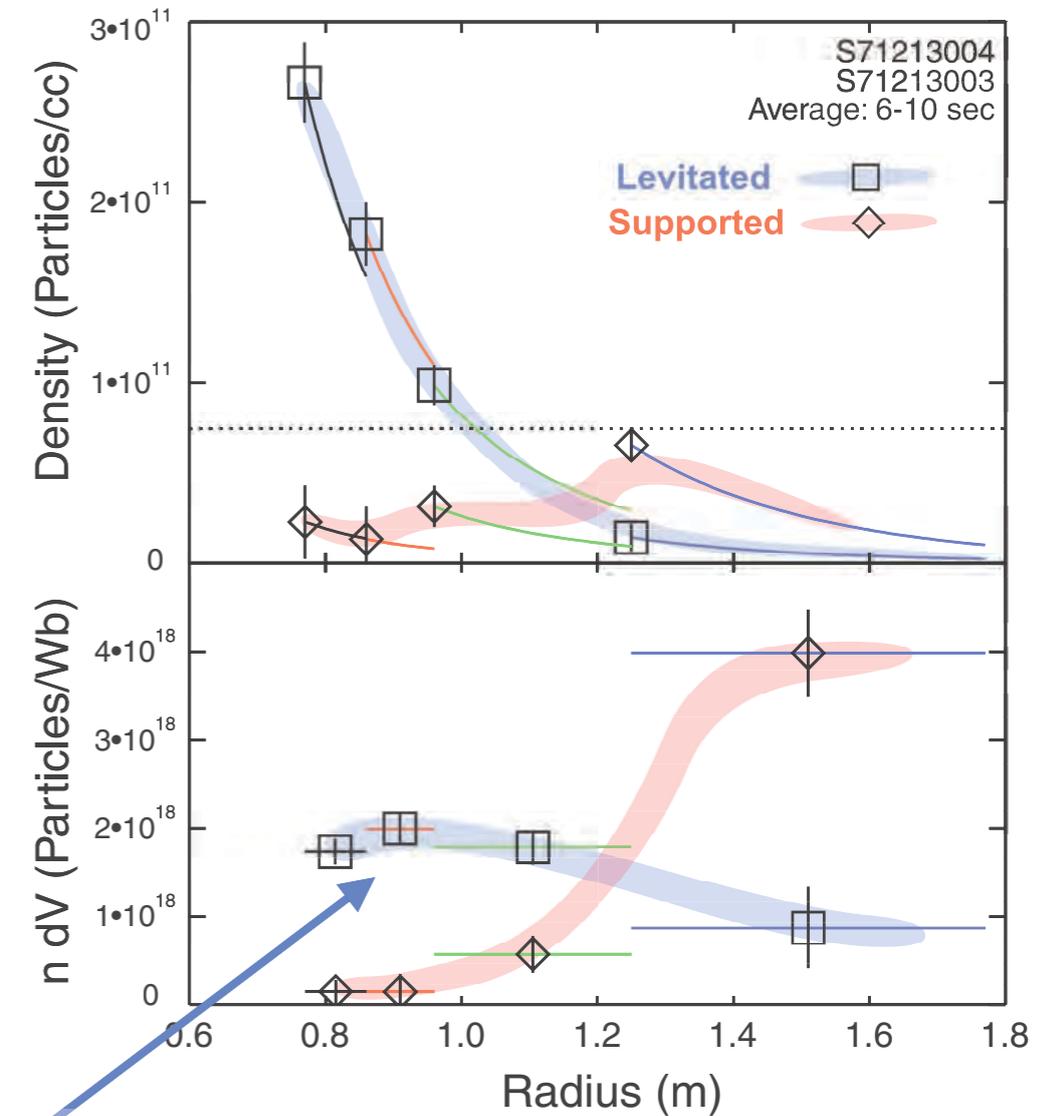
(a) Interferometer Cords



(b) Interferometer Measurements



(c) Density and Number Radial Profiles



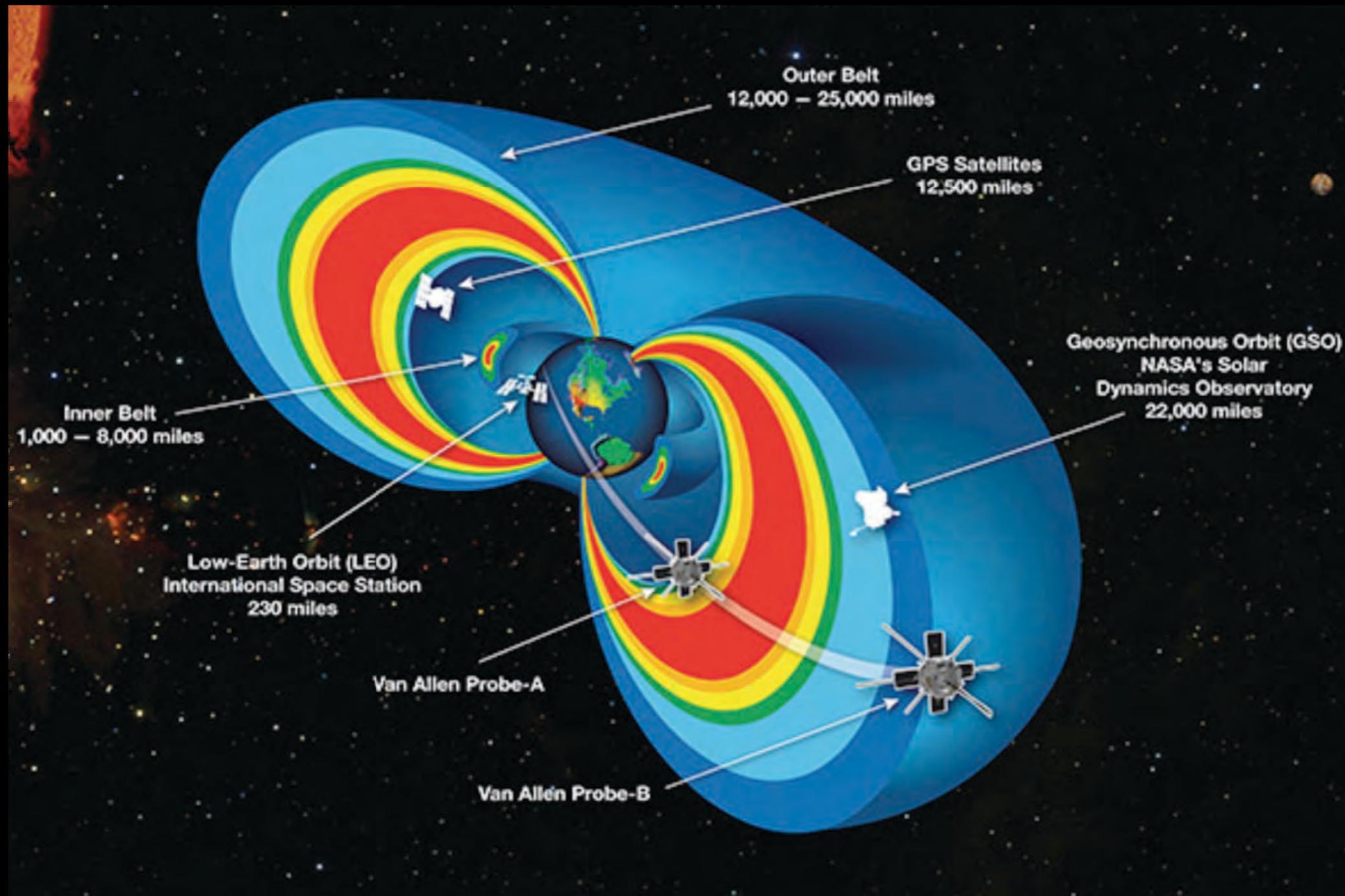
“Canonical” Profile:  $\delta(nV) \approx 0$

# Self-Organized Mixing: Dye Stirred in Glass



# Our Space Environment is Complex and Highly Variable

With Concurrent Plasma Processes and Important Questions to Answer



Van Allen Probes (A&B) Launched August 2012

Discovered **New** 3rd Radiation Belt (2 MeV e<sup>-</sup>) then annihilated by passage of interplanetary shock  
ScienceExpress, Baker, *et al.*, 28 Feb 2013

# Convection Electric Fields and the Diffusion of Trapped Magnetospheric Radiation

THOMAS J. BIRMINGHAM

$$\mathbf{E} \times \mathbf{B} \quad \left\{ \dot{\psi} = \nabla \psi \cdot \mathbf{V} = \frac{\partial \Phi}{\partial \varphi} = -R E_{\varphi} \right.$$

$$\text{Diffusion Coefficient} \quad \left\{ \begin{aligned} D_{\psi} &= \lim_{t \rightarrow \infty} \int_0^t dt \langle \dot{\psi}(t) \dot{\psi}(0) \rangle \equiv \langle \dot{\psi}^2 \rangle \tau_c \\ &= R^2 \langle E_{\varphi}^2 \rangle \tau_c \end{aligned} \right.$$

$$\text{Adiabatic Radial Transport} \quad \left\{ \frac{\partial F}{\partial t} = S + \frac{\partial}{\partial \psi} \Big|_{\mu, J} D_{\psi}(\mu, J) \frac{\partial F}{\partial \psi} \Big|_{\mu, J} \right.$$

## Collisionless Radiation Belt Particles

NORAD OV3-4 (1966) validated physics of inward pinch and adiabatic heating of drift-resonant radiation belt particles. Farley, et al., *Phys. Rev. Lett.*, 1970

# INNER MAGNETOSPHERIC MODELING WITH THE RICE CONVECTION MODEL

FRANK TOFFOLETTO, STANISLAV SAZYKIN, ROBERT SPIRO and RICHARD WOLF

Department of Physics and Astronomy, Rice University, Houston, TX 77005, U.S.A.

## Semi-collisional Plasmasphere and Ring Current

TABLE I

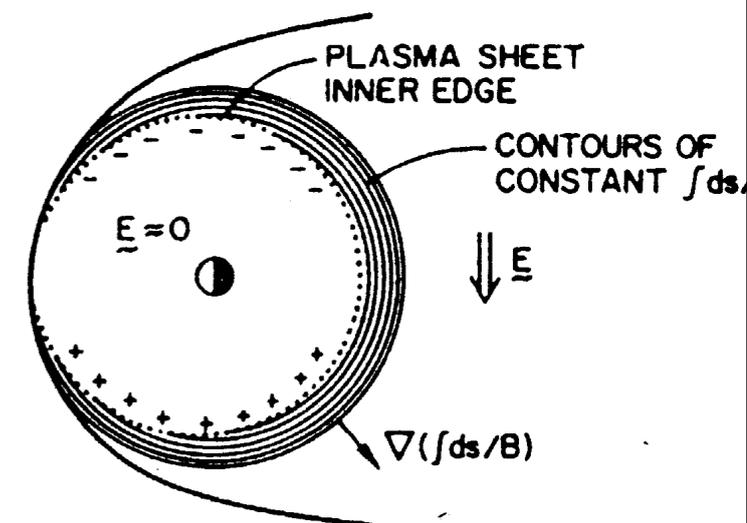
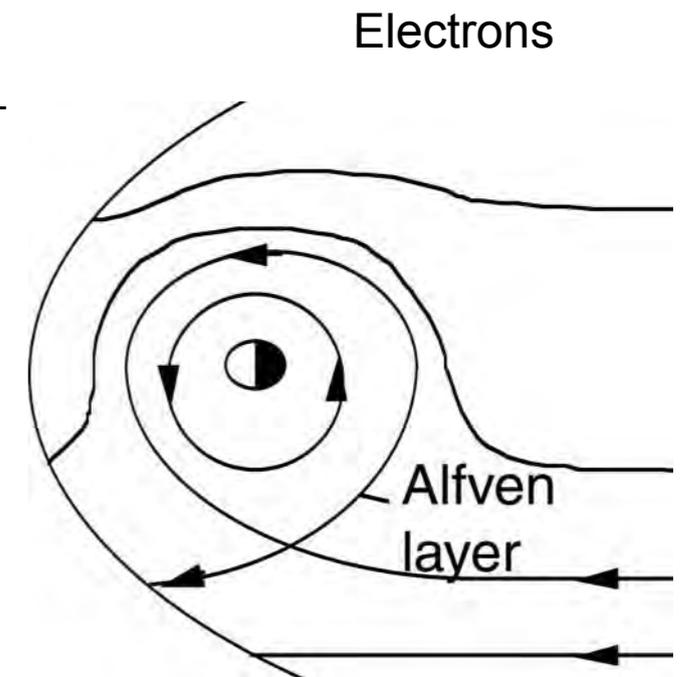
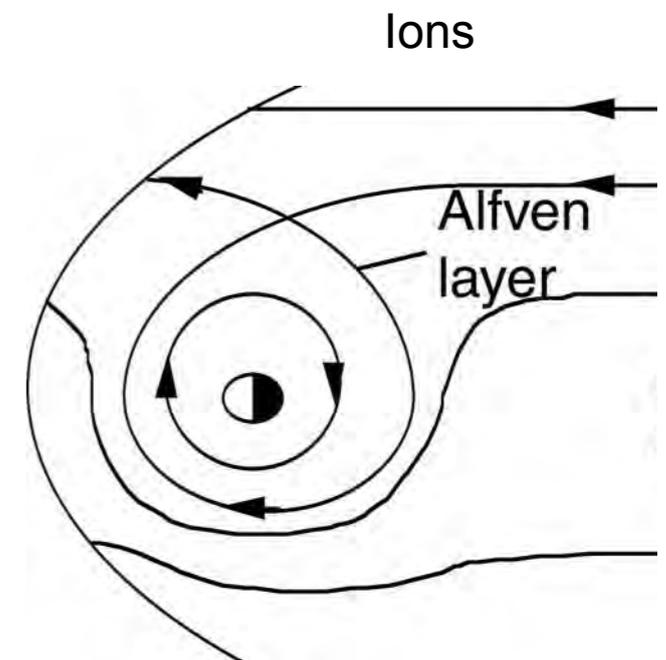
Comparison of equations of ideal MHD with those used in the RCM

Ideal MHD	RCM
$\frac{\partial \rho}{\partial t} + \nabla \cdot \rho \mathbf{v} = 0$	$\frac{\partial}{\partial t} \sum_k \eta_k \lambda_k \frac{\mathbf{x} \cdot \mathbf{t}}{V} + \nabla \cdot \mathbf{j}_k = S \eta_k - L \eta_k$
$\frac{\partial}{\partial t} \mathbf{v} + \nabla \cdot (\rho \mathbf{v} \mathbf{v}) + \mathbf{j} \times \mathbf{B} - \nabla P$	$\mathbf{j}_k \times \mathbf{B} - \nabla P_k$
$\frac{\partial}{\partial t} \mathbf{v} + \nabla \cdot (P \rho^{-5/3}) = 0$	$P = \frac{2}{3} \sum_k \eta_k \lambda_k V^{-5/3} \lambda_k \text{ constant}$
$\nabla \cdot \mathbf{B} = 0$	Part of the magnetic field model.
$\nabla \times \mathbf{B} = \mu_0 \mathbf{j}$	Included in magnetic field, but $\mathbf{j} = \sum_k \mathbf{j}_k$ .
$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$	Included implicitly in mapping.
$\mathbf{E} + \mathbf{v} \times \mathbf{B} = 0$	$\mathbf{E} + \mathbf{B} \cdot \nabla = 0$ and $\mathbf{E} \cdot \mathbf{v}_k = \frac{\nabla W \cdot \lambda_k \mathbf{x} \cdot \mathbf{t}}{q_k}$

For each species and invariant energy  $\lambda$ ,  $\eta$  is conserved along a drift path.

Specific Entropy

$$pV^\gamma = \frac{2}{3} \sum_s |\lambda_s| \eta_s$$



# Bounce-Averaged Turbulent Mixing in Toroidal Laboratory Plasmas

For isentropic mixing and when the turbulent spectrum is sufficiently broad to interact (nearly equally) with all particles, independent of energy and pitch-angle, the curvature pinch dominates.

**Diffusion of flux-tube particle number,  $n\delta V$ , ...**

$$\begin{aligned}\frac{\partial(\bar{n}\delta V)}{\partial t} &= \langle S \rangle + \frac{\partial}{\partial\psi} D_\psi \frac{\partial(\bar{n}\delta V)}{\partial\psi} \\ &= \langle S \rangle + \frac{\partial}{\partial\psi} \left[ \underbrace{D_\psi \delta V}_{\text{Diffusion}} \frac{\partial\bar{n}}{\partial\psi} + \bar{n} \underbrace{D_\psi \frac{\partial\delta V}{\partial\psi}}_{\text{Pinch Velocity}} \right]\end{aligned}$$

**Diffusion of Energy/Entropy,  $P\delta V^\gamma$ , ...**

$$\frac{\partial(\bar{P}\delta V^\gamma)}{\partial t} = \langle H \rangle + \frac{\partial}{\partial\psi} D_\psi \frac{\partial(\bar{P}\delta V^\gamma)}{\partial\psi}$$

# “Canonical” Profiles of Magnetized Plasma

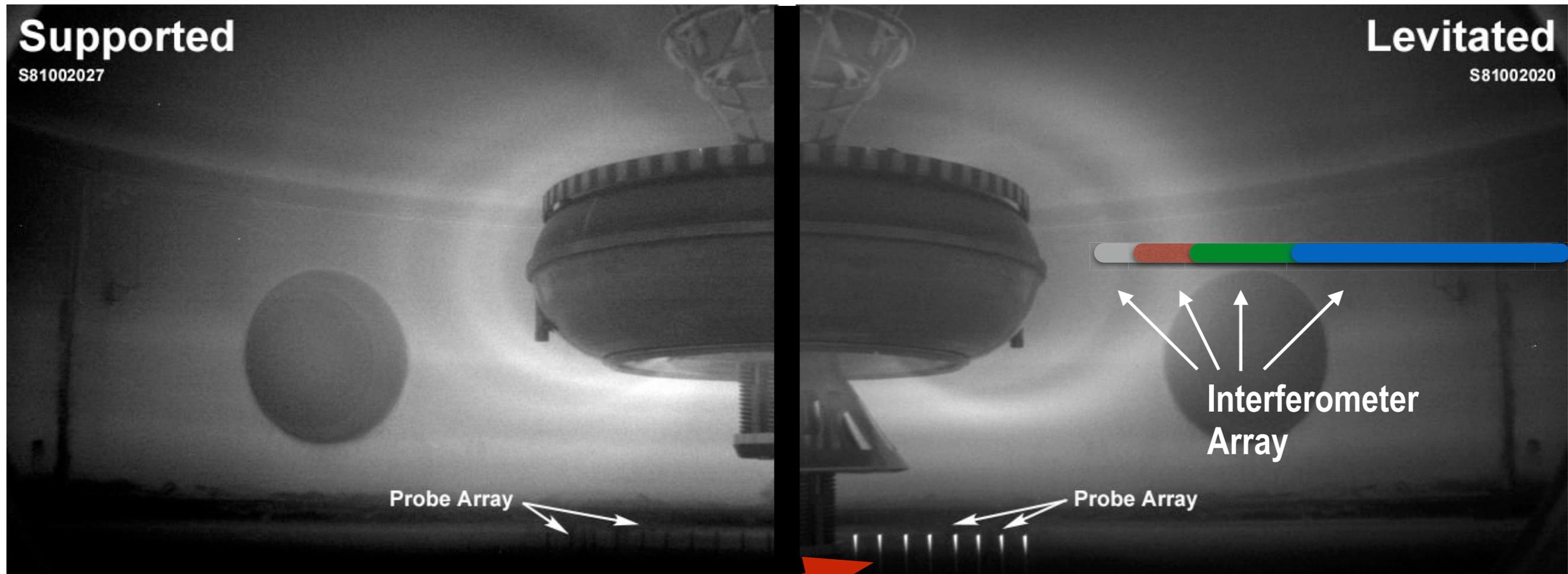
$$\delta(nV) \approx 0 \quad \& \quad \delta(PV^Y) \approx 0$$

- Low frequency fluctuations in strongly magnetized plasma,  $\omega_d \sim \omega \ll \omega_b \ll \omega_c$ , conserve *energy* or *Lagrangian invariants* of the flow.
- **Turbulent mixing across flux tube volumes “self organizes”** magnetized plasma to **canonical profiles**, which are nearly stationary  $\delta(nV) \approx 0$  and  $\delta(PV^Y) \approx 0$ .
- **Flux-tube geometry** determines curvature diffusive & pinch terms in coordinate-space.
- **Space (i.e. Dipole) geometry:**
  - ➔ Birmingham, *J. Geophysical Res.*, 1969
  - ▶ Harel, Wolf, *et al.*, *J. Geophys. Res.*, 1981
  - ▶ Kobayashi, Rogers, and Dorland, *Phys. Rev. Lett.*, 2010
  - ▶ Kesner, *et al.*, *Plasma Phys. Control. Fusion*, 2010; Kesner, *et al.*, *Phys. Plasmas*, 2011.
- **Tokamak geometry:**
  - ➔ Coppi, *Comments Plasma Phys. Controll. Fus.*, 1980
  - ▶ Yankov, *JETP Lett.*, 1994 and Isichenko, *et al.*, *Phys. Rev. Lett.*, 1995
  - ▶ Baker and Rosenbluth, *Phys. Plasmas*, 1998; Baker, *Phys. Plasmas*, 2002
  - ▶ Garbet, *et al.*, *Phys. Plasmas*, 2005

# Quantitative Verification of Turbulent Particle Pinch

Using only *measured electric field* fluctuations,  
Space weather diffusion model is verified with levitated dipole

5 m



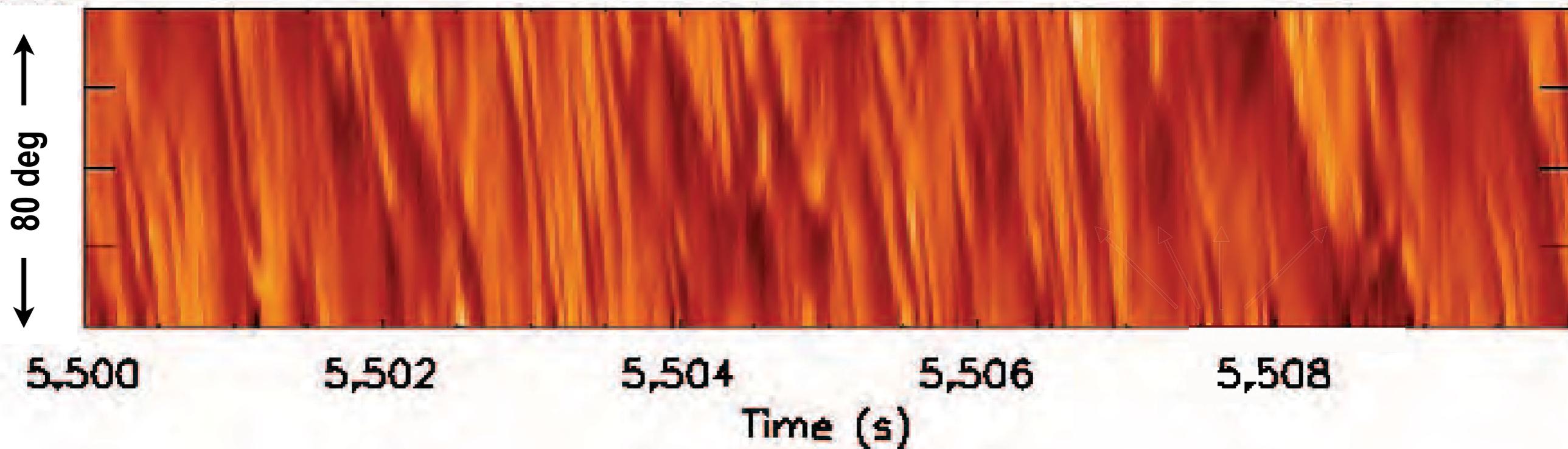
**Edge Probe Array:**

$$D = \lim_{t \rightarrow \infty} \int_0^t dt \langle \dot{\psi}(t) \dot{\psi}(0) \rangle \equiv \langle \dot{\psi}^2 \rangle \tau_c$$
$$D_\psi = R^2 \langle E_\varphi^2 \rangle \tau_c$$

# Quantitative Verification of Turbulent Particle Pinch

Using only *measured electric field* fluctuations,  
Thomas Birmingham's diffusion model is verified with levitated dipole

Floating Potential ( $\Phi > \pm 150$  V)



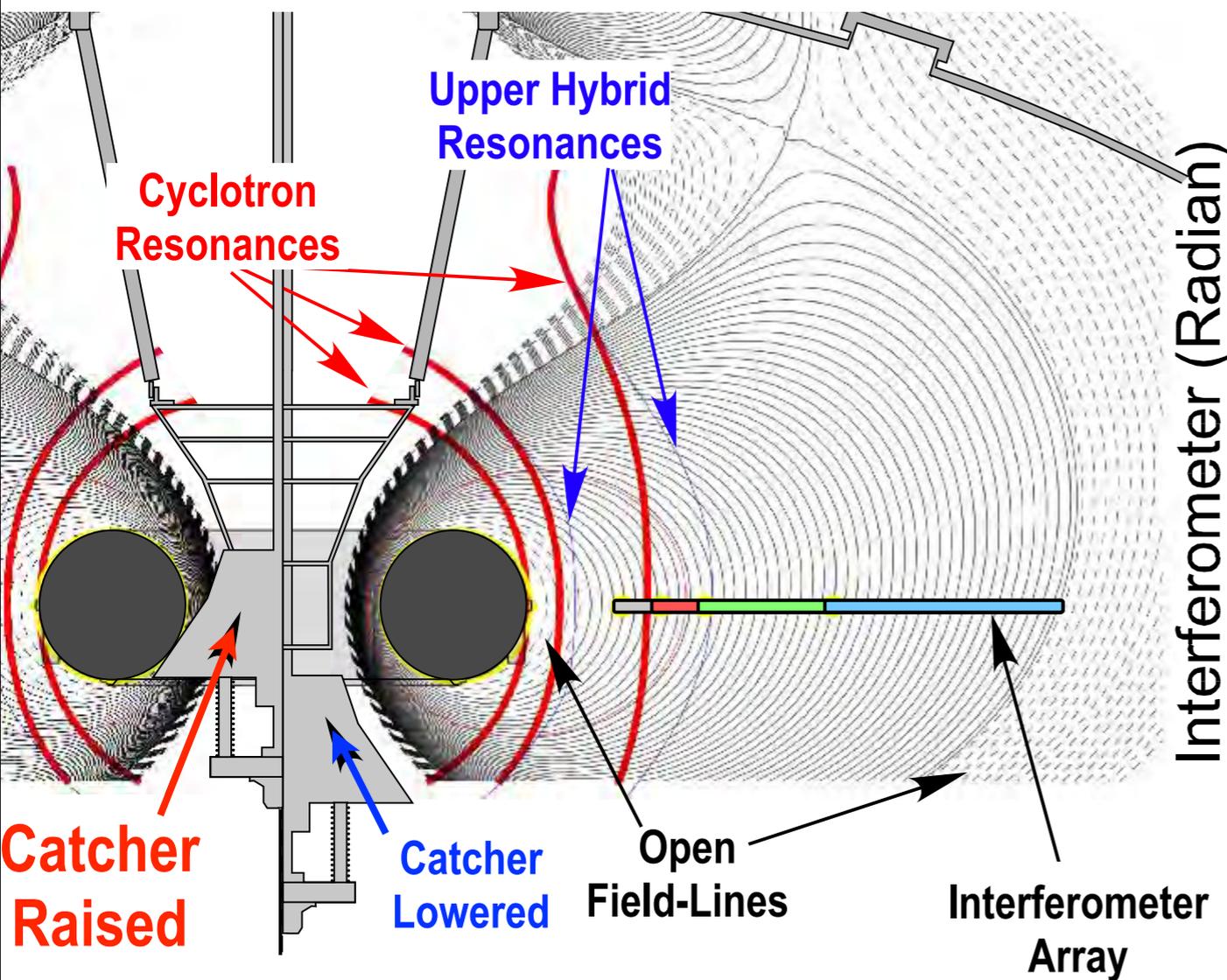
**Edge Probe Array:**

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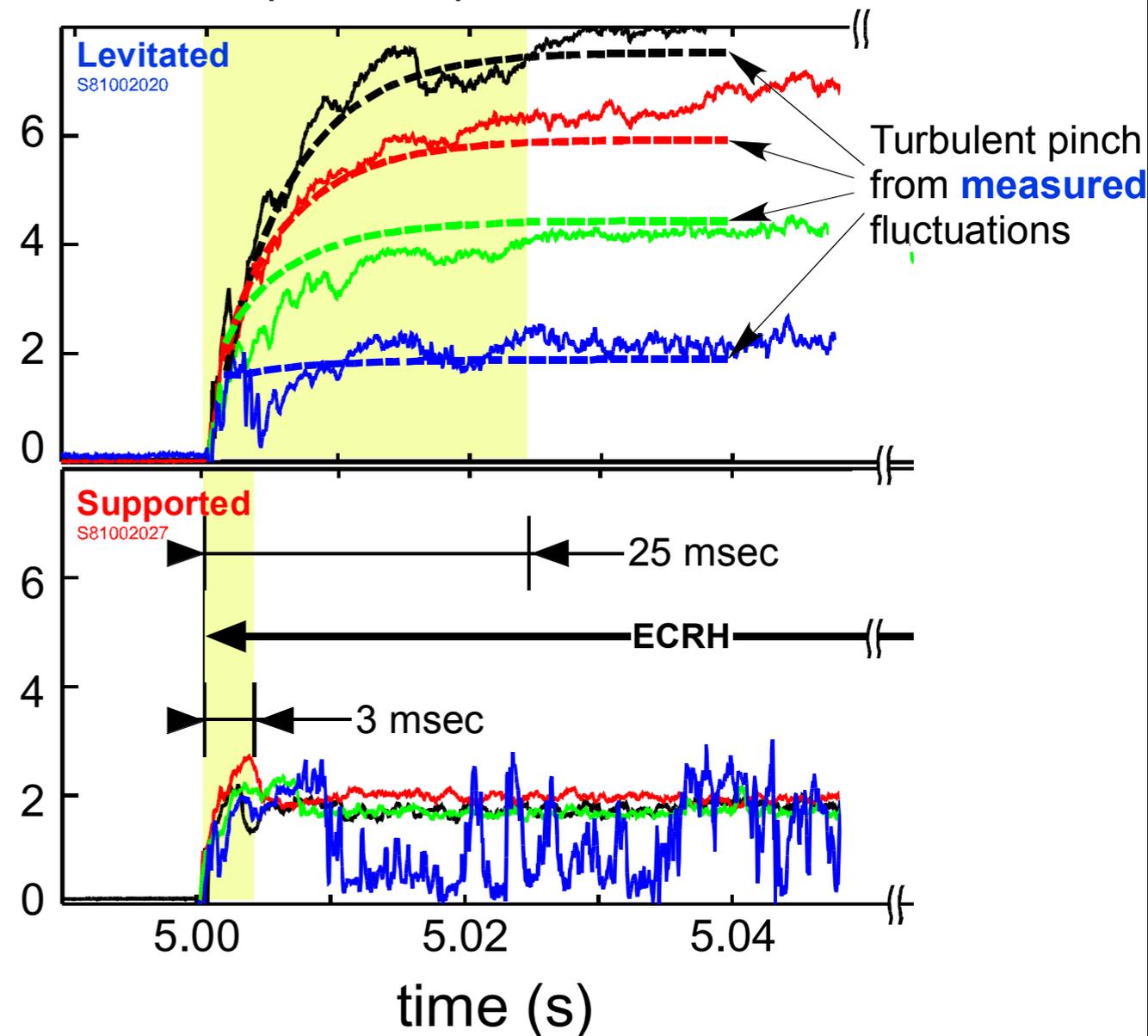
# Quantitative Verification of Inward Turbulent Pinch

$$\frac{\partial(\bar{n}\delta V)}{\partial t} = \langle S \rangle + \frac{\partial}{\partial \psi} D_{\psi} \frac{\partial(\bar{n}\delta V)}{\partial \psi}$$

With levitated dipole, inward turbulent transport sets profile evolution

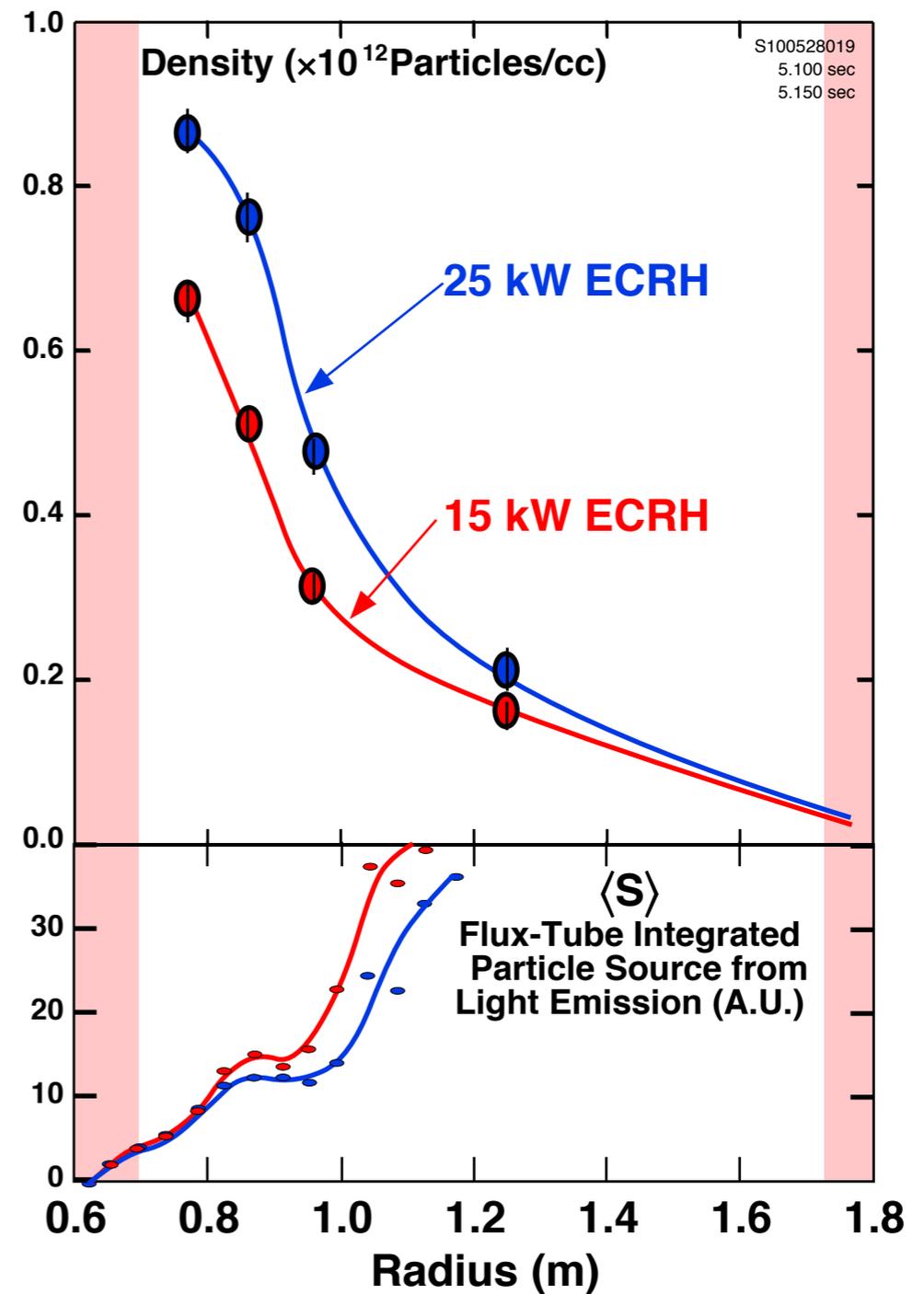
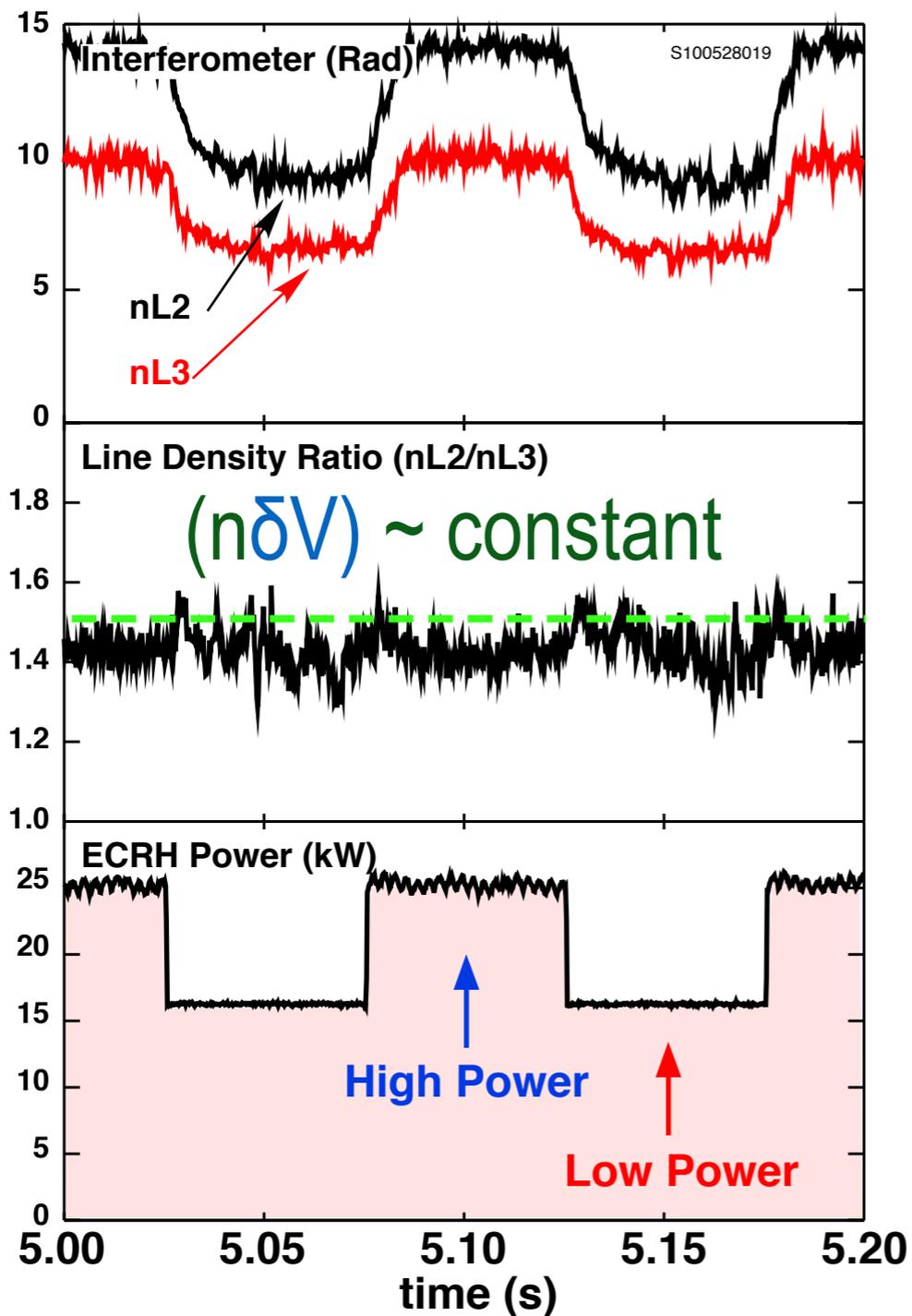


Interferometer (Radian)

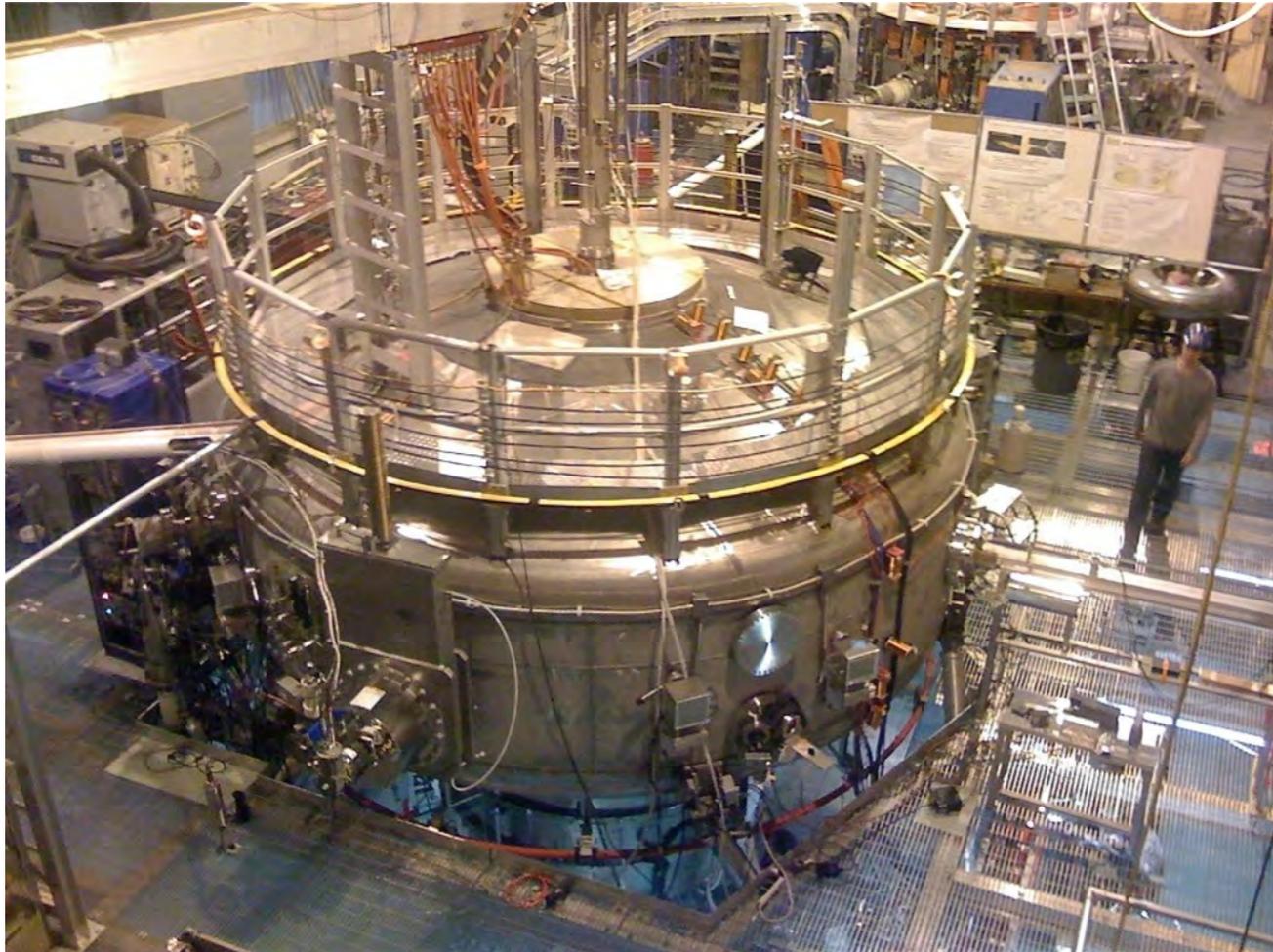


# Heating or gas modulation demonstrates **(Robust)** inward pinch & **Natural** “canonical” profile

- Density increases with power ( $T \sim \text{constant}$ ). Density profile shape is unchanged near  $(n\delta V) \sim \text{constant}$ .
- Gas source moves radially outward. **Inward pinch** required to increase central density.

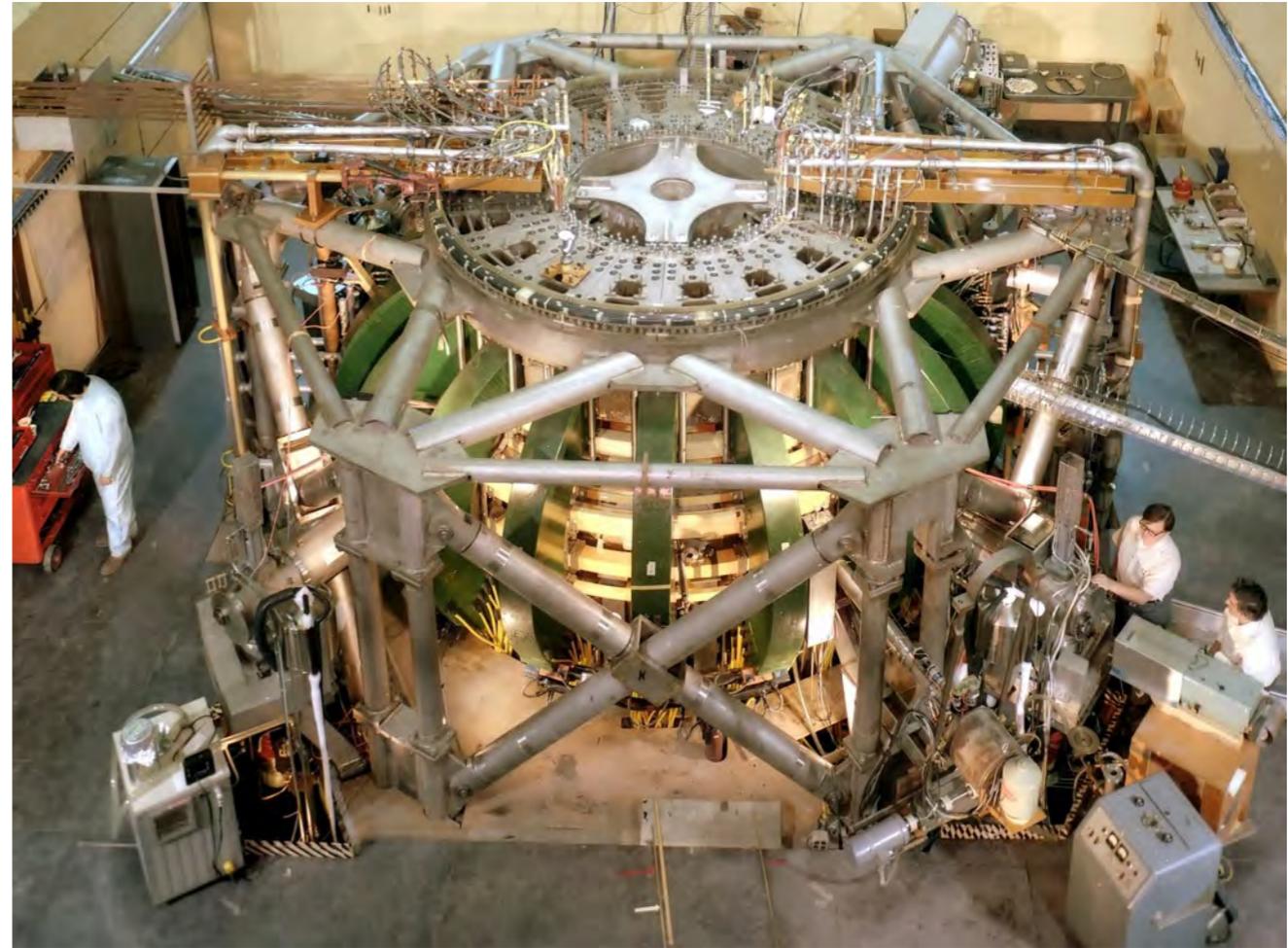


# Turbulent Pinch is a Fundamental Process found in Toroidal Magnetic Systems Including Tokamaks and Planetary Magnetospheres (but, different...)



**Levitated Dipole Experiment (LDX)**

1.2 MA Superconducting Ring  
Steady-State  
25 kW ECRH  
1 MW ICRF (unused)



**Princeton Large Torus (PLT)**

17 MA Copper Toroid  
1 sec pulses  
750 kW Ohmic  
75 kW LHCD  
2.5 MW NBI & 5 MW ICRF

# A (Historic) Density Rise Experiment on PLT

Jim Strachan, et al., Nuc. Fusion (1982)

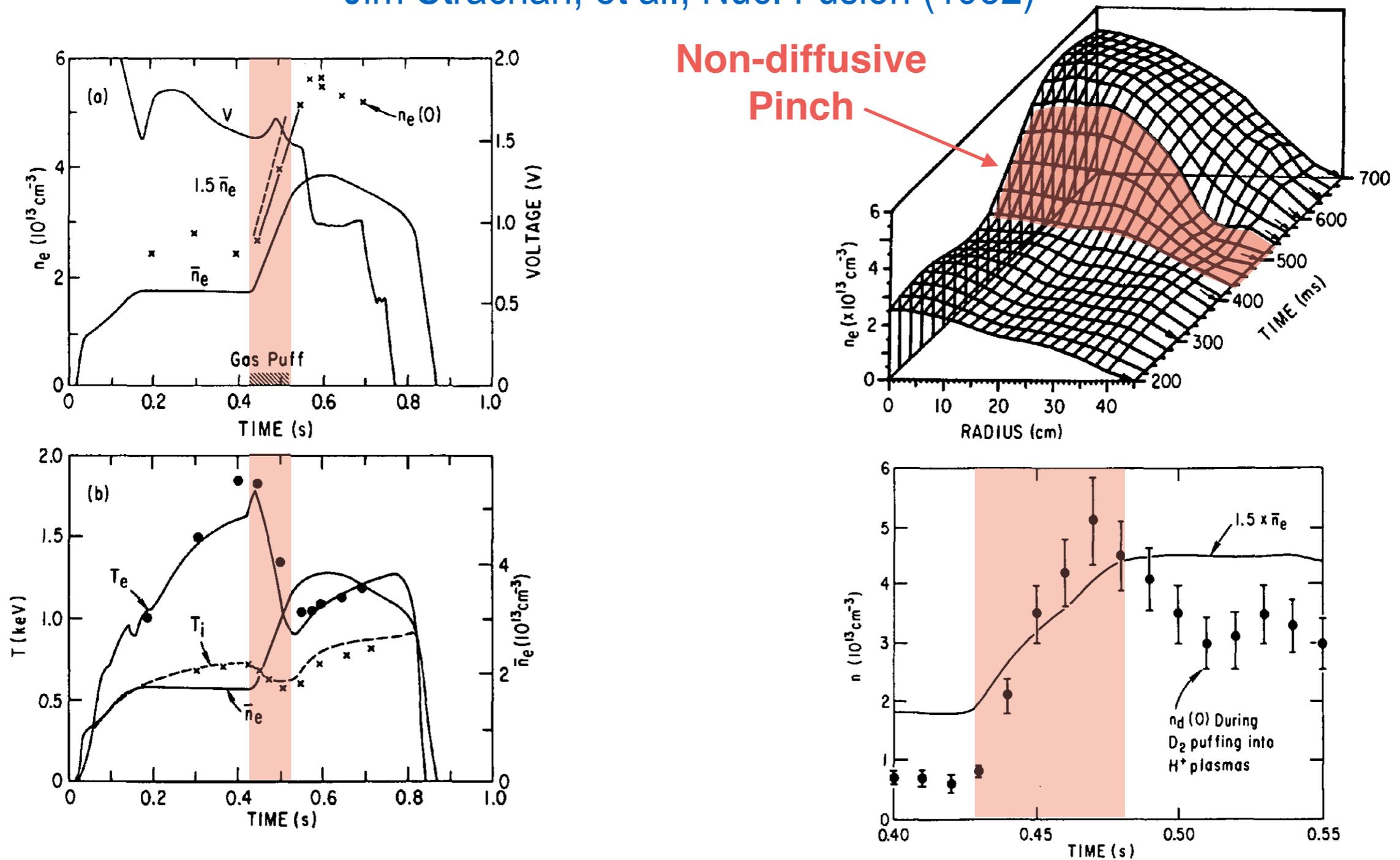


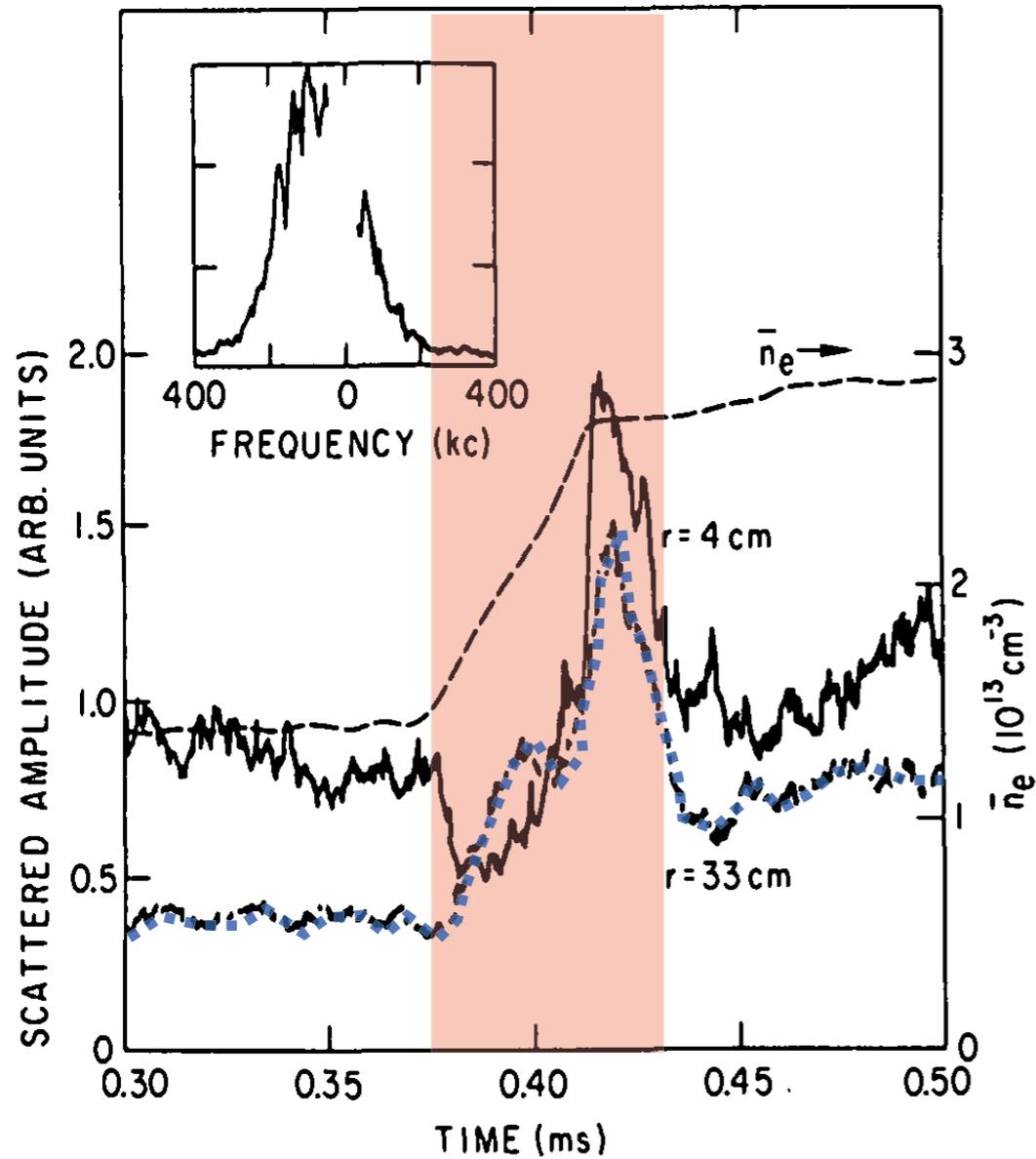
FIG.2. (a) Time evolution of the loop voltage,  $V$ , the line-average density  $\bar{n}_e$ , and the central electron density,  $n_e(0)$  during the density rise. (b) Time evolution of the central electron temperature from  $2\omega_{ce}$  (—), and from TVTS ( $\bullet$ ), with the time evolution of the central ion temperature from neutrons (— —), and from charge exchange (X) during the density rise.

Inward Turbulent Pinch "is necessary to model the experimental results" of peaked density from edge gas source

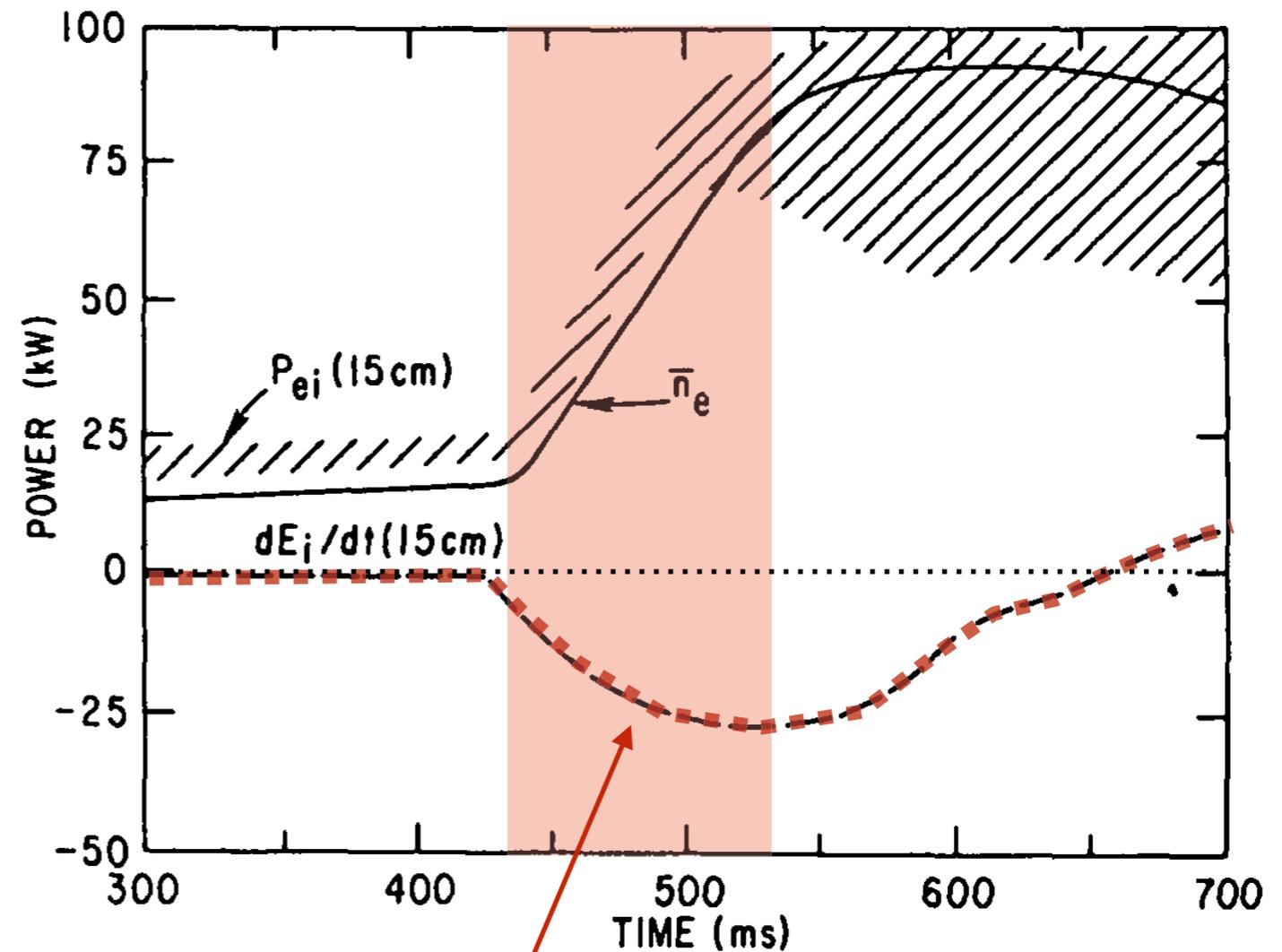
# A (Historic) Density Rise Experiment on PLT

Jim Strachan, et al., Nuc. Fusion (1982)

Enhanced Turbulent Fluctuation Intensity...



... Causing Central Ion Cooling



but gas puff intensifies turbulence and **Outward Ion Energy Flux** accompanies **Inward Turbulent Particle Pinch**

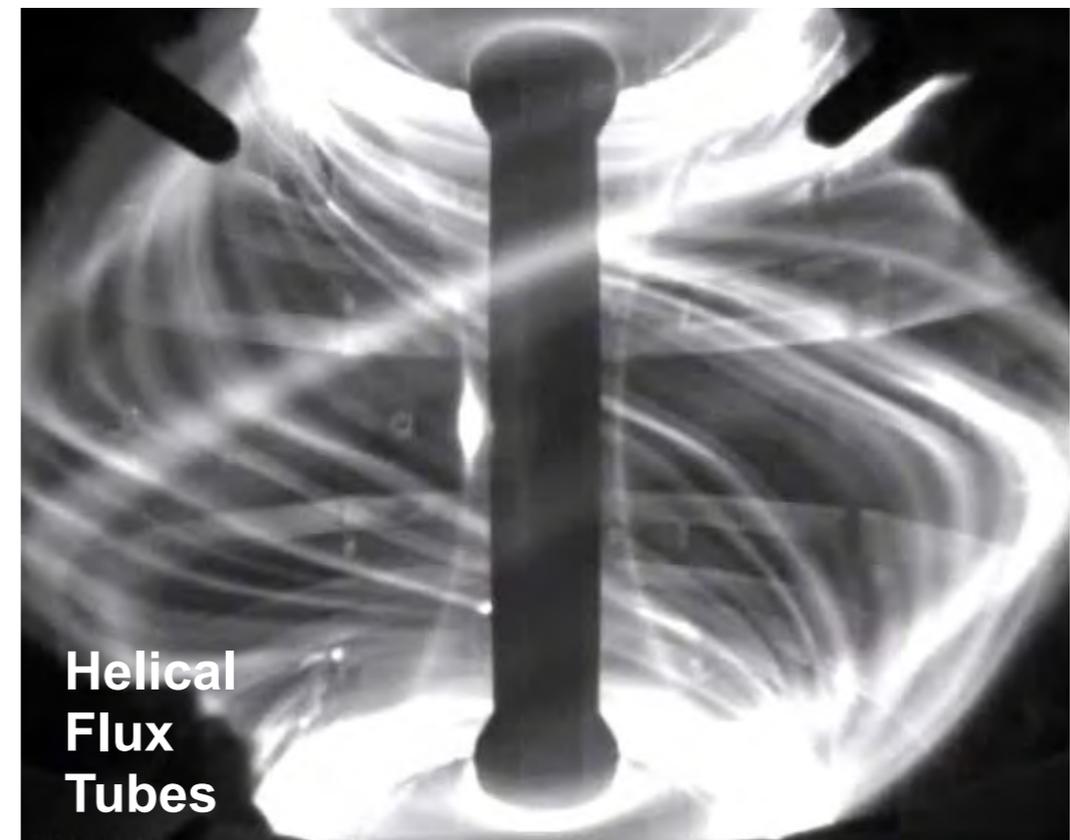
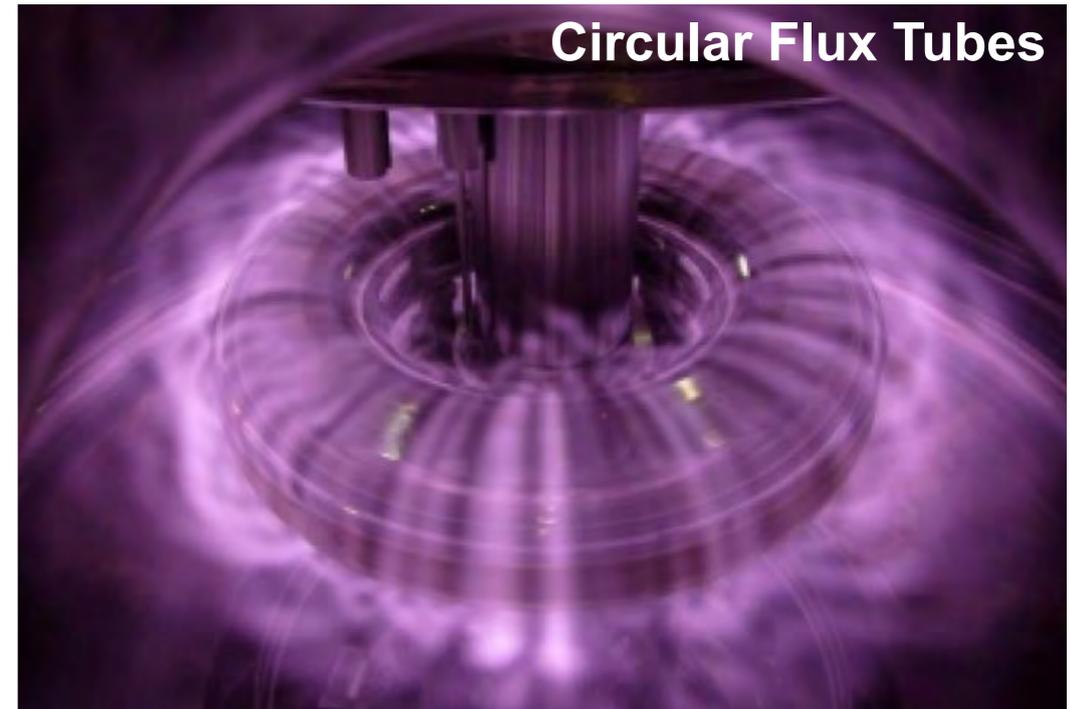
# But, Toroidal Confinement **without Toroidal Field** is different...

- **Dipole...**

- ▶ Interchange (**not drift-ballooning**) sets limits
- ▶  $\beta \sim 100\%$  with  $\omega^* \sim \omega_d$  (**isentropic**,  $\delta(PV^\gamma) \sim 0$ )
- ▶ Flux-tubes convect globally without bending
- ▶ No toroidally circulating particles
- ▶ Peaked profiles with flux tube volume  $\delta V \sim R^4$

- **Tokamak...**

- ▶ Ballooning and kinks set pressure limit
- ▶  $\beta \sim \epsilon/q \approx 5\%$  with  $\omega^* \gg \omega_d$  (**non-isentropic**)
- ▶ Short radial scale of drift waves fluctuations
- ▶ Passing  $\neq$  trapped particles
- ▶ Flat profiles with  $\delta V \sim qR$



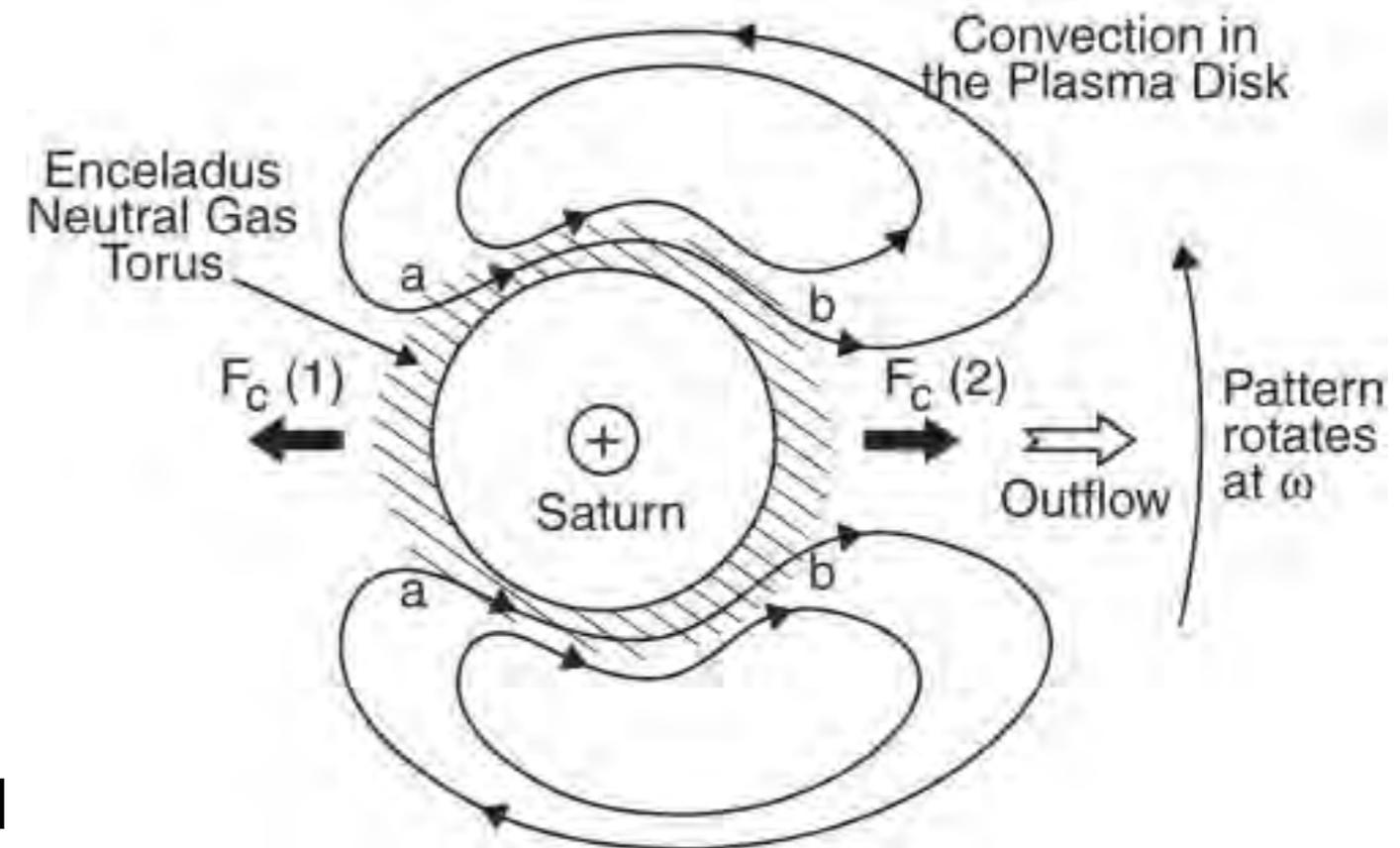
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- **Examples:** exploring plasma dynamics by injection of heat, particles, current, and magnetic perturbations by decreasing ion inertial lengths

# Interchange (or Entropy) Instabilities Always Dominate Turbulent Mixing

- Familiar magnetospheric convection, e.g. Saturnian convection
- Three modes in the laboratory with **same global structure** but different frequencies:
  - ▶ Fast electron gyrokinetic interchange: Collisionless ( $\omega_d \tau_{col} > 10^3$ ) with  $(\mu, J)$  invariance; frequency chirping
  - ▶ Centrifugal interchange Mach  $\sim 1$ : Semi-collisional ( $\Omega \tau_{col} \sim 1$ ) with  $(nV)$  invariance
  - ▶ Interchange/entropy modes: Semi-collisional ( $\omega_d \tau_{col} \sim 1$ ) with  $(PV^\gamma)$  &  $(nV)$  invariance

Gurnett, et al., *Science* **316**, 442 (2007)



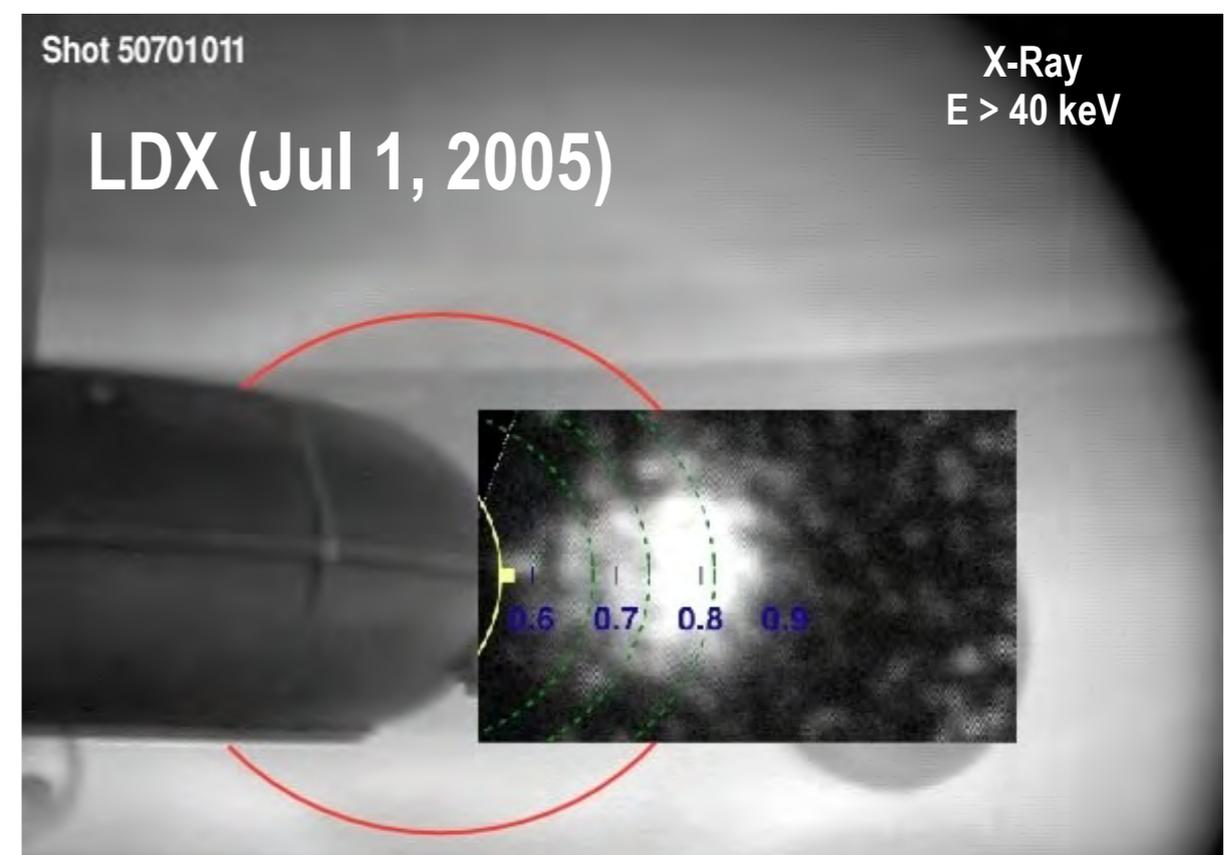
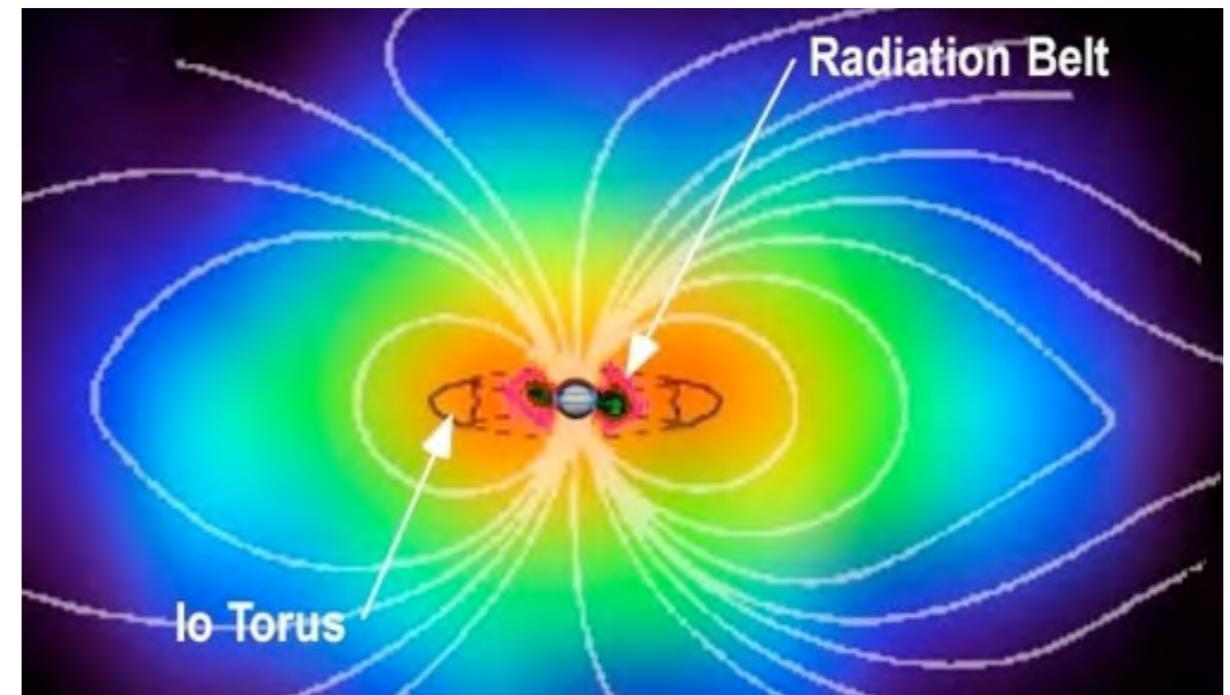
$$\delta(PV^\gamma) \sim \delta(nV) \sim 0$$

# Trapped energetic particles very well confined by dipole magnetic field

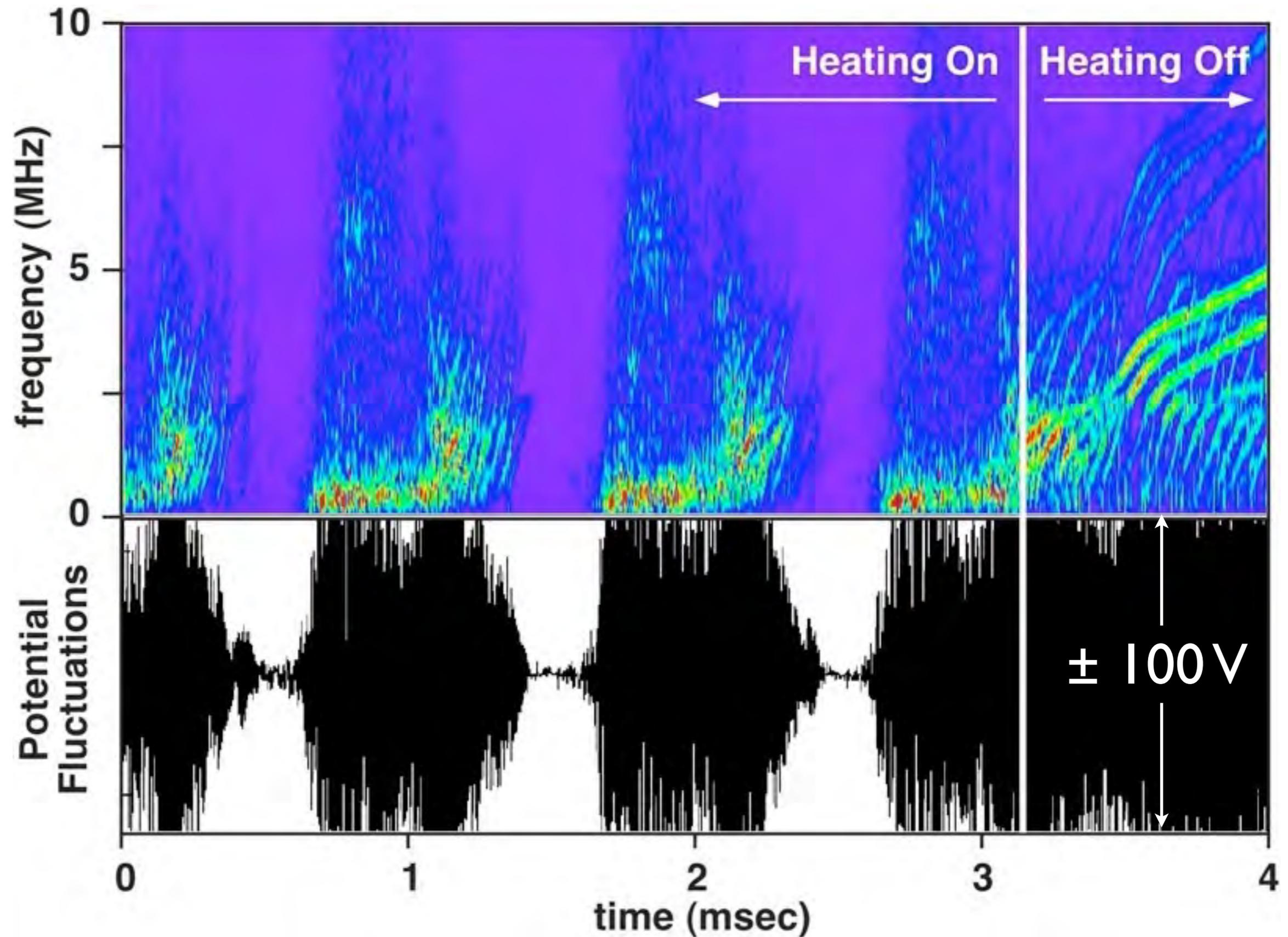
Cassini at Jupiter (Dec 30, 2000)

*The natural high beta in planetary magnetospheres can be achieved in the laboratory. Steady-state.*

- Garnier, POP (1999) shows equilibria with  $\beta > 100\%$  possible
- Garnier, POP (2006) reports peak beta 20% achieved
- Garnier, NF (2009) reports peak beta doubles with levitation
- ➔ Saitoh, JFE (2010) reports peak beta 70% achieved in RT-1

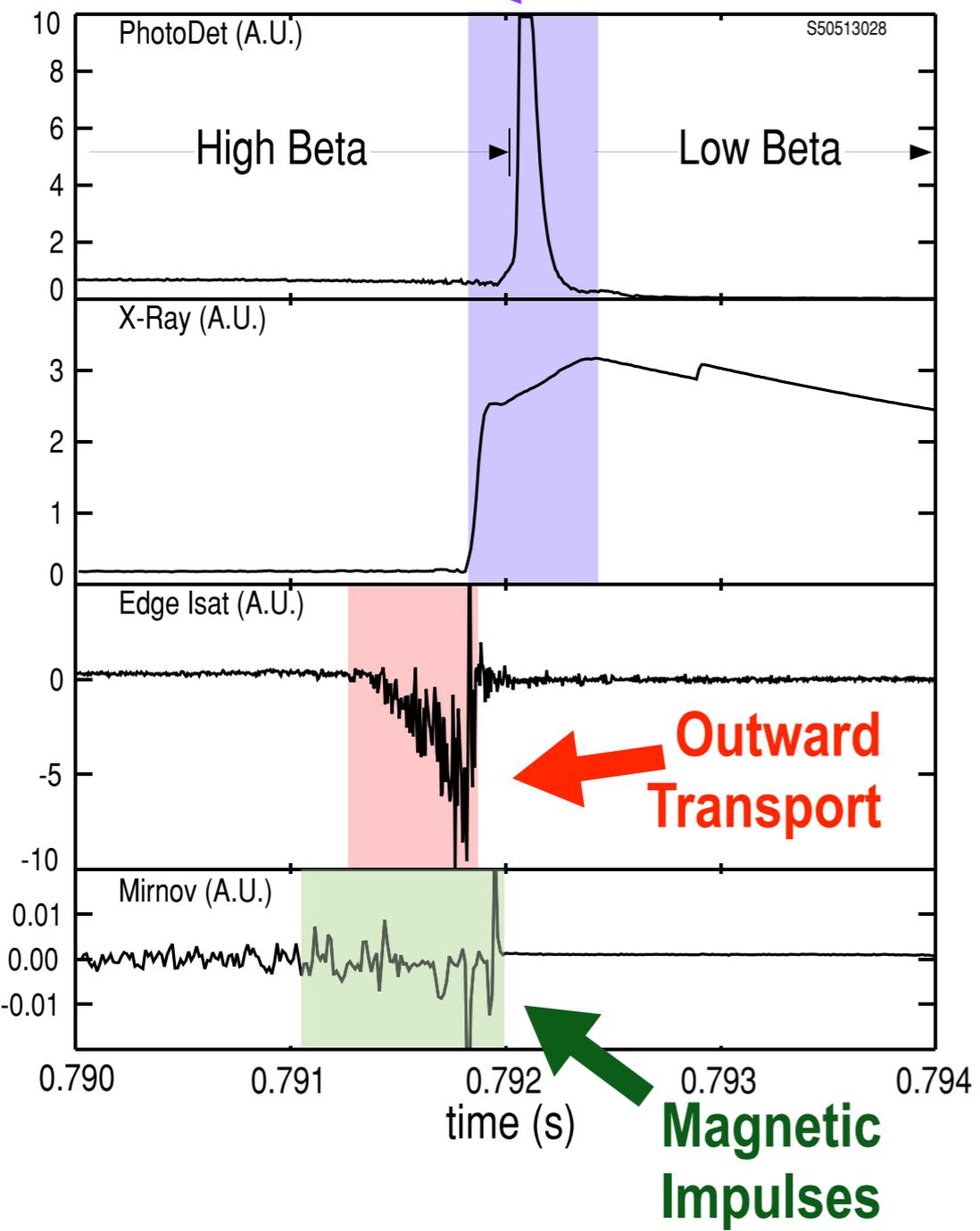


# Drift-Resonant (Hot Electron) Interchange Instability

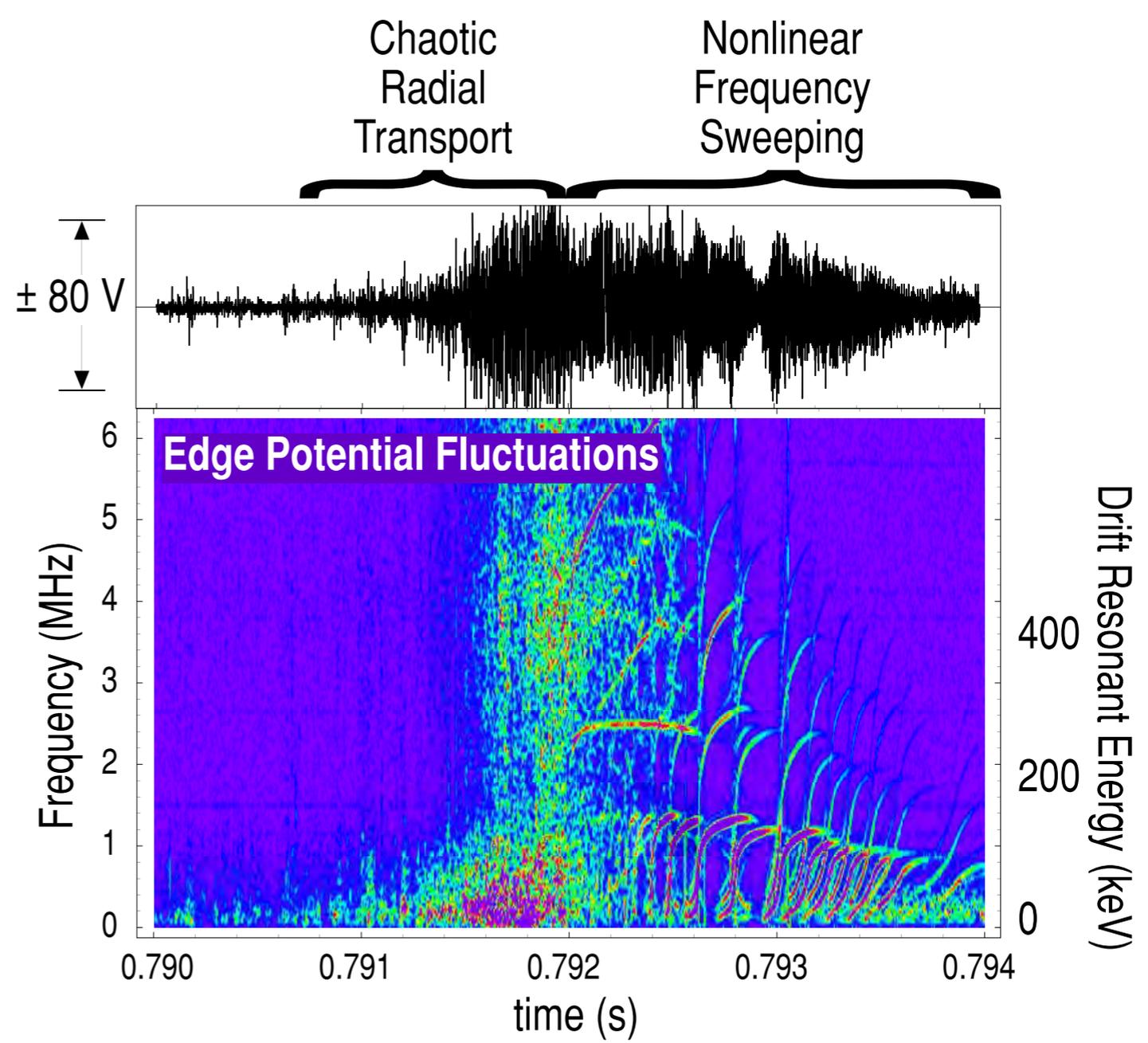


# Kinetic Interchange Drift Mode can also appear in LDX with $\beta \sim 40\%$ “Artificial Radiation Belt”

Inward Transport

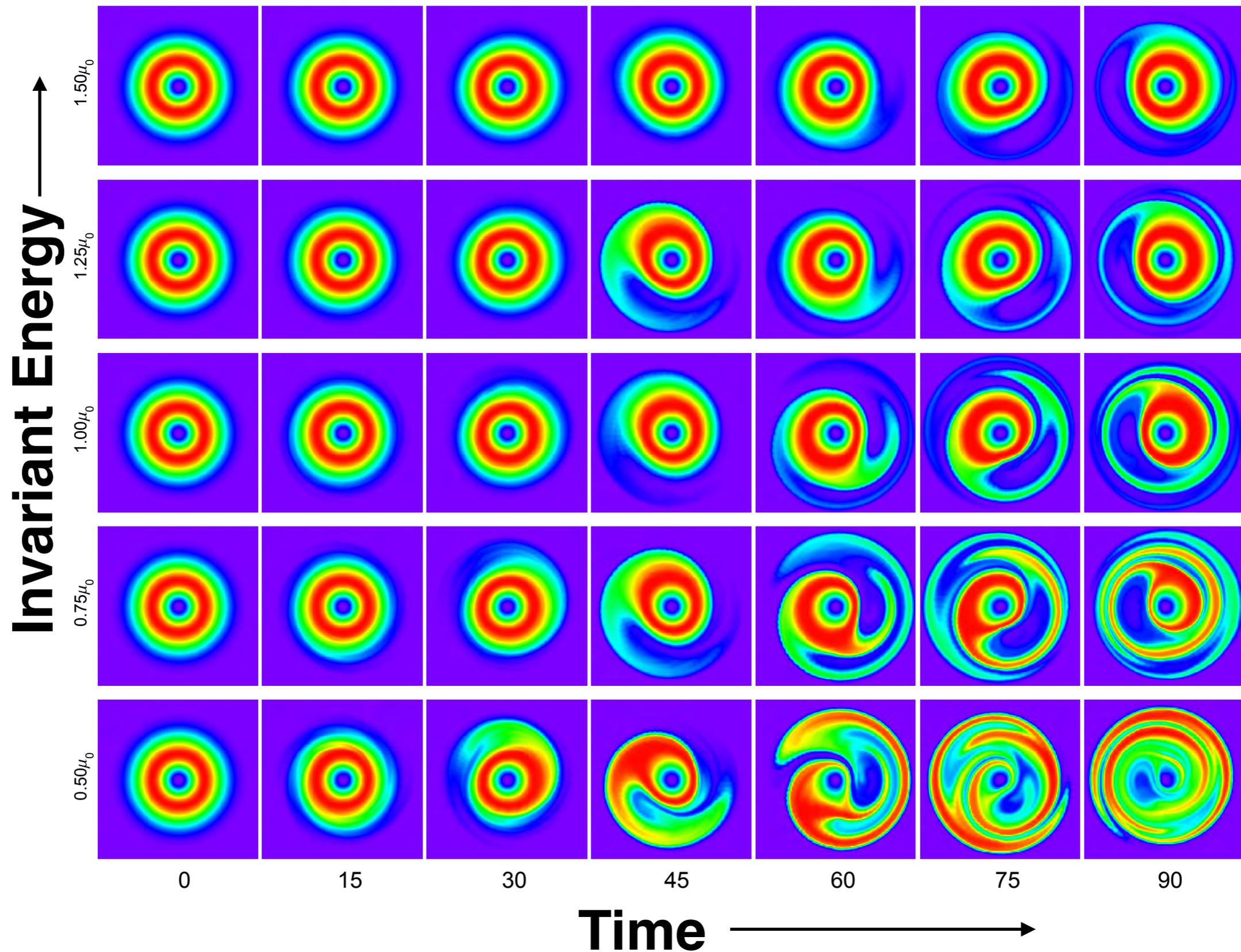


Fast drift-resonant instability resonates with fast electrons causing rapid radial transport...



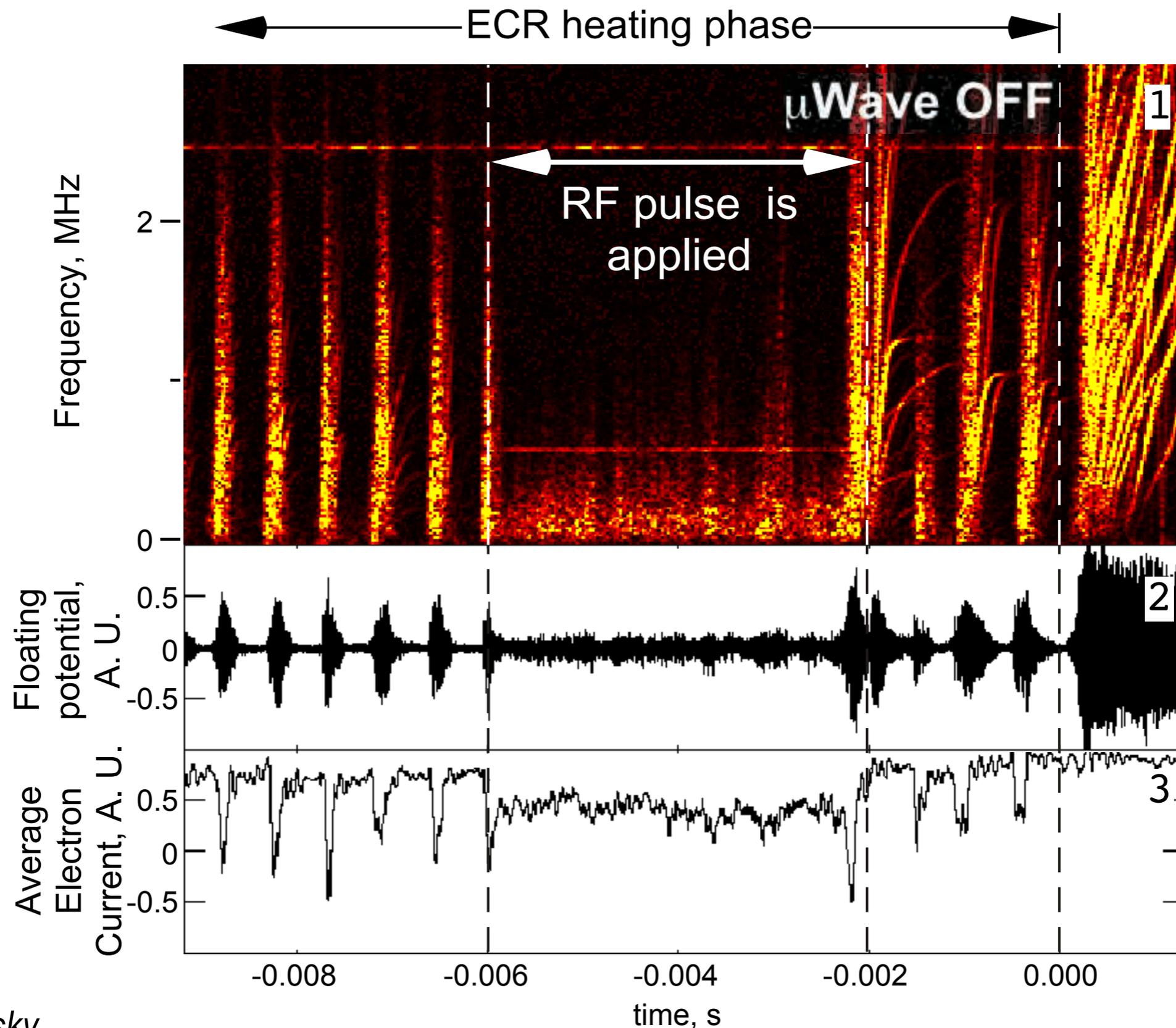
# Interchange Drift Resonance $(\mu, J) \sim 1/L^2$

*Well-modeled with global, nonlinear Bounce-Averaged gyrokinetic simulation...*



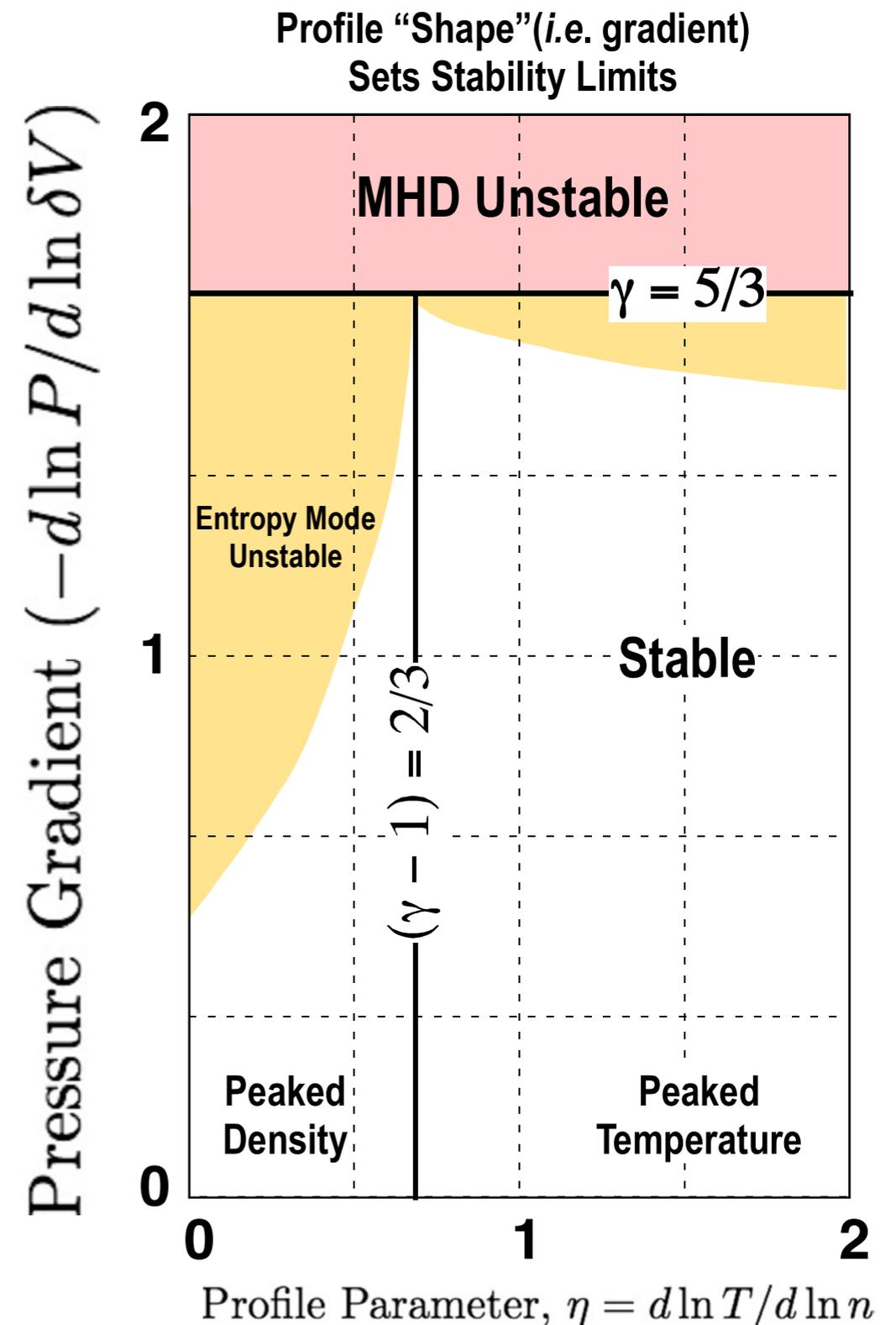
# “Chorus” Injection Fills-in Phase-Space Holes

*Well-modeled with global, nonlinear Bounce-Averaged gyrokinetic simulation...*



# Low frequency interchange & Entropy modes dominate Semi-collisional thermal plasma dynamics

- Interchange modes set pressure and density gradient limits in dipole-plasma (*not* ballooning-drift)
- **Entropy mode changed our thinking:** not just pressure and density gradients, also  $\eta = d(\ln T)/d(\ln n)$  (Kesner, *POP*, 2000; Kesner, Hastie, *POP*, 2002)
- Entropy modes generate zonal flows and self-regulate transport levels (Ricci, Rogers, Dorland, *PRL*, 2006)
- Fluctuations disappear with flat density profiles (Garnier, *JPP*, 2008; Kobayashi, et al., *PRL*, 2009)
- **Measurements show fluctuations throughout plasma** (*Nature-Physics*, 2010); inverse energy cascade (*POP*, 2009); intermittency (*PRL*, 2010)



# Turbulence drives plasma to steep profiles and creates “Canonical” Profiles: Self-Organization

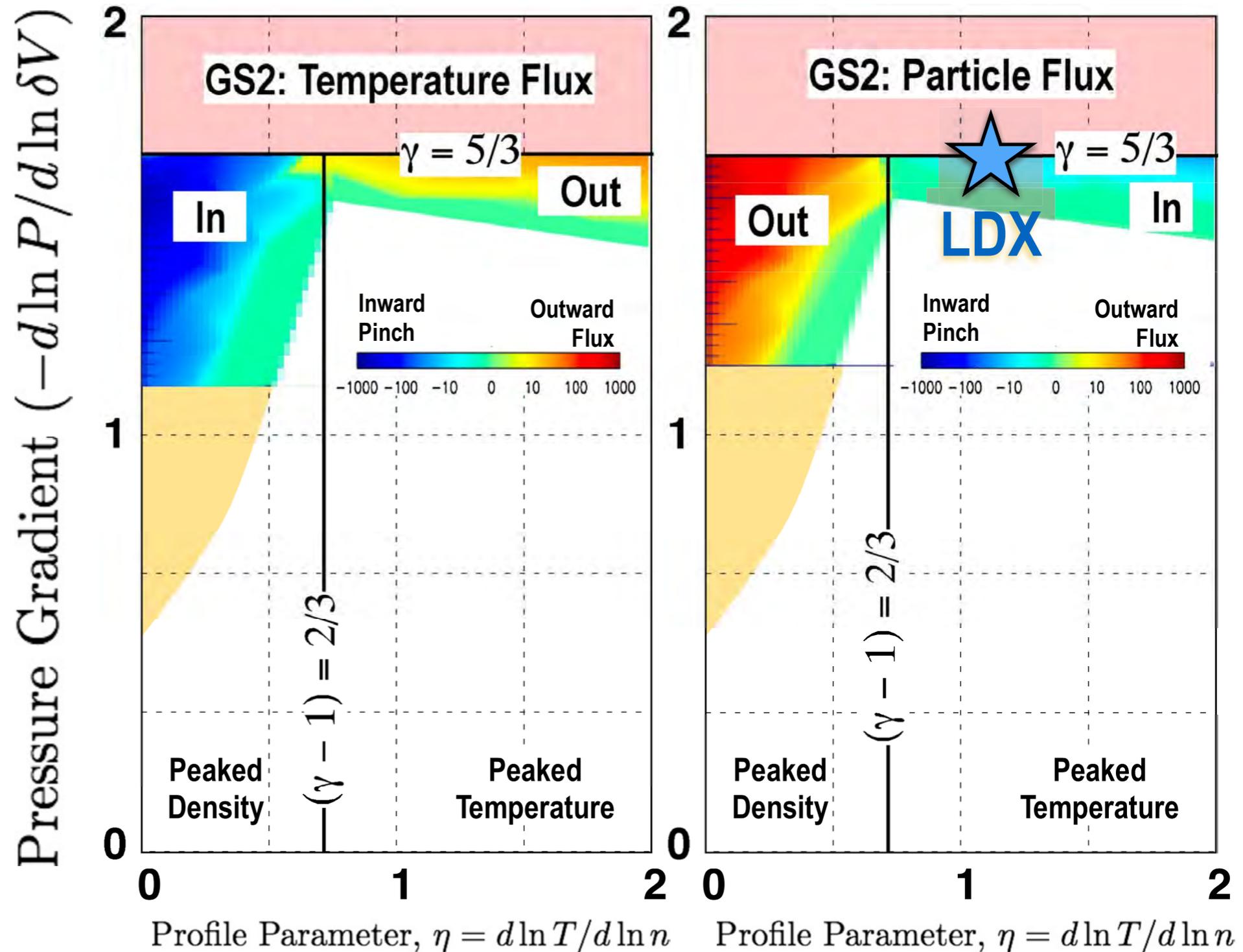
Gyrokinetic (GS2) simulations show turbulence drives particles or heat to maintain uniform entropy density

Kobayashi, Rogers, Dorland, *PRL* (2010)

$$\eta = \frac{d \ln T}{d \ln n} \rightarrow \frac{2}{3}$$

$$-\frac{d \ln n}{d \ln \delta V} \rightarrow 1$$

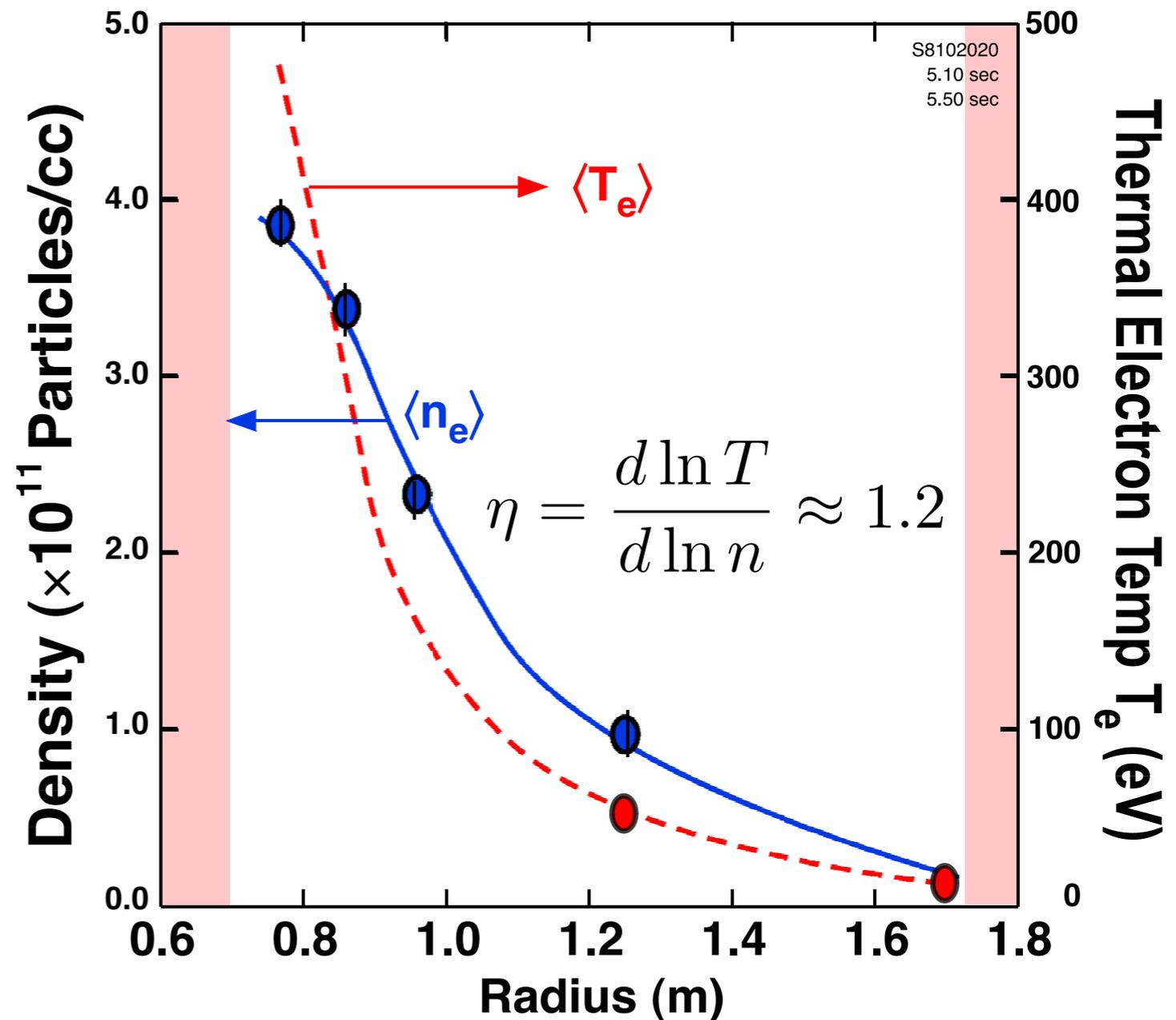
$$-\frac{d \ln P}{d \ln \delta V} \rightarrow \frac{5}{3}$$



# Turbulence Maintains Centrally-Peaked Self-Organized “Canonical” Profiles

$$-\frac{d \ln P}{d \ln \delta V} = \gamma = \frac{5}{3}$$

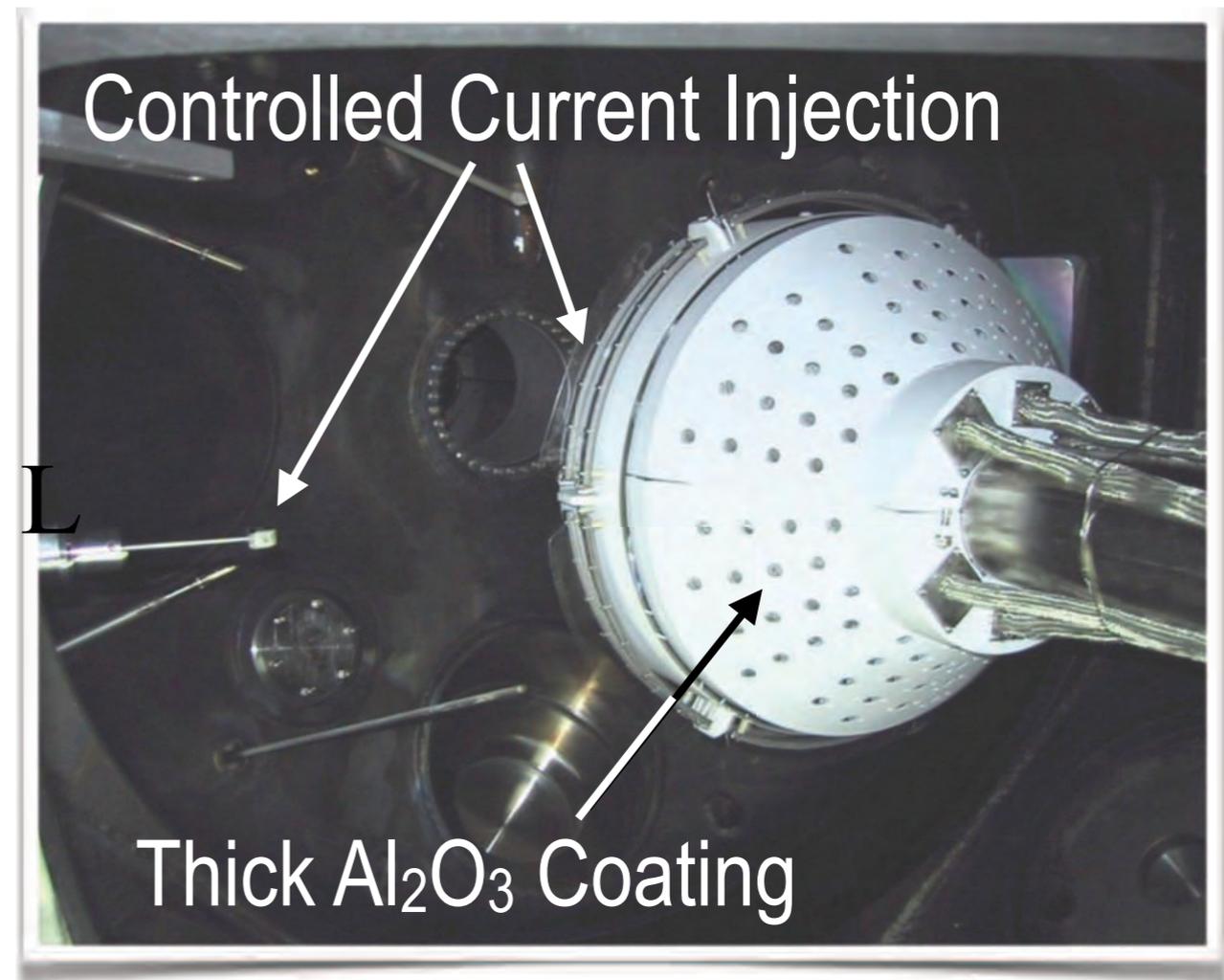
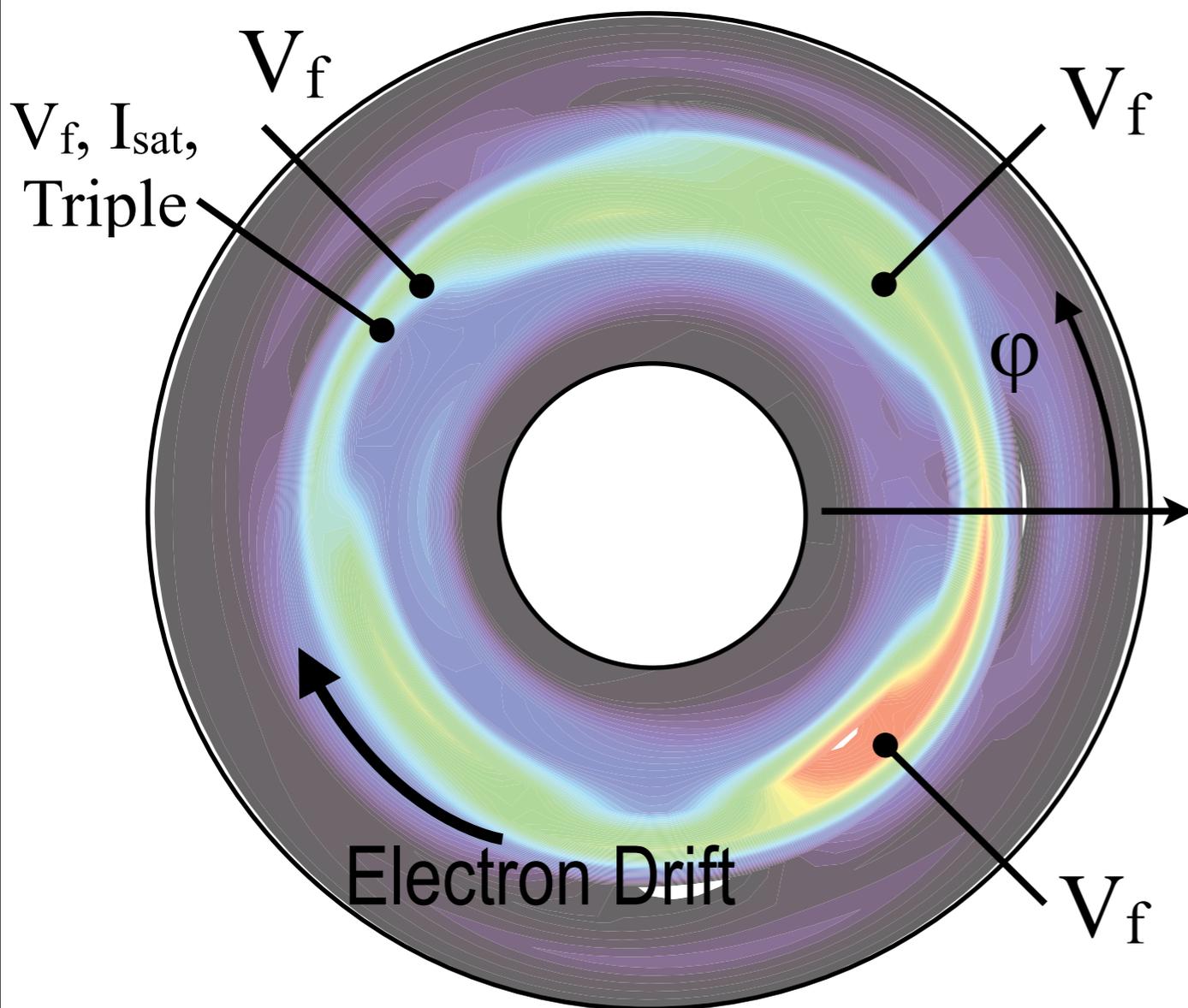
- Thermal plasma energy  $W_{\text{th}} \approx 100$  J with 11 kW ECRH.
- Measured *edge*  $T_e \approx 14$  eV, density profile, and stored energy, require *central*  $T_e \sim 0.5$  keV
- Outward thermal flux sustains inward particle flux,  $\eta \sim 1.2$



Boxer, *et al.*, *Nature Phys.* (2010)

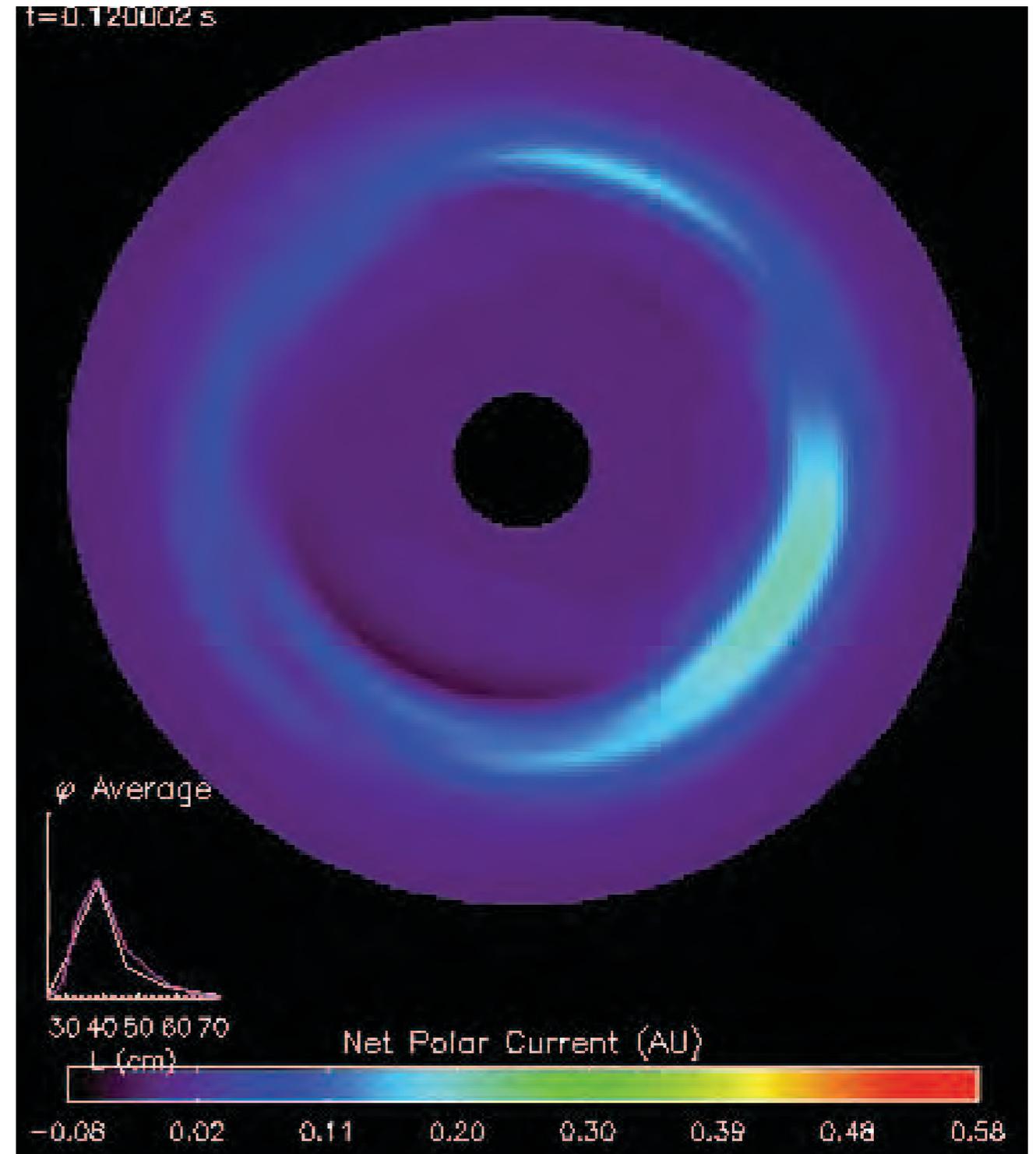
# Polar Imaging of Plasma Dynamics

*Investigations of Interchange/Entropy Mode Turbulence*



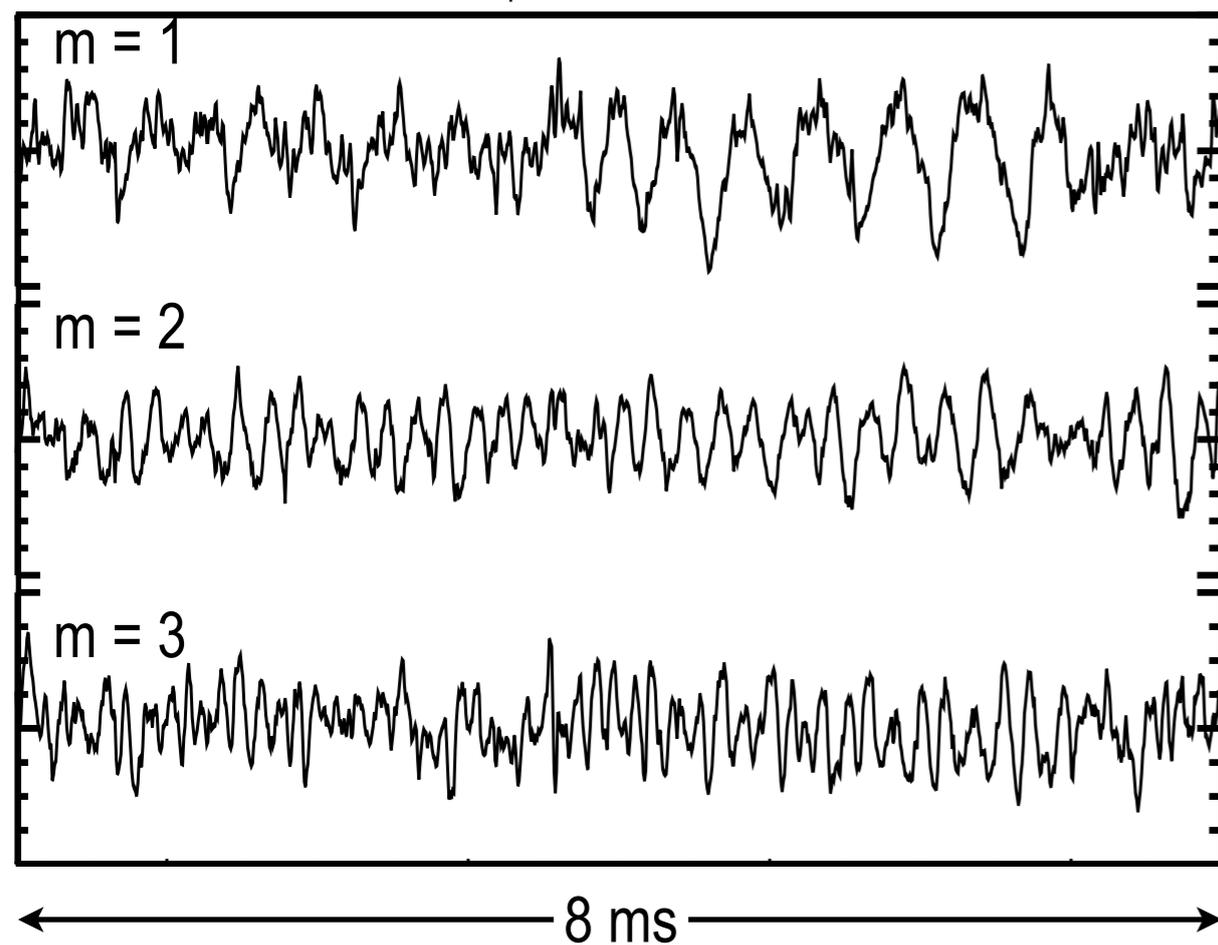
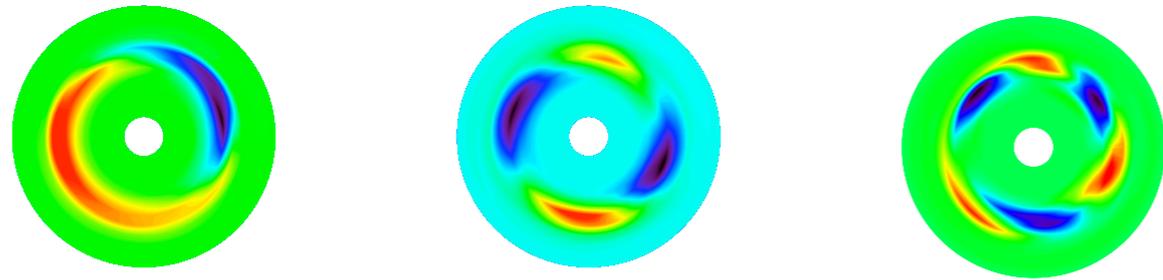
# High Speed Imaging of Interchange/Entropy Mode Turbulence at 0.5 Mfps

- Detectors biased to collect ion current
- Visualize turbulence
- Density fluctuations rotate in electron drift direction with random amplitude and phase modulations
- Compute turbulence cascade and compare with nonlinear simulations



# Low-Frequency Turbulent Convection: Detailed Observation of Particle Transport Process

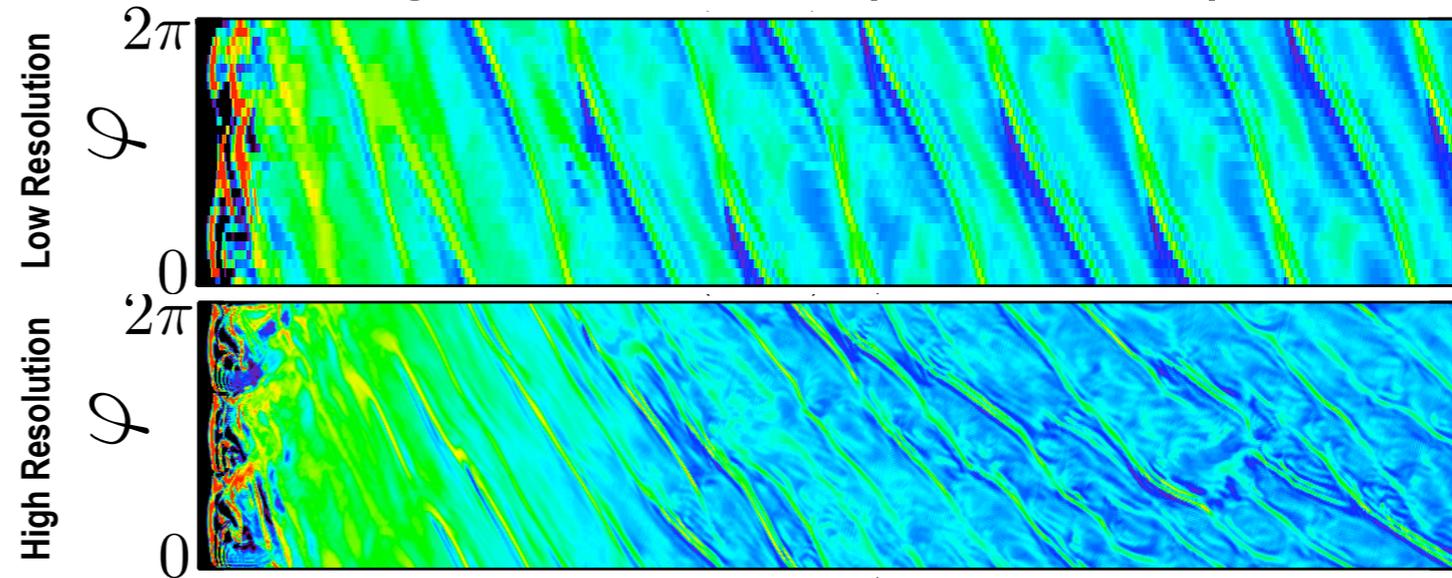
*Well-modeled with global, nonlinear Bounce-Averaged gyrokinetic simulation...*



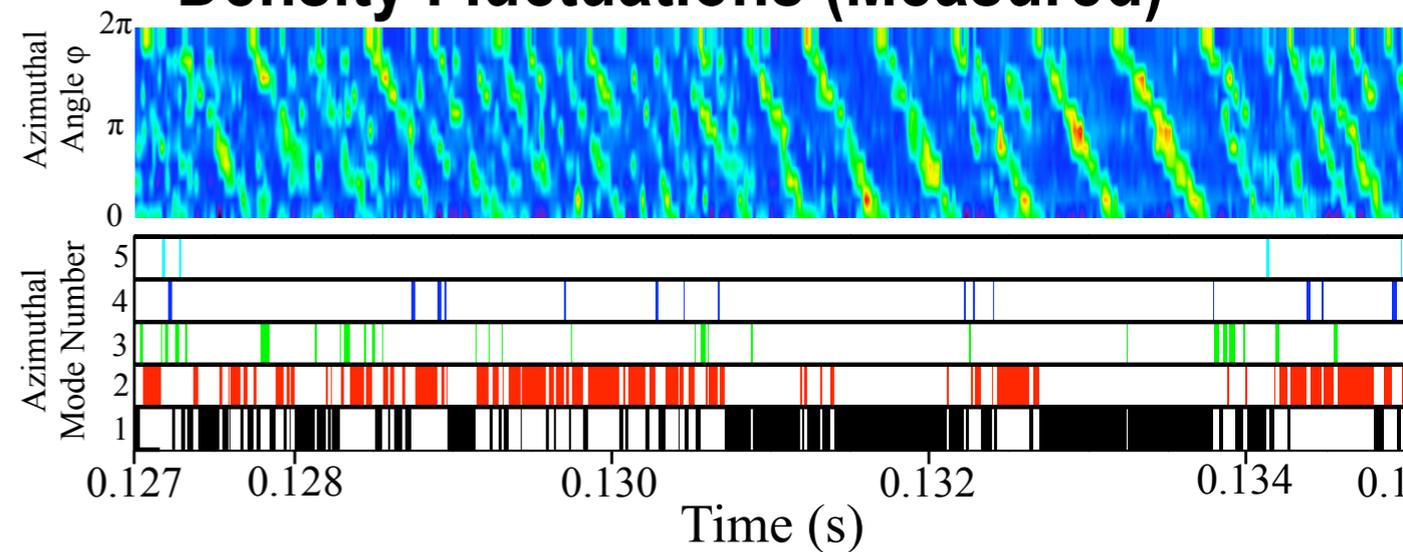
8 ms

Convective Structures Dynamics

## Density Fluctuations (Simulation)

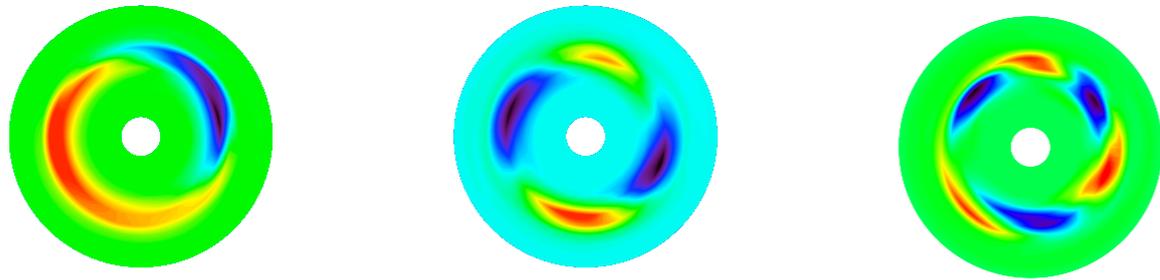


## Density Fluctuations (Measured)

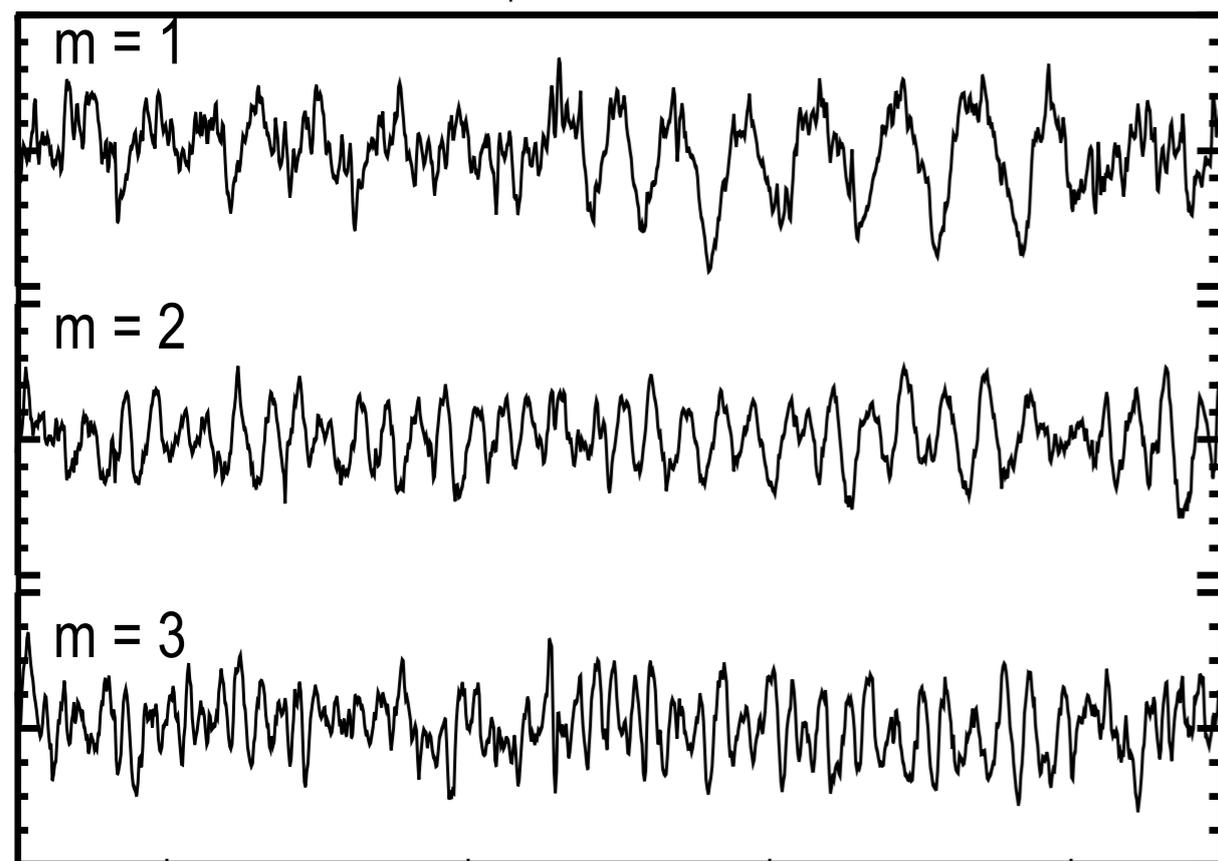


Time (s)

# Low-Frequency Turbulent Convection: Detailed Observation of Particle Transport Process

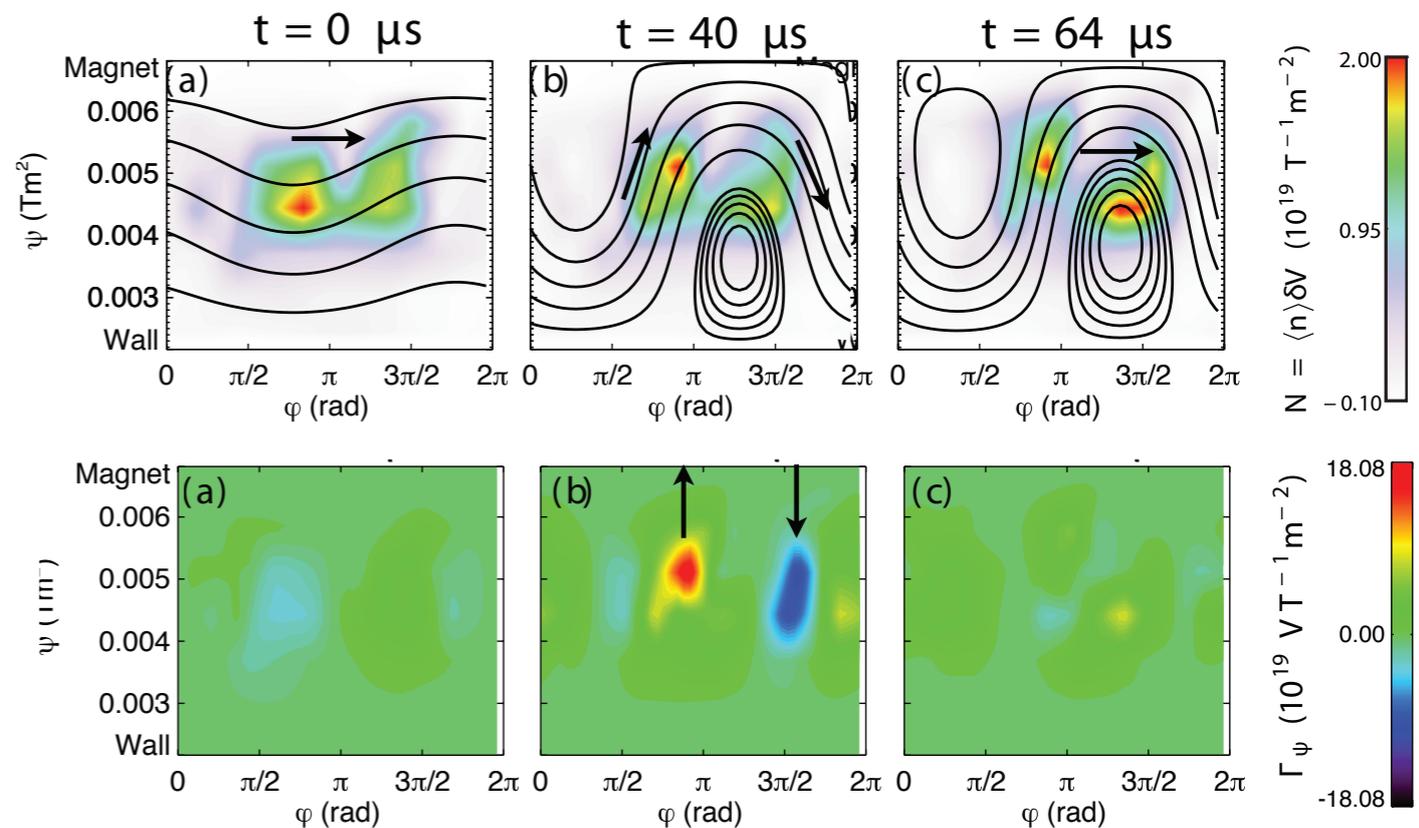


Interchange Transport of  
“**Inward**” and “**Outward**” Moving  
Plasma-Filled Flux Tubes



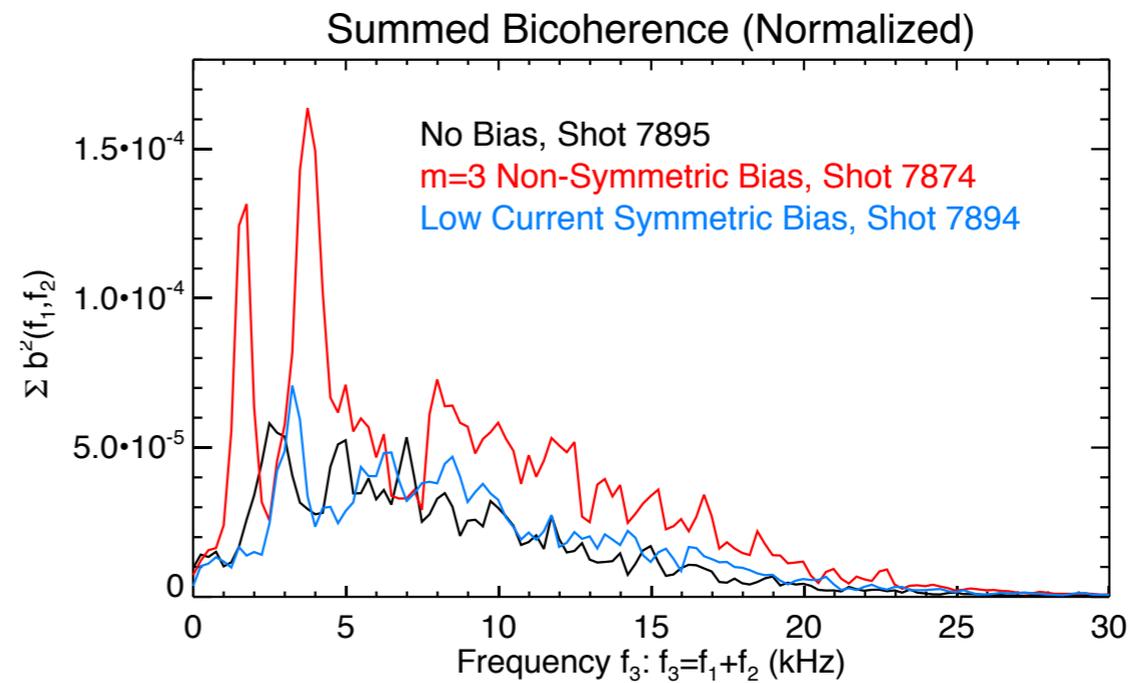
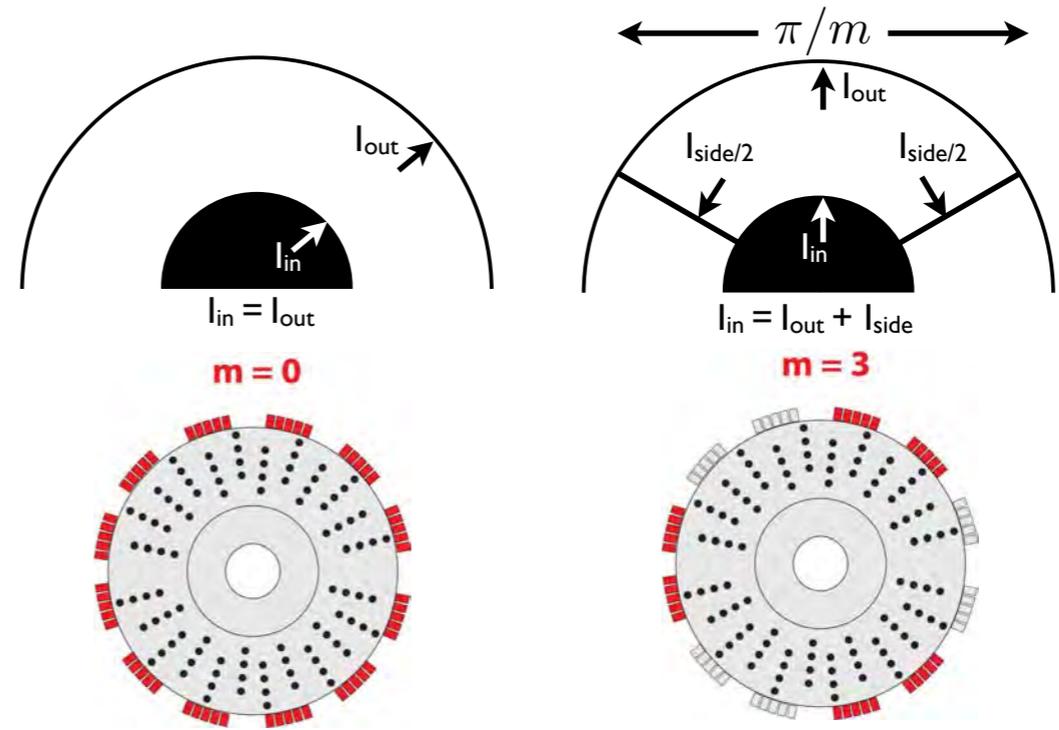
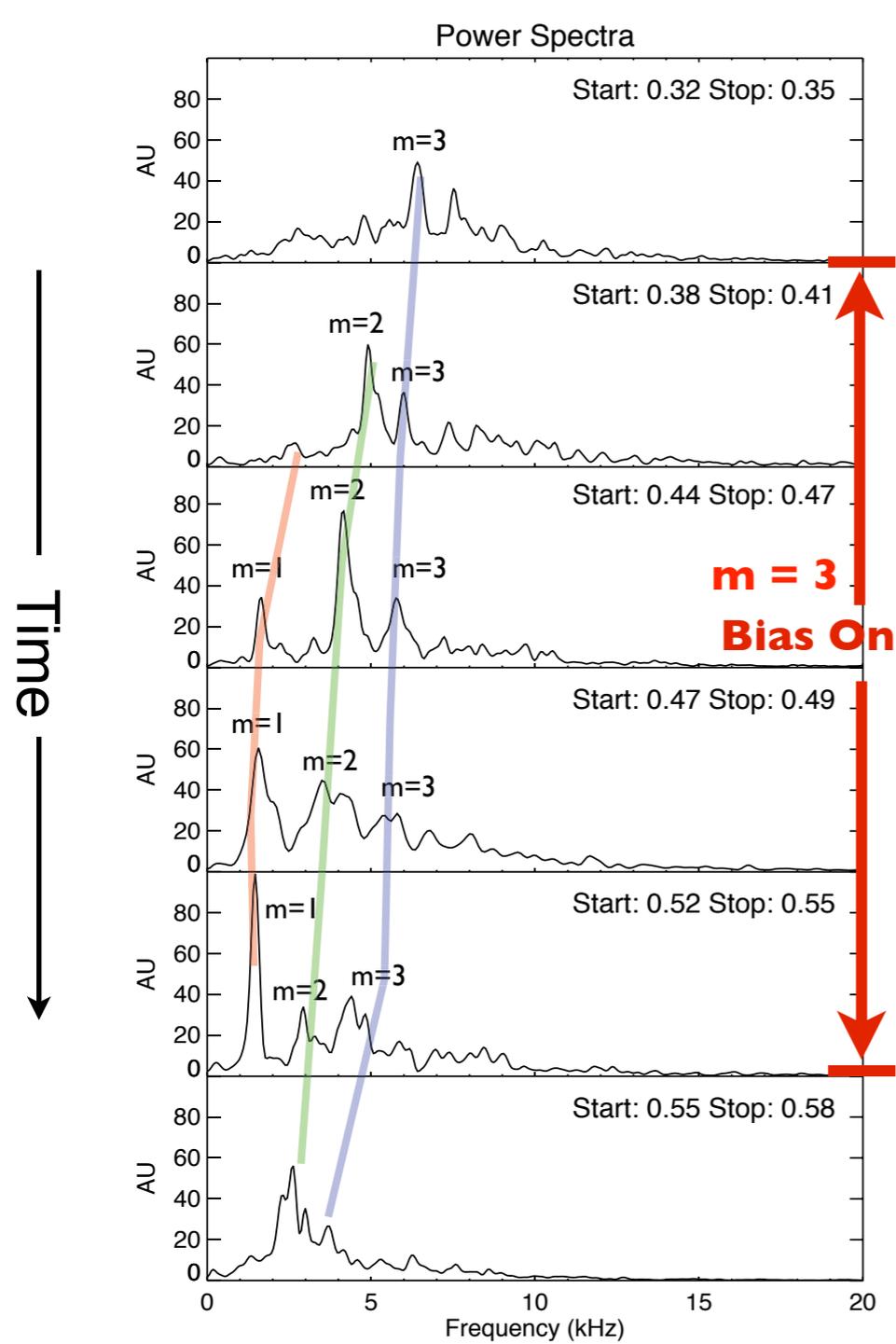
← 8 ms →

Convective Structures Dynamics

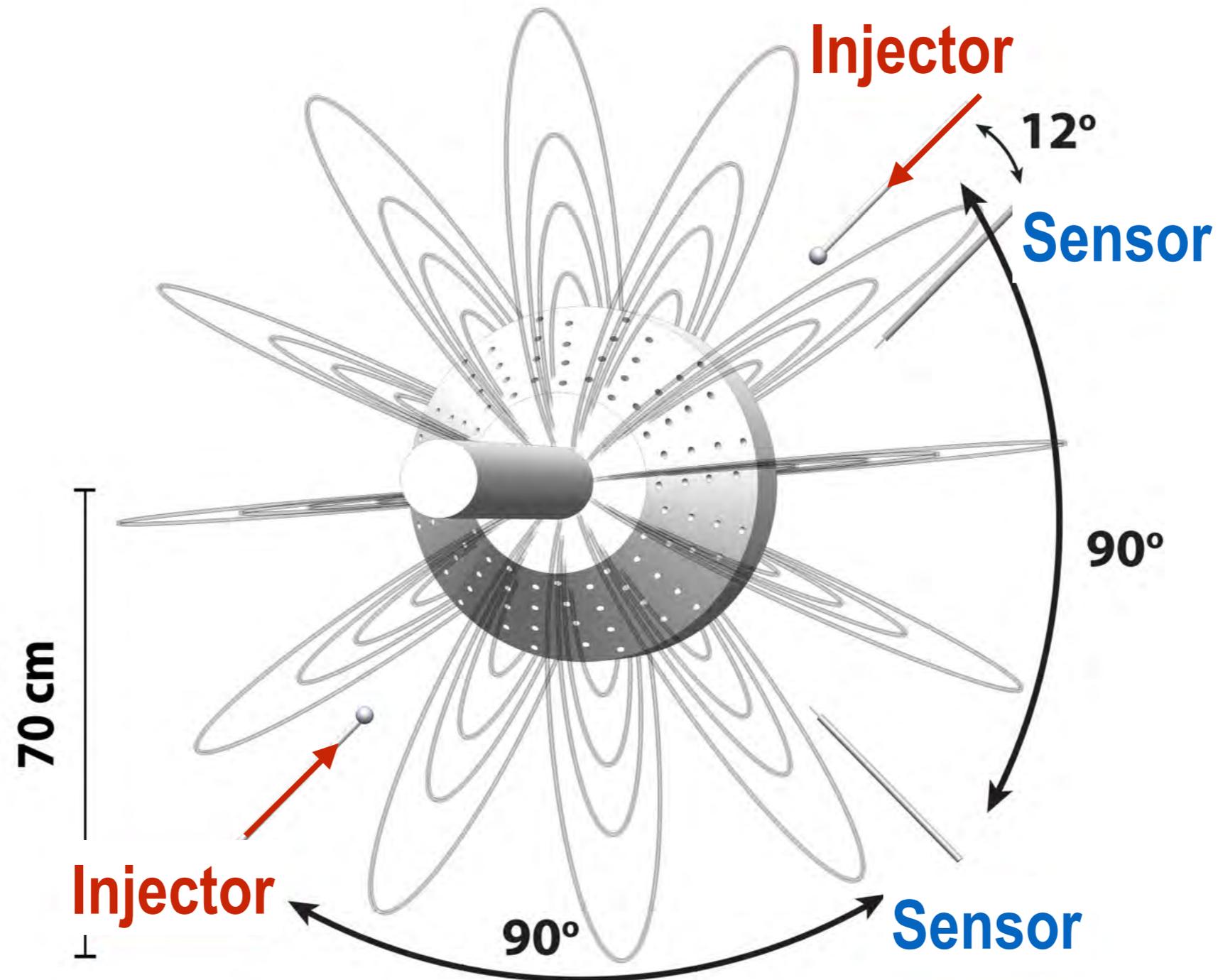


Chaotic Interaction between  
Convective  $E \times B$  Streamlines and  
Plasma Density Perturbations

# Symmetry Breaking and the 2D Inverse Energy Cascade.

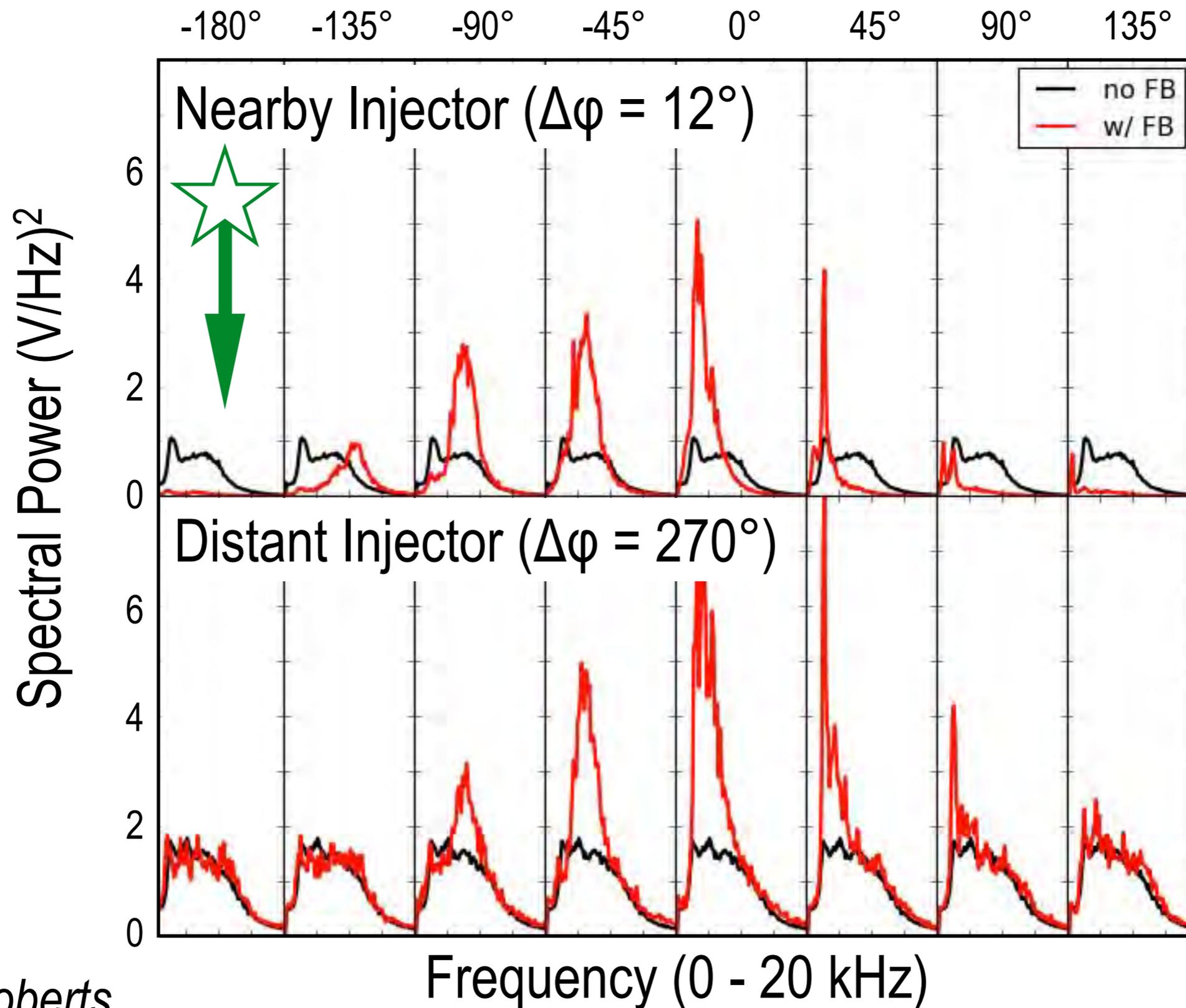


# Local Current Injection to Explore Interchange/ Entropy Mode Turbulence

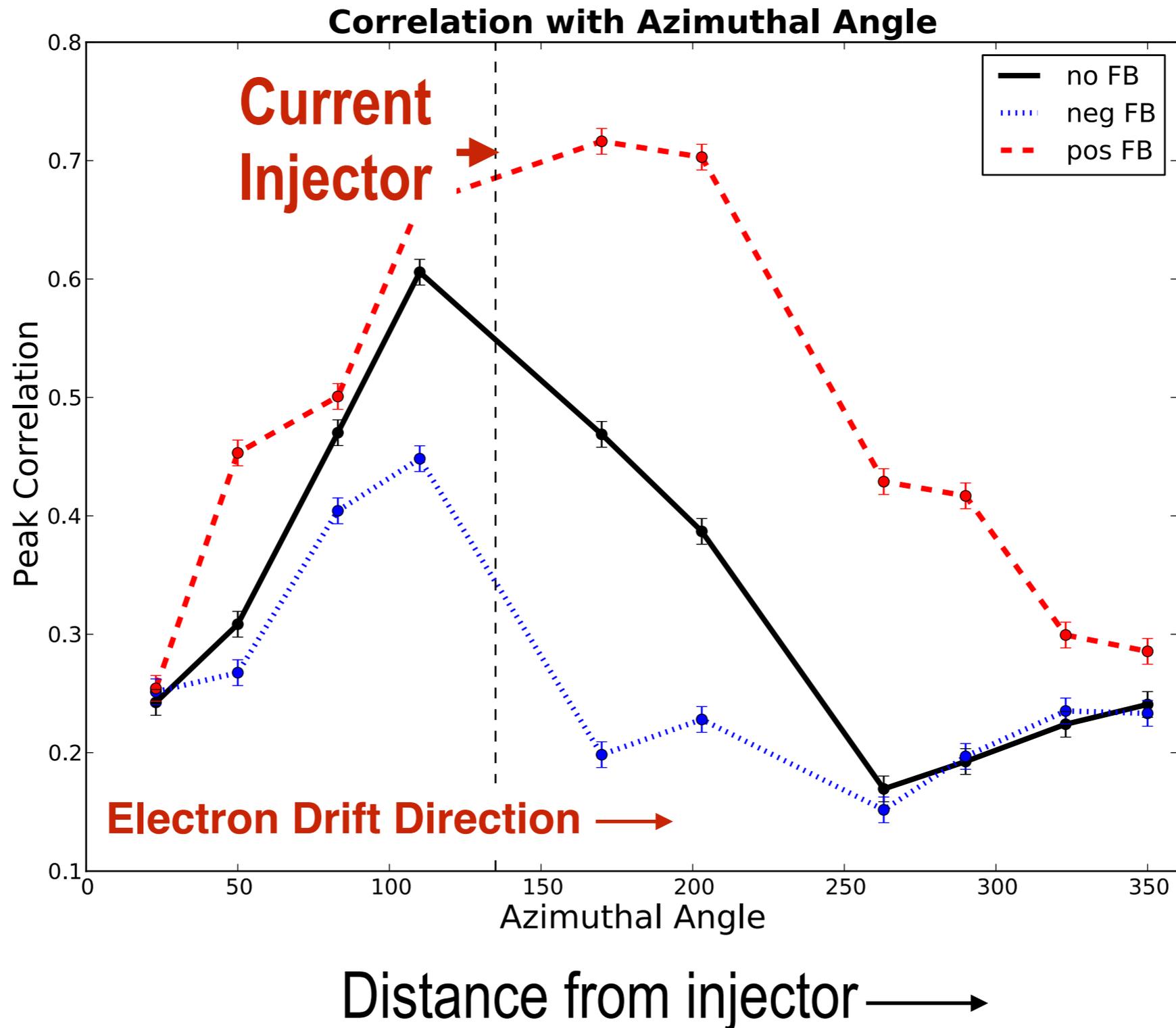


$$\int \frac{ds}{B} \nabla \cdot \mathbf{J}_{\perp} = \int \frac{ds}{B} \nabla \cdot \mathbf{J}_{prb} \propto I_{prb} \delta(\psi - \psi_{probe}) \delta(\varphi - \varphi_{prb})$$

# Current Injection results in Global Amplification or *Local* Suppression of $m = 1$ Entropy Modes



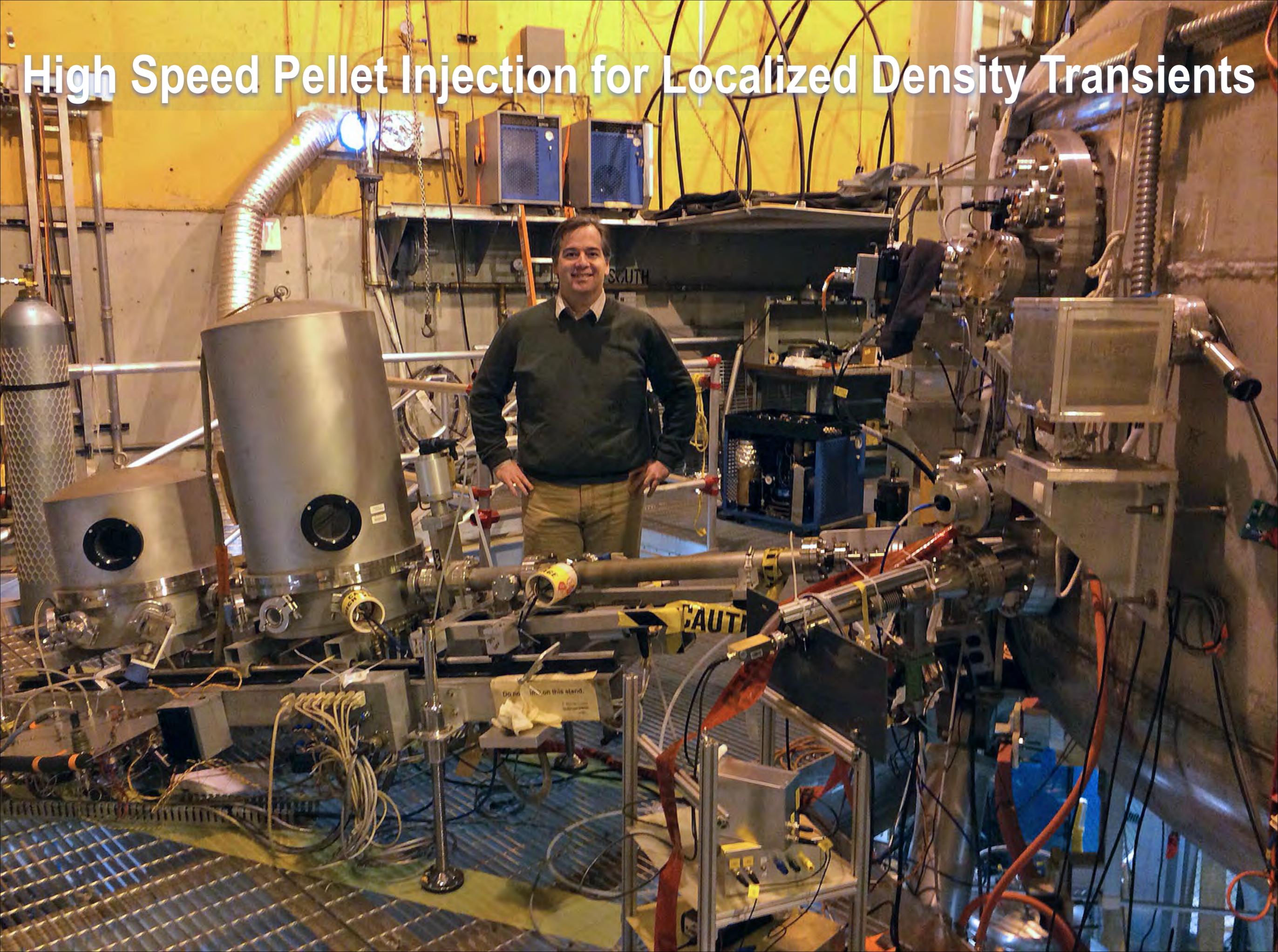
# Current Injection results in Global Amplification or Local Suppression of $m = 1$ Entropy Modes



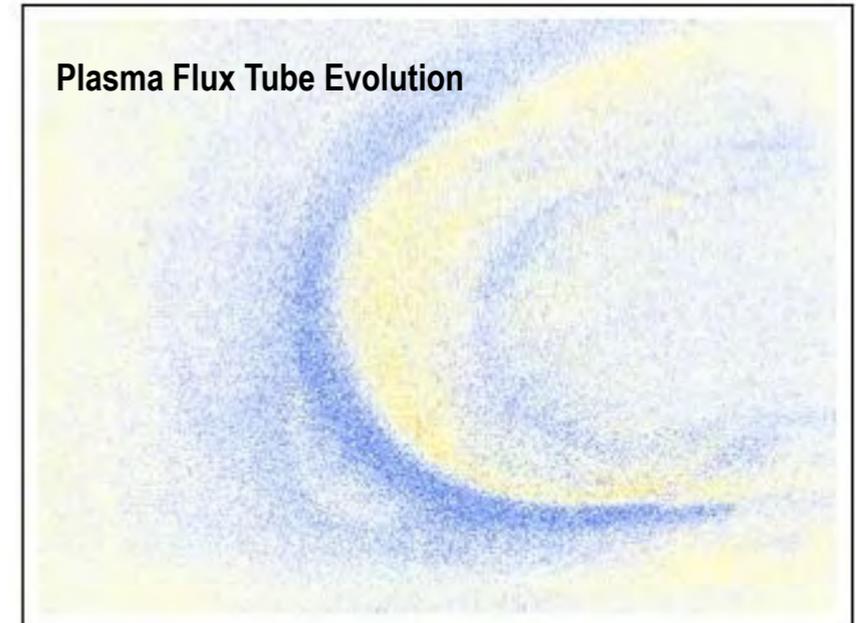
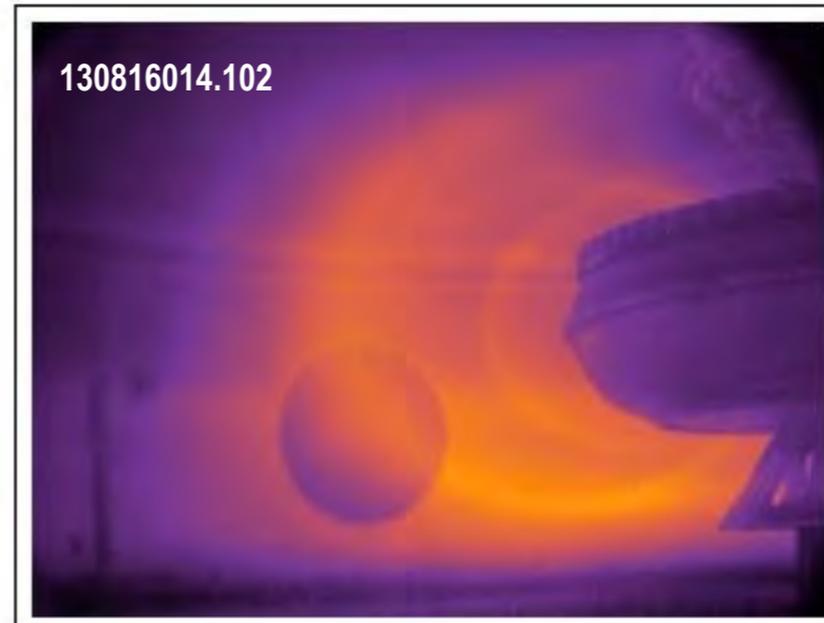
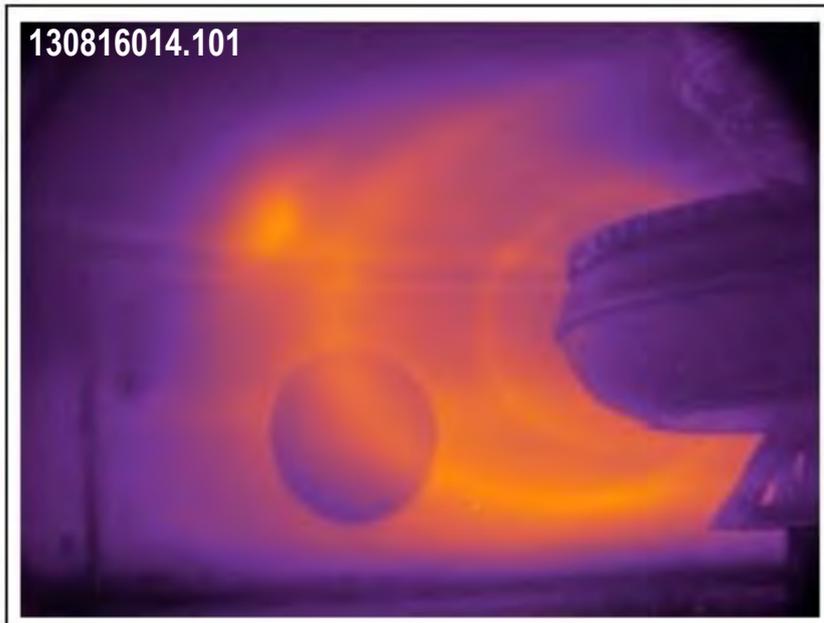
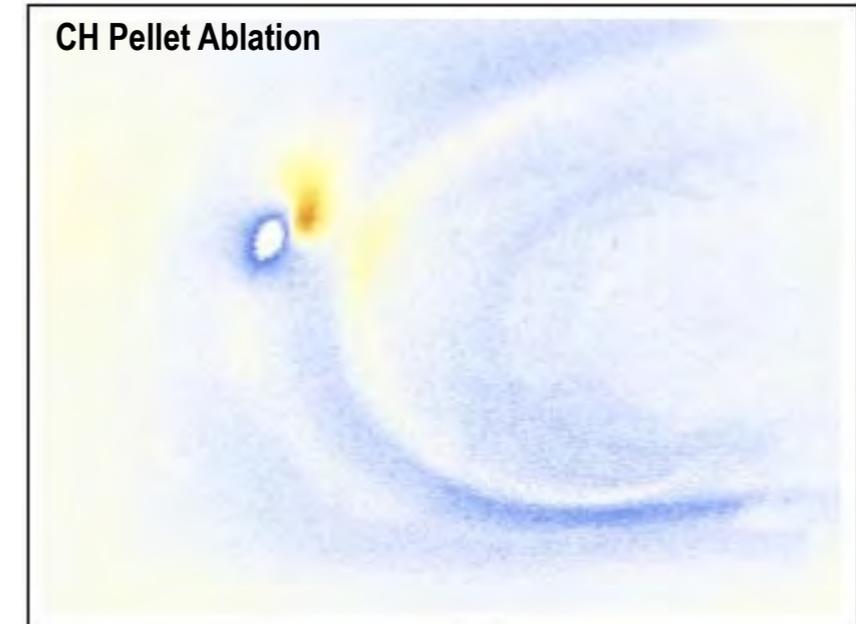
# Outline

- How does a laboratory magnetosphere work?
- Interchange disturbances and magnetic drift resonances
  - ▶ **Low frequency interchange turbulence: steady “canonical” profiles**
  - ▶ **Three interchange instabilities: Fast drift-kinetic, centrifugal interchange, semi-collisional entropy modes**
- **Examples:** exploring plasma dynamics by injection of heat, particles, current, and magnetic perturbations by decreasing ion inertial lengths

# High Speed Pellet Injection for Localized Density Transients



# Flux Tube Dynamics Following Pellet Release Experiments in Laboratory Magnetospheres



# Low-cost "Smart-Probes" for Multiple-Point *in situ* Measurements

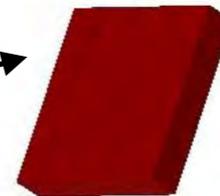


FRDM-KL05Z Development Board  
With Arduino & USB Interfaces  
3-axis accelerometer

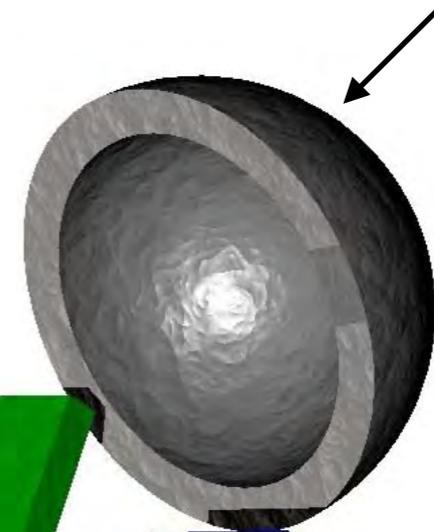
32 MB Flash Memory



KL05 MCU



Smart Probe Enclosure



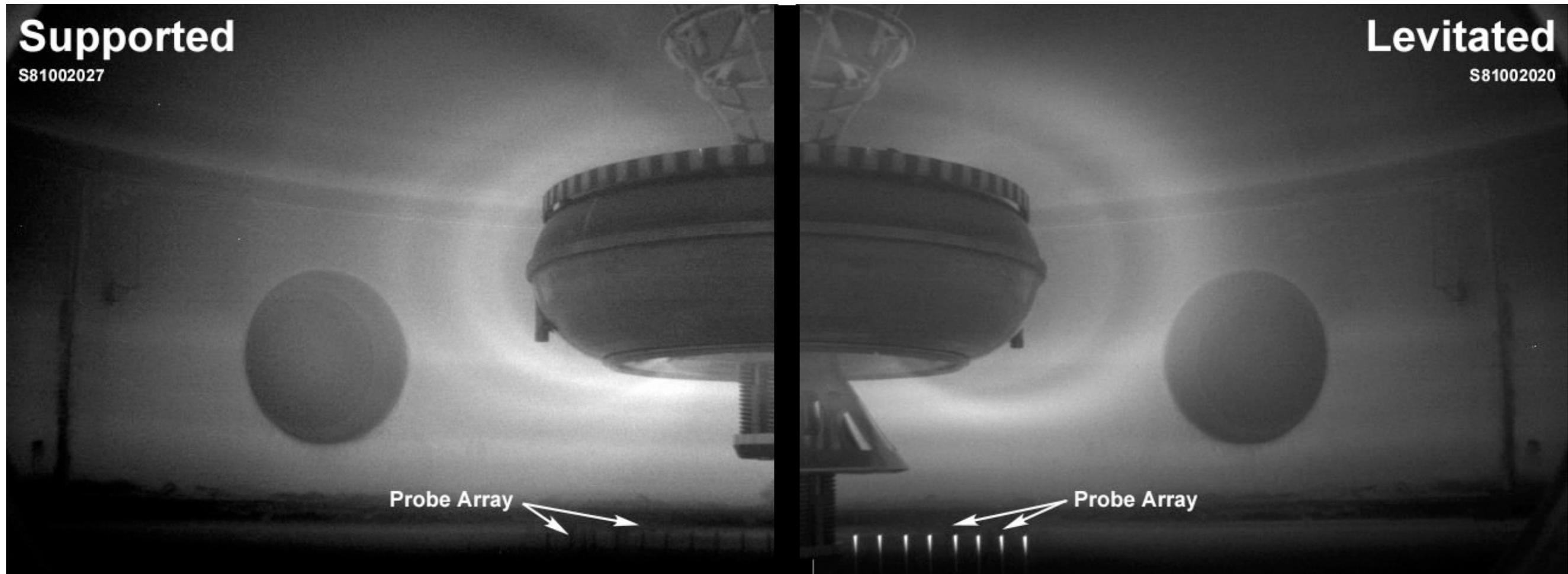
Battery Power



10 mm Dia

# World's Largest Lab Magnetosphere

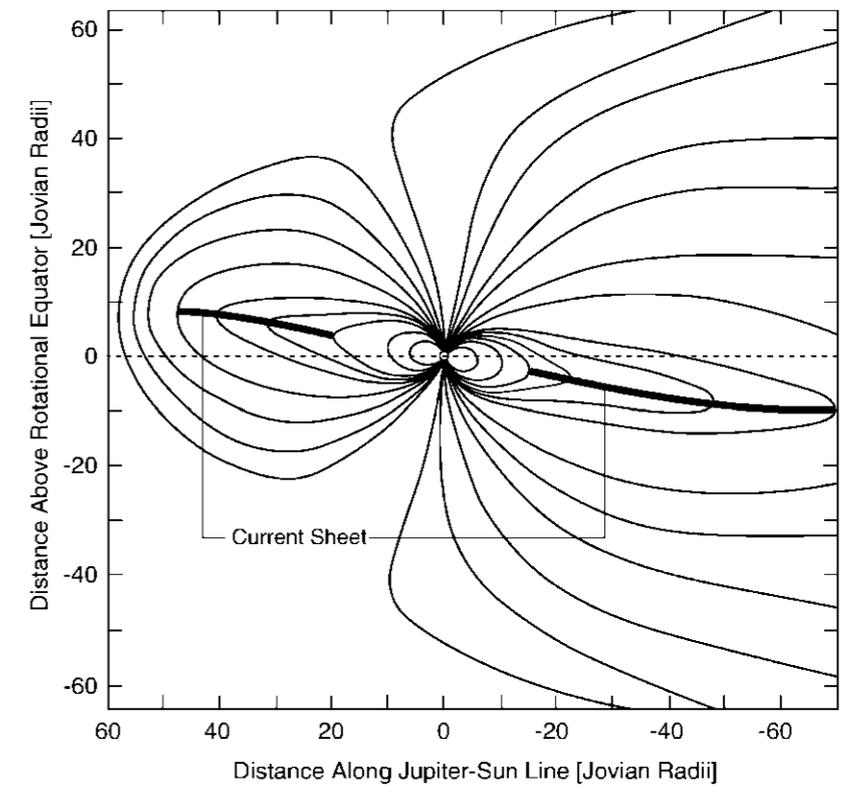
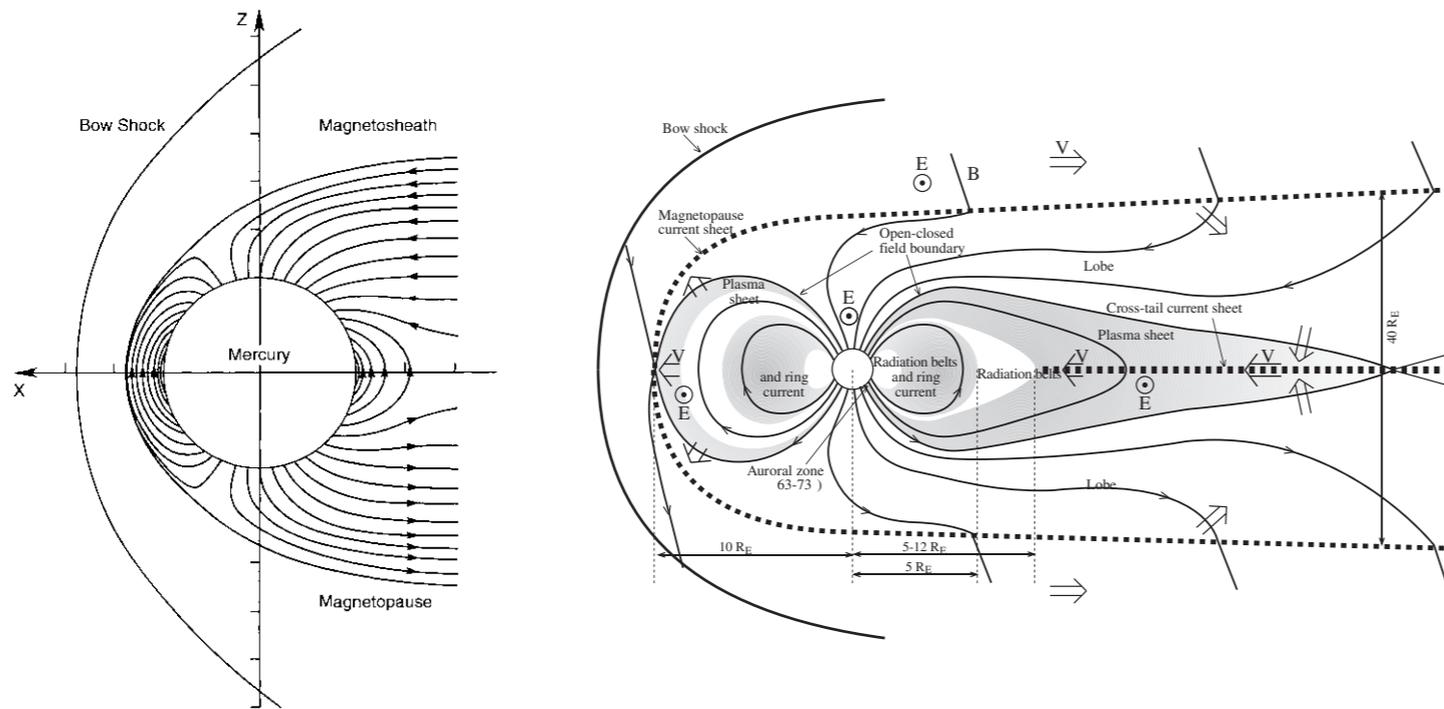
5 m



## ***Size matters:***

At larger size, trapped particle energy, intensity of “artificial radiation belt”, and plasma density significantly increase

# High Density and Large Size are required for Controlled Investigations of Alfvén Wave Dynamics



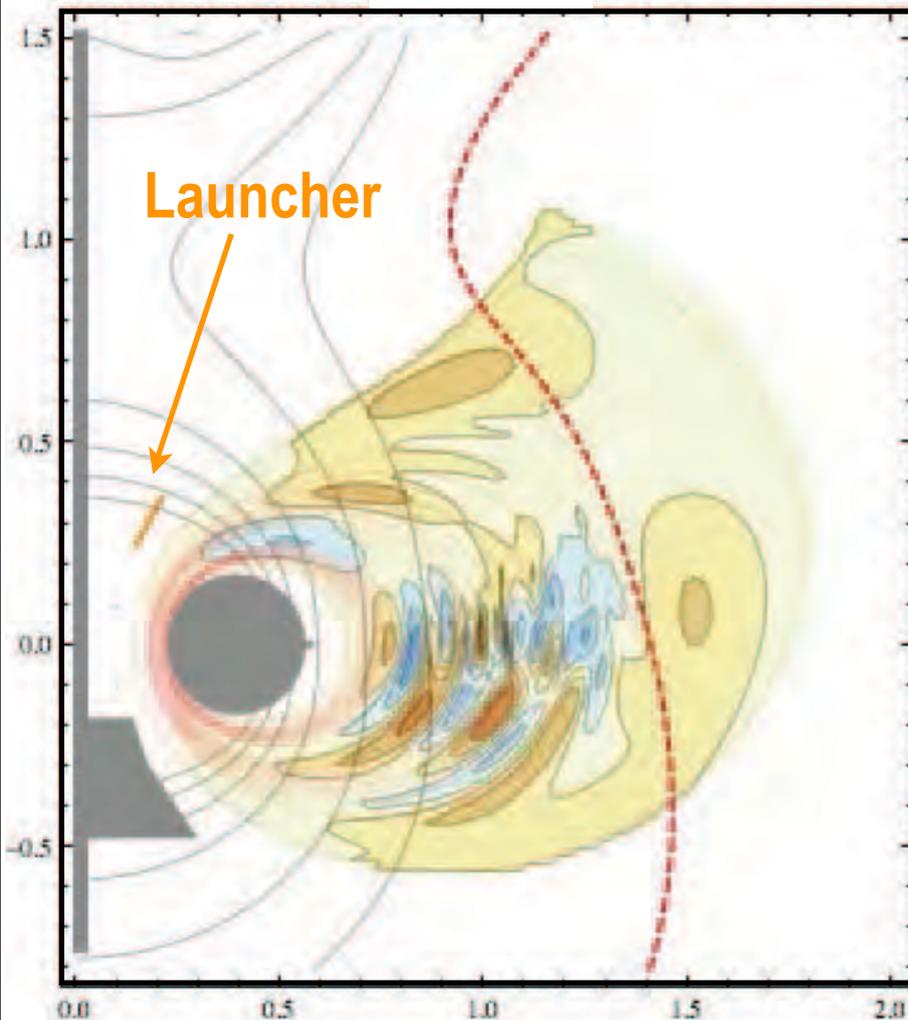
$$\frac{V_A}{L} \sim f_A \ll f_{ci} \rightarrow \frac{c/\omega_{pi}}{L} \ll 1$$

	Mercury	Earth	Jupiter
<b>Size</b>	2 R	10 R	100 R
<b>Density (<math>c / \omega</math>)</b>	0.1	0.003	0.00001
<b>Comments</b>	V	Alfvén Resonances	Propagating Alfvén

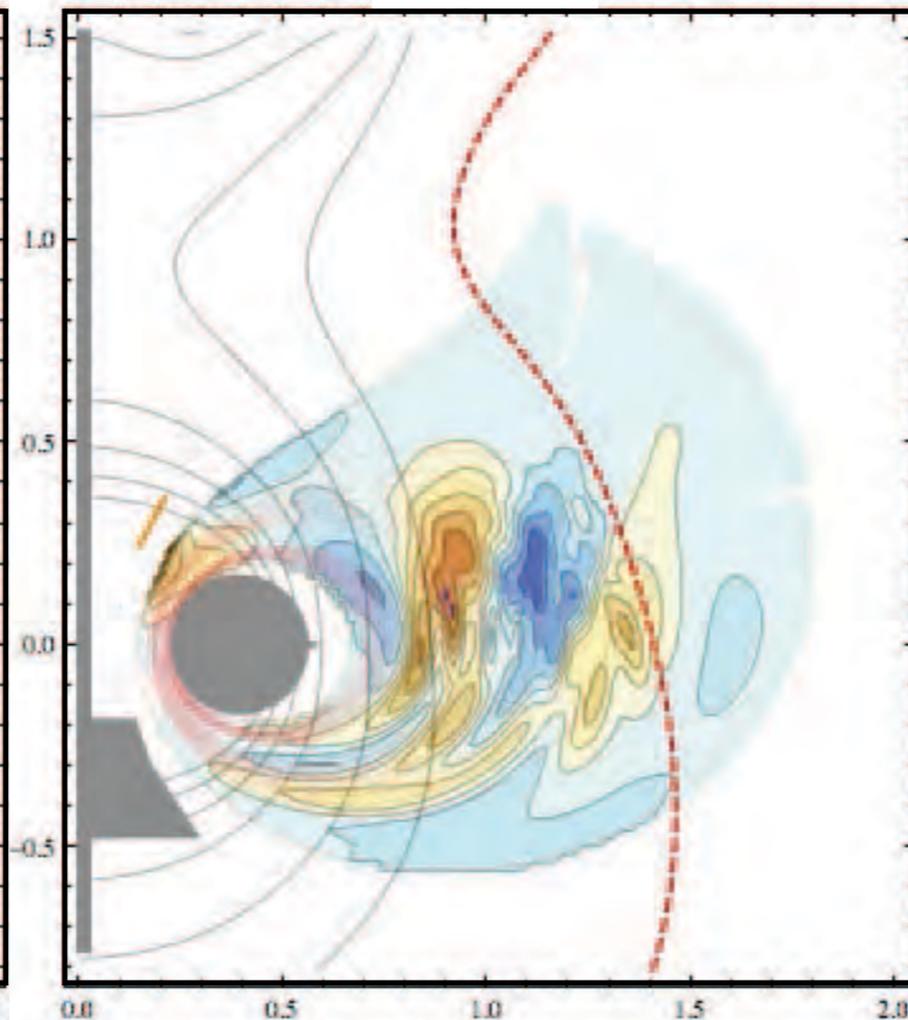
# Alfvén Wave Excitation in LDX: Opportunity for a Many Important Experiments

- Alfvén Wave Spectroscopy and Resonances
- Toroidal-Poloidal Polarization Coupling
- Alfvén Wave interactions with Radiation Belt Particles
- Ion Cyclotron Resonance and FLR

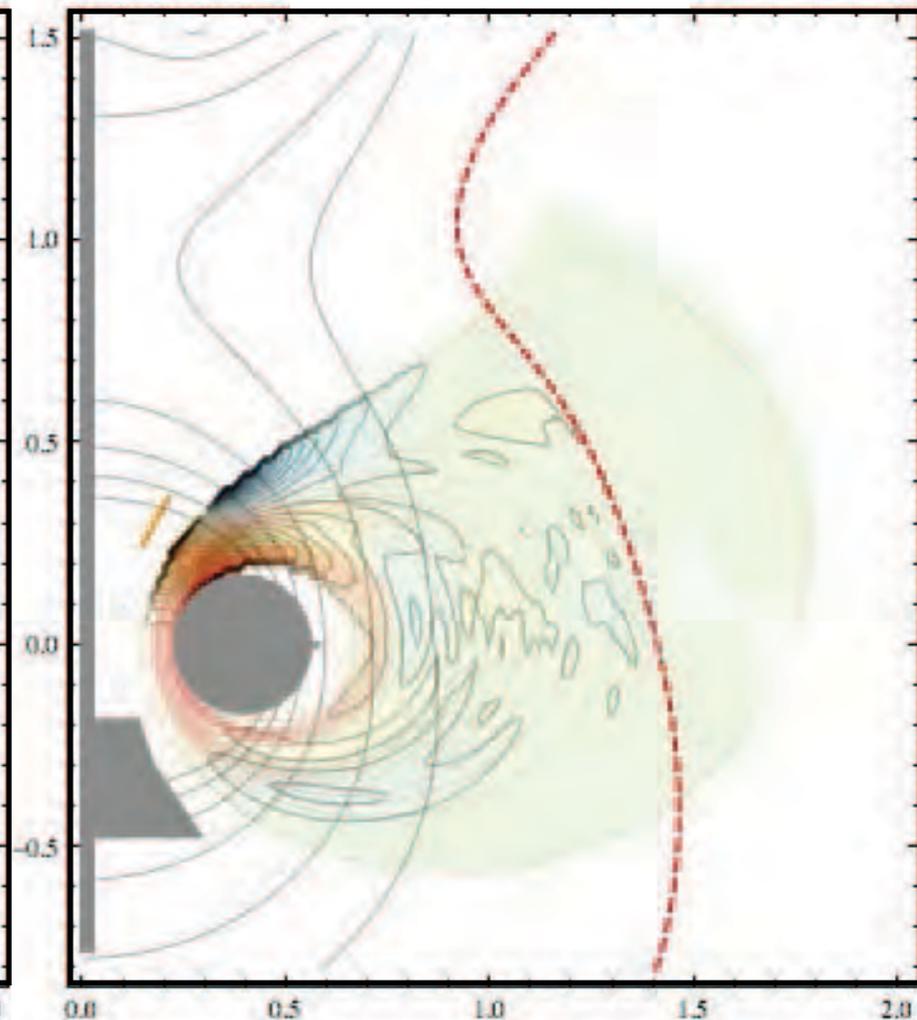
Toroidal



Poloidal



Compressional



Example: 200 kHz  $m = 2$  Polar Launcher

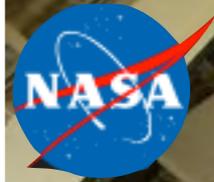
# NASA's early effort in Laboratory Testing and Validation can be Significantly Advanced with Modern Modeling and Diagnostics



NASA Glenn #5 (1966)



# A Large Space Chamber Could be Filled with a Laboratory Magnetosphere



## Space Power Facility (SPF)

Plum Brook Facility at Sandusky  
World's Largest Vacuum Vessel



# Laboratory Magnetospheres are Unique Opportunities for Controlled Plasma Science Experiments

- Laboratory magnetospheres are facilities for *conducting controlled tests* of space-weather models in relevant magnetic geometry and for *exploring* magnetospheric phenomena by *controlling the injection of heat, particles, and perturbations*
- Semi-collisional and trapped *“artificial radiation belt”* dynamics and transport have been studied.
- Larger laboratory magnetospheres significantly increase trapped particle energy, intensity of “artificial radiation belt”, and plasma density. Allowing new controlled tests of *complex Alfvén wave interactions* in the magnetosphere.
- *Very large plasmas* can be produced in the laboratory, continuously, with low power and great flexibility. *Verification and discovery* of critical plasma science.
- *Outlook*: We can build/operate the *largest laboratory plasma on Earth*