



# Inward Turbulent Diffusion of Plasma in a Levitated Dipole

#### LDX Experimental Team

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## Diffusion due to Random Velocity Fluctuations

$$X(t + \Delta t) = X(t) + \int_{t}^{t + \Delta t} dt' \tilde{V}(t')$$
  
where  $\langle \tilde{V} \rangle = 0$   
then  $\frac{\partial N}{\partial t} = \frac{\partial}{\partial X} D \frac{\partial N}{\partial X}$   
with  $D = \int_{0}^{t \to \infty} dt' \langle \tilde{V}(t') \tilde{V}(0) \rangle$   
 $= \tau_{cor} \tilde{V}_{RMS}^{2}$   
 $N(x, t)$ 

# Shake Sand on Plate



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# "Inward" Diffusion in Magnetized Plasma

(Flux tube Motion due to Random Low-frequency E×B Fluctuations)



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## "Inward" Diffusion in Magnetized Plasma

(Flux tube Motion due to Random Low-frequency E×B Fluctuations)





Turbulent "Inward Pinch"

$$\begin{aligned} \frac{\partial N}{\partial t} &= \frac{\partial}{\partial \psi} D \frac{\partial N}{\partial \psi} \\ D_{\psi,\psi} &= \lim_{t \to \infty} \oint_0^t dt \langle \dot{\psi}(t) \dot{\psi}(0) \rangle \\ &\equiv \langle \dot{\psi}^2 \rangle \tau_{cor} = R^2 \langle E_{\phi}^2 \rangle \tau_{cor} \end{aligned}$$

Levitated: Density (Particles/cc)



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# "Inward" Diffusion in Magnetized Plasma

(Flux tube Motion due to Random Low-frequency E×B Fluctuations)



Centrally peaked profiles result from turbulent interchange mixing: Electrostatic Self-Organization

# Naturally peaked profiles **sustained steady-state** by microwave heating.

Levitated: Density (Particles/cc)



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Inserted

ШC

## **TFTR** Density Profile *q*-Scaling



Glow from

Plasma

Support Withdrawn

FIG. 1. Density in units of  $10^{19}$  m<sup>-3</sup> as a function of minor radius in cm. The dots are data points from the supershot TFTR-76770, the dashed curve is proportional to 1/q, and the solid curve is calculated from Eq. (1).

V. Yankov, 1994

- The pinch effect [is the result] of a turbulent uniform distribution of particles over some phasespace surfaces specified by the geometry of the magnetic field and by invariants is introduced.
- Large-scale electrostatic modes lead to a turbulent uniform distribution nq = const with a maximum particle density at the center of the column.
- Leading to a natural explanation of the self-consistency of profiles.



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# Outline

- Plasma transport due to low-frequency fluctuations in a magnetospheric/dipole field: *The Turbulent Pinch*
- Levitated Dipole Experiment (LDX)
- Comparing discharges confined by a Supported and Levitated superconducting magnet
- Observation of the **turbulent inward particle pinch** and measurement of random **E**×**B** motion at edge.
- Turbulent transport of entropy density, G = PδV<sup>γ</sup>
- New research tools for LDX
- Tritium-suppressed fusion

#### Particle Dynamics Characterized by Adiabatic Invariants: Gyration ( $\mu$ ), Bounce (J), and Drift ( $\psi$ )

Northrup and Teller, "Stability of the Adiabatic Motion of Charged Particles in the Earth's Field," Phys Rev (1960) Warren, et al. "On Arnol'd diffusion in a perturbed magnetic dipole field," *GRL* (1992)



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# Magnetosphere



### Structure of Magnetosphere **Electric Field**



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Vol. 74, No. 9, MAY 1, 1969

**Electric Convection** 

#### **Convection Electric Fields and the Diffusion of Trapped Magnetospheric Radiation Collisionless Random**

THOMAS J. BIRMINGHAM

$$\frac{\partial \langle \bar{Q} \rangle (\alpha, M, J, t)}{\partial t} = \frac{\partial}{\partial \alpha} \left[ \overline{D_{\alpha \alpha}} \frac{\partial \langle \bar{Q} \rangle}{\partial \alpha} \right] \quad (5)$$

#### $\alpha$ = magnetic flux, $\Psi$

dipole field. We describe  $\mathbf{E}$  by the potential V

$$V = \frac{A(t)r}{\sin^2\vartheta}\sin\phi \qquad (2)$$

A being a positive, time-dependent amplitude. The form equation 2 is the fundamental (m = 1)asymmetric mode in Fälthammar's [1965] Fourier potential. Since  $r \sin^{-2} \vartheta$  and  $\phi$  are both constant on dipole field lines, **B** lines are equipotentials, and **E** · **B** is zero. In the  $\vartheta = \pi/2$ , equatorial plane

$$\overline{D_{aa}} \approx \frac{c^2 \mu^2}{4\alpha^2} \left(\pi\right)^{1/2} \tau_c \alpha \tag{18}$$

A reasonable direction to proceed, in view of the paucity of direct experimental evidence of electric fields and their time variations, is to assume that the autocorrelation  $(\delta A(t - \tau))$  $\delta A(t)$  has the form

$$\langle \delta A(t-\tau) \ \delta A(t) \rangle = \alpha \exp - \frac{\tau^2}{\tau_o^2}$$
 (16)

from dawn to dusk, and is random on the time expansion of a general longitudinally dependent scale on which the solar wind executes time variations of large spatial extent. (The correlation time  $\tau_{\bullet}$  is thus typically one hour.)

### **Random Interchange Motion**

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### Stationary Turbulent Profiles: Connection with Magnetic Geometry

- Plasma interchange dynamics is characterized by flux-tube averaged quantities:
  - Flux tube particle number,  $N = \int ds n/B \approx n \, \delta V$
  - Entropy density,  $G = P \,\delta V^{\gamma}$ , where  $\gamma \approx 5/3$

 $(n, P) \Leftrightarrow (N, G)$  are related by flux tube volume (geometry),  $\delta V = \int ds/B$ 

- Random fluctuations cause radial diffusion or plasma "flux-tubes". Interchange mixing flattens  $\partial$ [*N* and G]/ $\partial \psi \rightarrow 0$  at the same rate.
- Steady turbulent profiles imply **N** and **G** are homogeneous.
- Natural profiles are "stationary" since fluctuating E×B flows do not change (*N*, *G*).

#### **Natural Profiles are also Marginally Stable Profiles**

- N = constant, is the D. B. Melrose criterion (1967) for stability to centrifugal interchange mode in rotating magnetosphere.
- G = P δV<sup>Y</sup> = constant, is the T. Gold criterion (1959) for marginal stability of pressure-driven interchange mode in magnetosphere, and also Rosenbluth-Longmire (1957) and Bernstein, et al., (1958).
- Self-Organization is possible: e.g. steep central pressure gradients excites instability that drives inward turbulent particle pinch while relaxing pressure to P δV<sup>Y</sup> = constant

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## **Natural Profiles in Solenoidal Geometry**

#### Theta-pinch, large aspect ratio solenoid, ...

- Flux tube volume:
  - $\delta V = \int ds/B = \text{constant}$
  - $\delta V = \int ds/B = (q\mathcal{H})^{-0.8}$  (tokamak)
- Natural profiles:
  - $n \, \delta V = \text{constant}$
  - P δV<sup>γ</sup> = constant
  - Density and pressure profiles are flat
- Density, pressure, and temperature at edge and at core are equal unless interchange mixing is suppressed.



### **Natural Profiles in Dipole Geometry**



# **Electrostatic Self-Organization**

Heat injection creates *super-critical gradients* creating global turbulent fluctuations that *relax gradients* while *driving particles inward*.



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# LDX Experiment



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#### Levitated Dipole Experiment (LDX)



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# **Floating Coil Cross-Section**



- 1. Magnet Winding Pack
- 2. Heat Exchanger tubing
- 3. Winding pack centering clamp
- 4. He Pressure Vessel (Inconel 625)
- 5. Thermal Shield (Lead/ glass composite)
- 6. Shield supports (Pyrex)
- 7. He Vessel Vertical Supports/Bumpers
- 8. He Vessel Horizontal Bumpers
- 9. Vacuum Vessel (SST)
- 10. Multi-Layer Insulation
- 11. Laser measurement surfaces
- 13. Outer structural ring

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# RT-1 (University of Tokyo)





1/3-scale as LDX
High-beta (40%)
10 keV electrons
0.2 sec hot electron
confinement-time

**Previous Result using a Supported Dipole:** 

#### High-beta (β ~ 26%) plasma created by multiplefrequency ECRH with sufficient gas fueling

- Using 5 kW of long-pulse ECRH, plasma with trapped fast electrons ( $E_h > 50$  keV) were sustained for many seconds.
- Magnetic equilibrium reconstruction and x-ray imaging showed high stored energy > 300 J (τ<sub>E</sub> > 60 msec), high peak β ~26%, and anisotropic fast electron pressure, P<sub>⊥</sub>/P<sub>||</sub> ~ 5.
- Stability of the high-beta fast electrons was maintained with sufficient gas fueling (> 10<sup>-6</sup> Torr) and plasma density.
- D. Garnier, et al., PoP, (2006)







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#### Thin Supports were a Major Power Loss...



#### Lifting, Launching, Levitation, Experiments, Catching



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#### **Levitated Dipole Plasma Experiments**



#### Levitated Dipole Plasma Experiments



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#### New Result with Levitated Dipole:

# Centrally peaked density profiles and Increased plasma pressure occur during levitation

- Magnetic levitation eliminates parallel losses, and plasma profiles are determined by radial transport processes.
- Multi-cord interferometry reveals dramatic (up to 10-fold) central peaking of plasma density during levitation.
- Profile peaking occurs rapidly, allowing direct measurement of the inward particle pinch.
- Low-frequency fluctuations are observed with an intensity consistent with the observed inward pinch.
- The turbulent pinch is associated with increased plasma pressure consistent with constant entropy density, G = PδV<sup>γ</sup>, and high thermal electron temperature, T<sub>e</sub> > 300 eV.

### Density Profile with/ without Levitation

- Procedure:
  - Adjust levitation coil to produce equivalent magnetic geometry
  - Investigate multiplefrequency ECRH heating
- **Observe:** Evolution of density profile with 4 channel interferometer
- Compare: Density profile evolution with supported and levitated dipole



Alex Boxer, MIT PhD, (2008)

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## **Plasma Confined by a Supported Dipole**

- 5 kW ECRH power
- D<sub>2</sub> pressure ~ 10<sup>-6</sup> Torr
- Fast electron instability, ~ 0.5 s
- Ip ~ 1.3 kA or 150 J
- Cyclotron emission (V-band) shows fast-electrons
- Long, low-density "afterglow" with fast electrons
- ➡ 1×10<sup>13</sup> cm<sup>-2</sup> line density



### **Plasma Confined by a Levitated Dipole**



### Multi-Cord Interferometer Shows Strong Density Peaking During Levitation





## **Inversion of Chord Measurements**



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### **Inversion of Chord Measurements**



#### Levitation Always Causes More Peaked Profiles Relative to Supported Discharges

- Comparison of density profiles for levitated and supported discharges always show more peaked profiles during levitation.
- Natural density profiles are created regardless of plasma pressure (*i.e.* both low and high beta).
- Natural density profiles are established rapidly, within ~20 msec.
- Natural density profiles are sustained steady-state by microwave heating.

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## Natural Density Profiles Established Rapidly

- Levitation vs. Supported comparisons provide an opportunity to directly observe the effects of turbulent transport, as the parallel losses are switched off/on.
- Short 1/2 second heating pulses minimize influence of hot electrons on plasma dynamics.
- Turbulent fluctuations are established quickly as the ECRH is switched on.
   Fluctuations diminish after ECRH is switched off.



### **Naturally Peaked Profiles Established Rapidly**



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### Neutral Source Appears at Outer Edge (Levitation Shields Neutrals from Core)



# **Floating Potential Probe Array**

- Edge floating potential oscillations
- 4 deg spacing @ 1 m radius
- 24 probes
- Very long data records for excellent statistics!!



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#### Low-Frequency Fluctuations are Observed throughout Plasma and Probably Cause Naturally Peaked Profiles

- Low-frequency fluctuations ( $f \sim 1$  kHz and < 20 kHz) are observed with edge probes, multiple photodiode arrays, interferometry, and fast video cameras.
- The structure of these fluctuations are complex, turbulent, and *not understood*.
- Edge fluctuations can be intense ( $E \sim 200$  V/m) and are dominated by longwavelength modes that rotate with the plasma at 1-2 kHz
- High-speed digital records many seconds long enable analysis of turbulent spectra in a single shot. We find the edge fluctuations are characteristic of viscously-damped 2D interchange turbulence.
- See Brian Grierson, *et al.* "Global and local characterization of turbulent and chaotic structures in a dipole-confined plasma," *Phys Plasmas* (2009).

# Plasma ExB Motion

$$\mathbf{V} = -\hat{\varphi}R\frac{\partial\Phi}{\partial\psi} + \frac{\hat{\psi}}{RB}\frac{\partial\Phi}{\partial\varphi}$$

•

$$\dot{\psi} = \nabla \psi \cdot \mathbf{V} = \frac{\partial \Phi}{\partial \varphi} = -RE_{\varphi}$$
  
Measured  
at edge

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### Random Interchange Particle Diffusion



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#### **Naturally Peaked Profiles Established Rapidly**



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#### Turbulent Particle Pinch is associated with Turbulent Entropy Pinch: Pressure Peaking

 Flux-tube density and entropy density have identical dynamics for a plasma with an adiabatic closure, G = PδV<sup>γ</sup>

$$\frac{\partial N}{\partial t} - \frac{\partial}{\partial \varphi} \left( N \frac{\partial \Phi}{\partial \psi} \right) + \frac{\partial}{\partial \psi} \left( N \frac{\partial \Phi}{\partial \varphi} \right) = S$$
$$\frac{\partial G}{\partial t} - \frac{\partial}{\partial \varphi} \left( G \frac{\partial \Phi}{\partial \psi} \right) + \frac{\partial}{\partial \psi} \left( G \frac{\partial \Phi}{\partial \varphi} \right) = H$$

- (N, G) ~ constant implies peaked density and pressure profiles (if γ > 1)
- Edge T<sub>e</sub> ~ 15 eV, implies central T<sub>e</sub> ~ 500 eV with measured diamagnetism and measured density profile
- Thermal stored energy of 60 J (this example levitated discharge, 2 µTorr D<sub>2</sub>)



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$$\frac{\partial G}{\partial t} - \frac{\partial}{\partial \varphi} \left( G \frac{\partial \Phi}{\partial \psi} \right) + \frac{\partial}{\partial \psi} \left( G \frac{\partial \Phi}{\partial \varphi} \right) = H$$

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- Thermal stored energy of 60 J (this example levitated discharge, 2 µTorr D<sub>2</sub>)

Adiabatic mixing implies core parameters determined by edge & compressibility:



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### **Next Steps in LDX Dipole Confinement Physics**

- Do natural pressure profiles, P ~ 1/δV<sup>Y</sup>, develop? Soft x-ray diagnostics (installed) and Thomson scattering (SSPX) for warm plasma pressure profile measurements.
- What are the spatial structures of the convective flows? Install additional interferometer channels, reflectometer, and complete high-speed optical tomography analysis (in progress).
- Higher density plasma with additional heating options:
  - ✓ 10 kW CW 28 GHz gyrotron (1st experiments successful)
  - ▶ 1 MW CW ICRF heating (*TSW2500 from GA, starting...*)
- What is the effect of magnetic field errors on confinement? Install non-axisymmetric trim/error coils. Induce ~15 kA plasma current to create very weak rotational transform.

• Back to The Future (July 3, 1985) Fuel: banana, beer

• Spider-Man 2 (June 30, 2004) Fuel: tritium

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- Opened July 19, 2009. (Written and directed by Duncan Jones, son of David Bowie.)
- It is the near future. Astronaut Sam Bell is living on the far side of the moon, completing a three-year contract with Lunar Industries to mine Earth's primary source of energy, Helium-3. It is a lonely job, made harder by a broken satellite that allows no live communications home. Taped messages are all Sam can send and receive.





#### **Deuterium-Fueled Power Plants with Tritium Suppression**

John Sheffield and Mohamed Sawan, Fus. Sci. Tech. (2008)





Fig. 1. dpa and He production rates in ferritic steel for D-T and D-D systems for the first wall of a ferritic steel/ $H_2O$  shield.

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### Levitated Dipole Confinement Concept: Combining the Physics of Space & Laboratory Plasmas

- Steady state
- Non-interlocking coils
- Good field utilization
- Possibility for  $\tau_E > \tau_p$
- Advanced fuel cycle
- Internal ring

#### **Levitated Dipole Reactor**



# **Dipole Fusion Concept**

ITER<br/>ts Generation ReactorLevitated Dipole<br/>Sud Generation ReactorImage: Stress of the stres

Kesner, et. al. Nucl. Fus. 2004

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# **Summary**

• Levitation eliminates parallel particle losses and allows a dramatic peaking of central density.

LDX has demonstrated the formation of natural density profiles in a laboratory dipole plasma and the applicability of space physics to fusion science.

- Random fluctuations of density, light emission, potential, and electric field provide evidence of random E×B motion that causes interchange mixing and an turbulent inward pinch.
- Intensity of  $E_{\phi}$  fluctuations measured at edge can account for inward diffusion.
- Increased stored energy consistent with adiabatic entropy density profile: a necessary physics requirement for dipole fusion.



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