

# Avoidance of NTMs in High Performance DIII-D Plasmas

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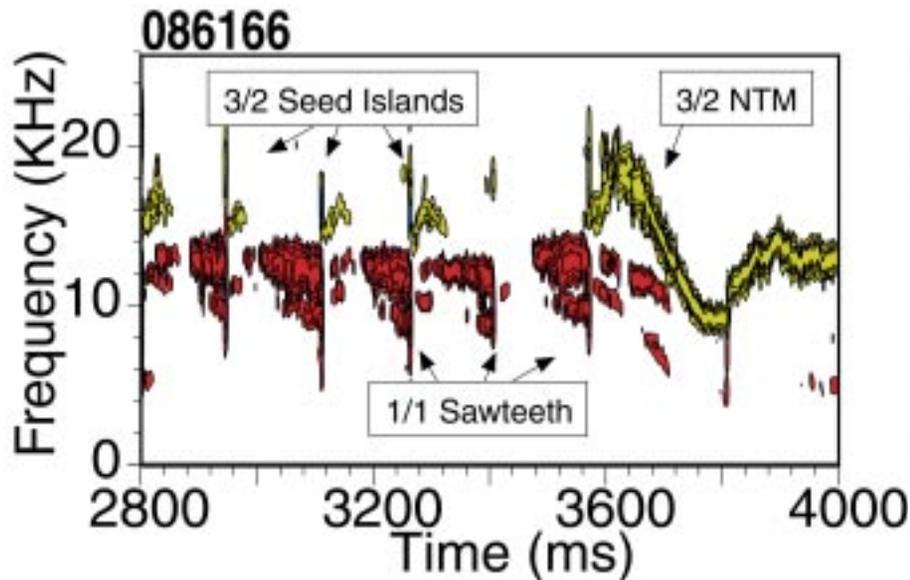
# New Understanding of Onset Mechanism Can Lead to Avoidance of NTMs

NTMs are linearly stable but nonlinearly unstable, ie. Metastable

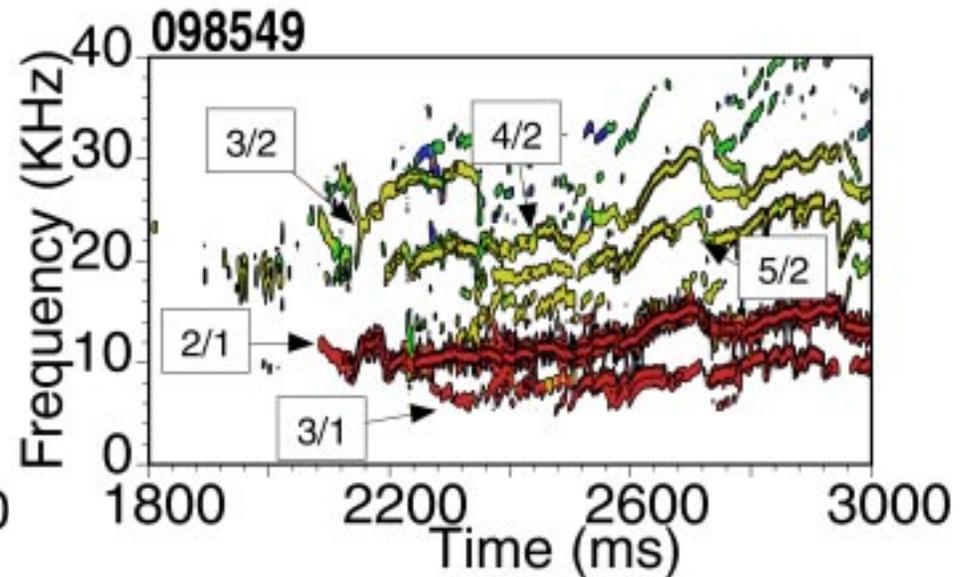
- Need “seed” or triggering event

Onset mechanism explains two common puzzles:

$n^{\text{th}}$  Sawtooth Seeds an NTM?

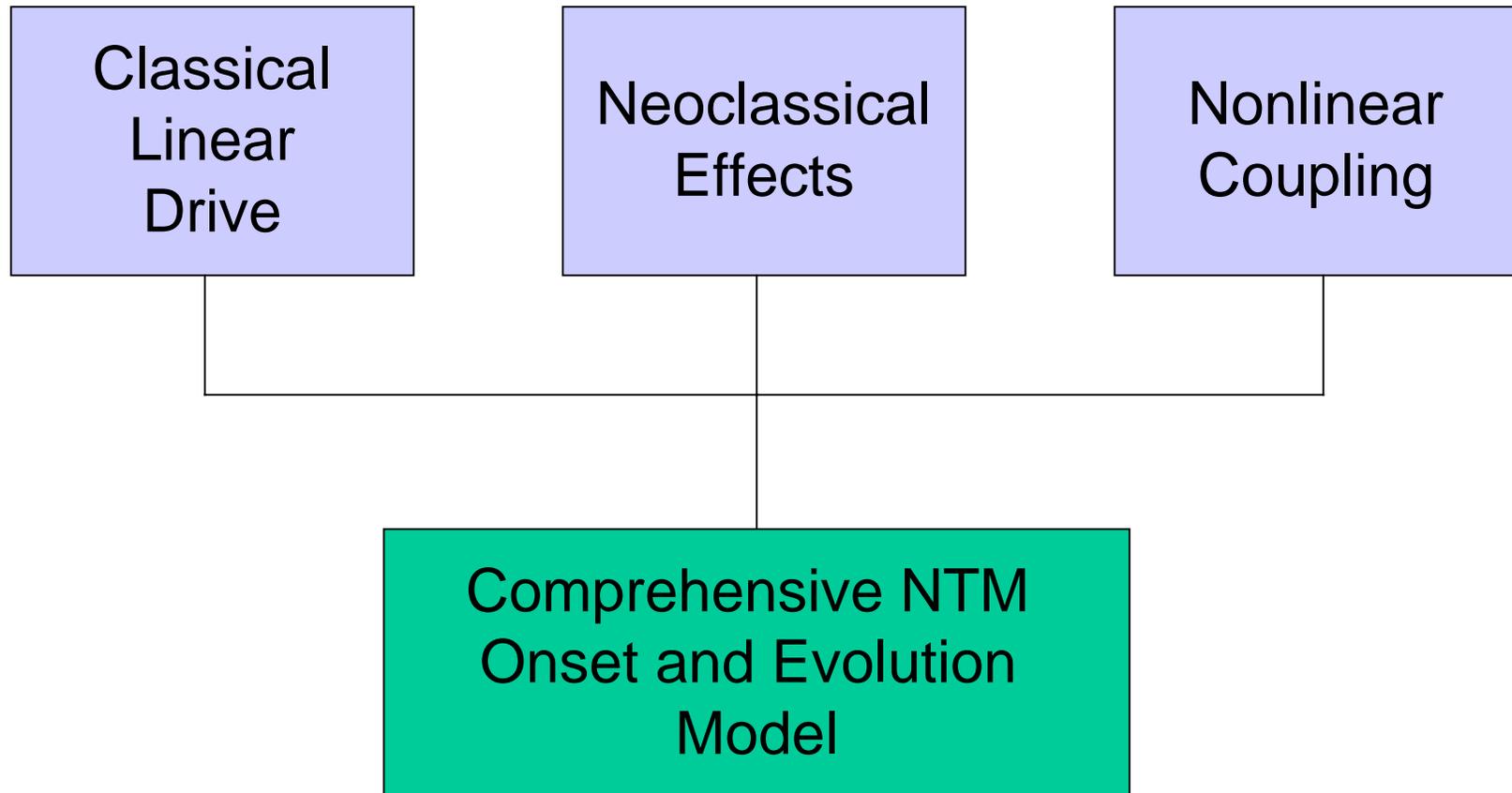


Seedless NTMs?



# A Comprehensive Model of NTM Onset Emerges From a Combination of Theories

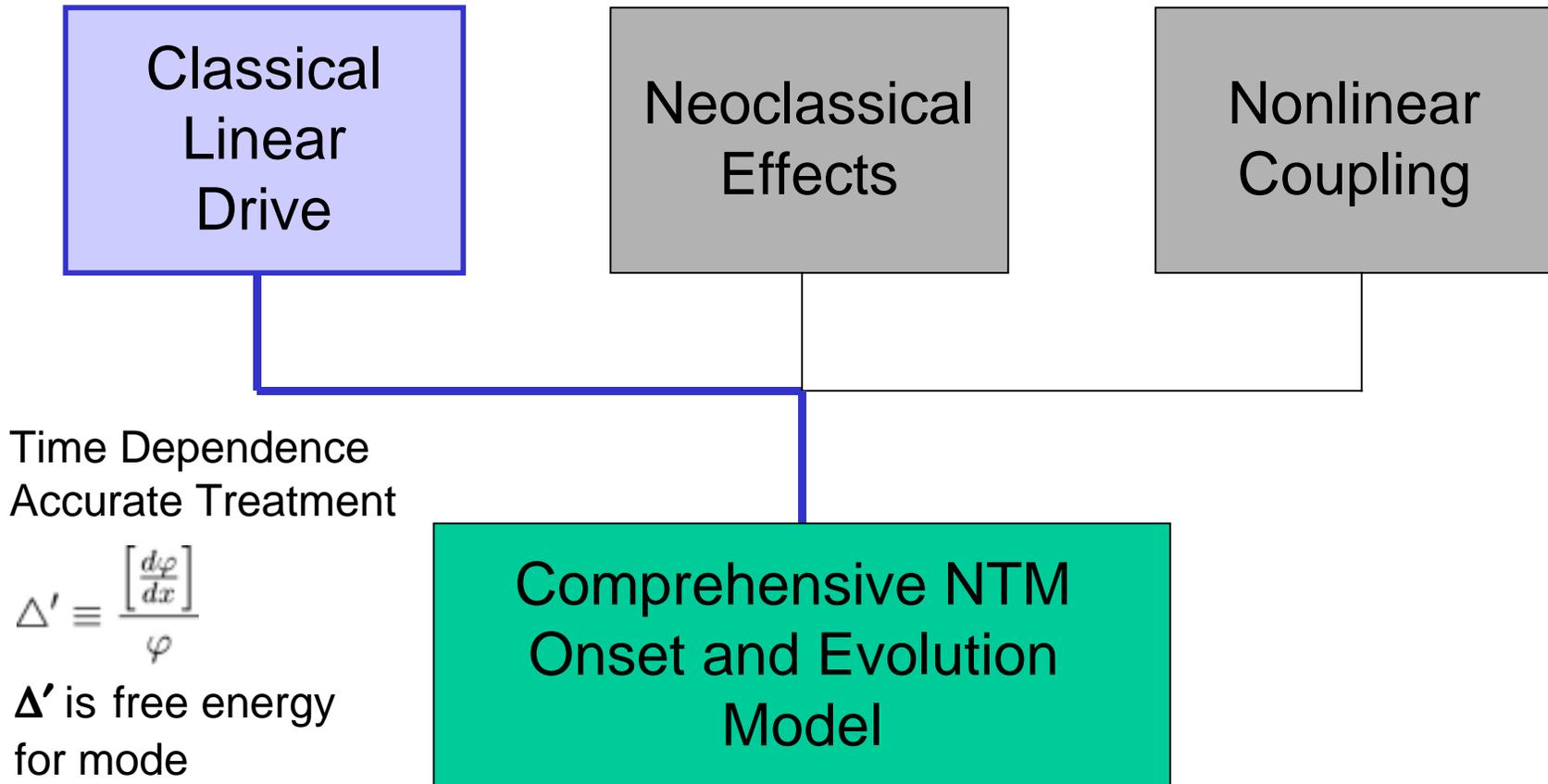
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All three components are necessary to explain the onset and evolution

# A Comprehensive Model of NTM Onset Emerges From a Combination of Theories

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All three components are necessary to explain the onset and evolution

# Outline

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**Thesis:**  $\Delta'(t)$  depends strongly on the equilibrium parameters near ideal limit \_ key physics for NTM onset in some cases \_ **this is a key to avoidance.**

**Island Evolution Equation** : essential physics of nonlinear evolution

**Analytic model** : the basic physics of the time dependence of  $\Delta'$

**Sawtooth Seeding of 3/2 NTM** : DIII-D discharge which encompasses **nonlinear**, **neoclassical** and **classical** effects is comprehensively analyzed showing the critical time dependence in  $\Delta'$ .

**Pole Experiment** : theoretical predictions of the effects of time dependence in  $\Delta'$  are compared to results from a DIII-D experiment to isolate these effects.

**Open Questions on Avoidance:** implications on control of NTMs

# Island Evolution Equation Captures Essential Physics Necessary to Describe Onset and Early Evolution

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Coupling not included

$\Delta'$  often assumed  
constant negative

**With accurate time  
dependence and  
weak coupling,  
onset and early  
evolution can be  
predicted**

$$\frac{dw}{dt} = \frac{\eta^*}{k_0} \left[ \Delta^* + \frac{k_1}{w} (D_{nc} + \frac{D_R}{\alpha_s - H}) + \frac{D_{pol}}{w^3} \right]$$

where

$$\Delta^* = \Delta' \left( \frac{w}{2} \right)^{-2\alpha_l} (-4D_I)^{1/2}$$

$$\frac{\eta^*}{k_0} \sim \frac{r_s^2}{\tau_r}$$

Classical drive

$$k_1 = \frac{w^2}{w^2 + w_d^2}$$

Neoclassical drive

$$D_{nc} = k_2 \sqrt{\epsilon} \beta_\theta \frac{L_q}{L_p}$$

Polarization drive

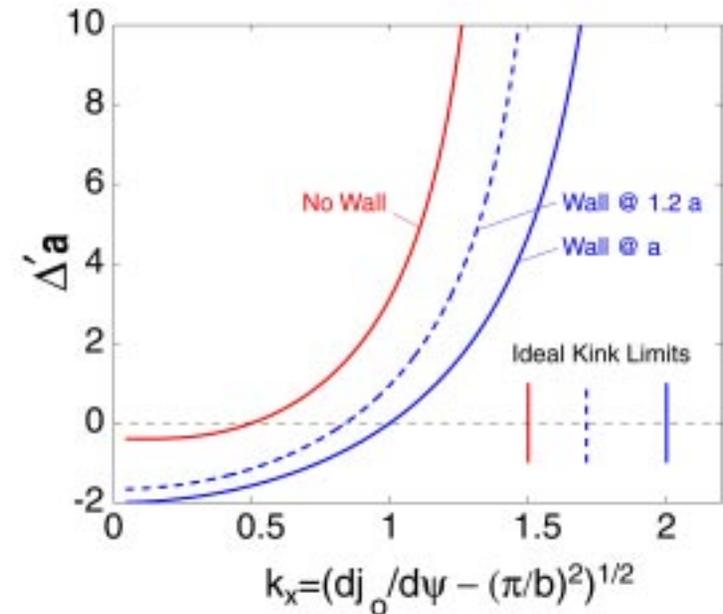
$$D_{pol} = -D_{nc} \frac{\rho_{i\theta}}{a^2} \frac{L_q}{L_p} g$$

# Analytic Models of Linear Tearing Stability Show Strong Variation of $\Delta'$ Near Ideal Instability

Small change in equilibrium and/or conducting wall dramatically affects  $\Delta'$  near ideal limit due to

**POLE DISCONTINUITY** at ideal limit.

The Pole Form is Ubiquitous  
Among Derivations, Numeric and Analytic



With a conducting wall at a:

$j'_o$  constant,  
slab geometry:

$$\Delta'a = -2k_x a \cot(k_x a)$$

$$k_x = \sqrt{j'_o - k_y^2}$$

With a vacuum region from a to b:

$$\Delta'a = 2k_x a \frac{E \sin(k_x a) + \cos(k_x a)}{E \cos(k_x a) - \sin(k_x a)}$$

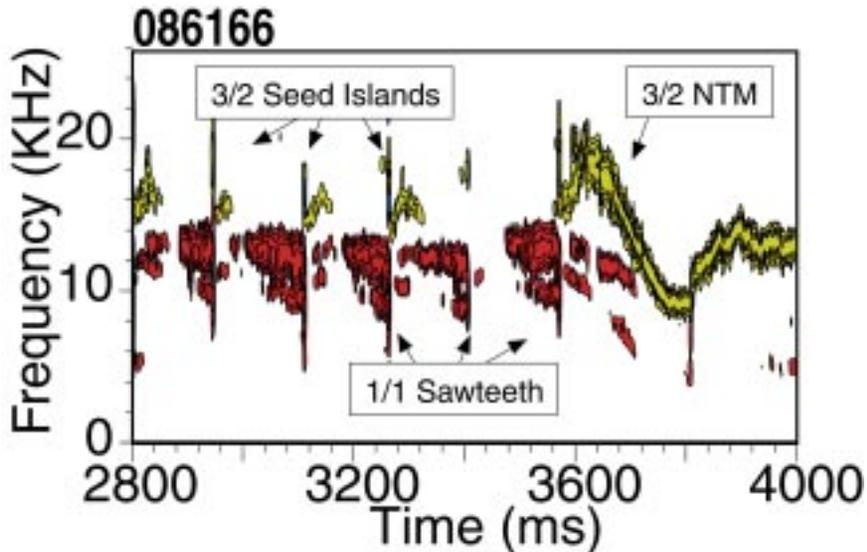
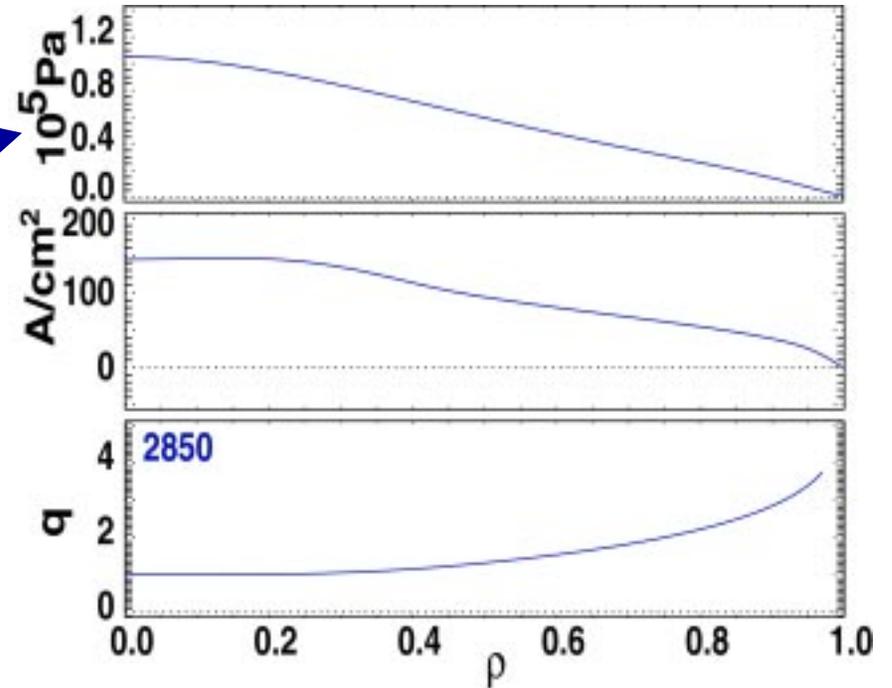
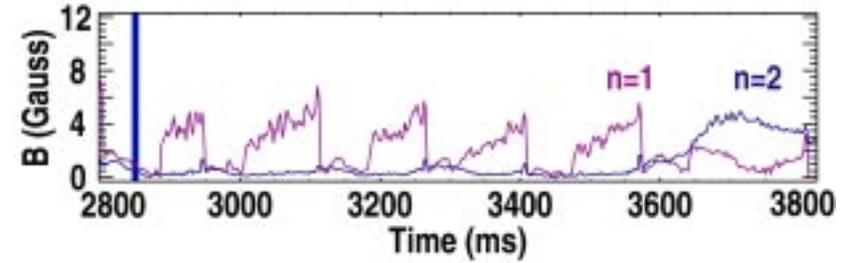
$$E = \frac{e^{k_x a} - e^{k_x(2b-a)}}{e^{k_x a} + e^{k_x(2b-a)}}$$

$$k_x = \sqrt{j'_o - k_y^2}$$

# Slight Increase in Core Pressure Destabilizes a Seed Island from a Sawtooth and Causes the Onset of a 3/2 NTM

Equilibrium reconstructions between sawteeth

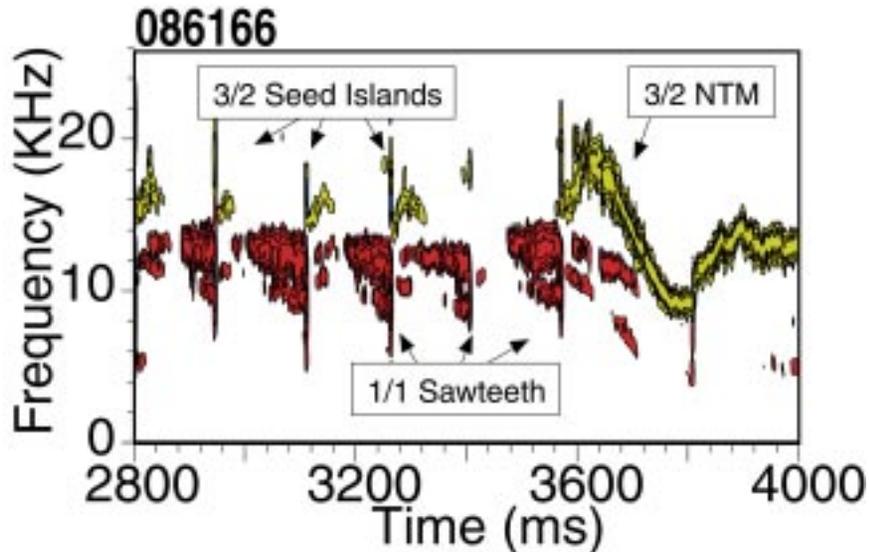
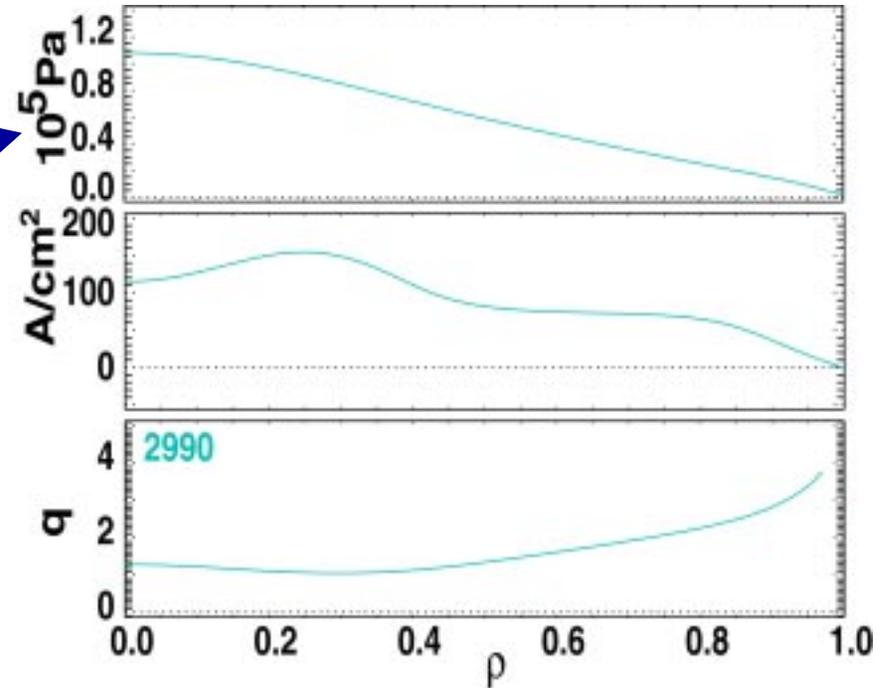
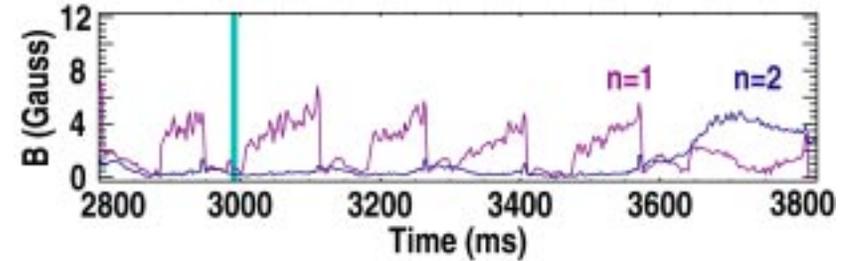
Most pronounced profile variation is core pressure just before onset.



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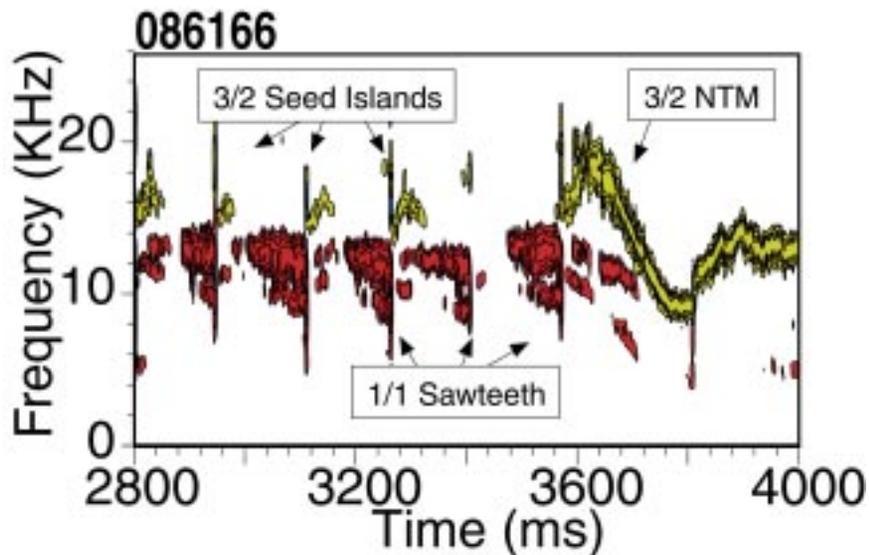
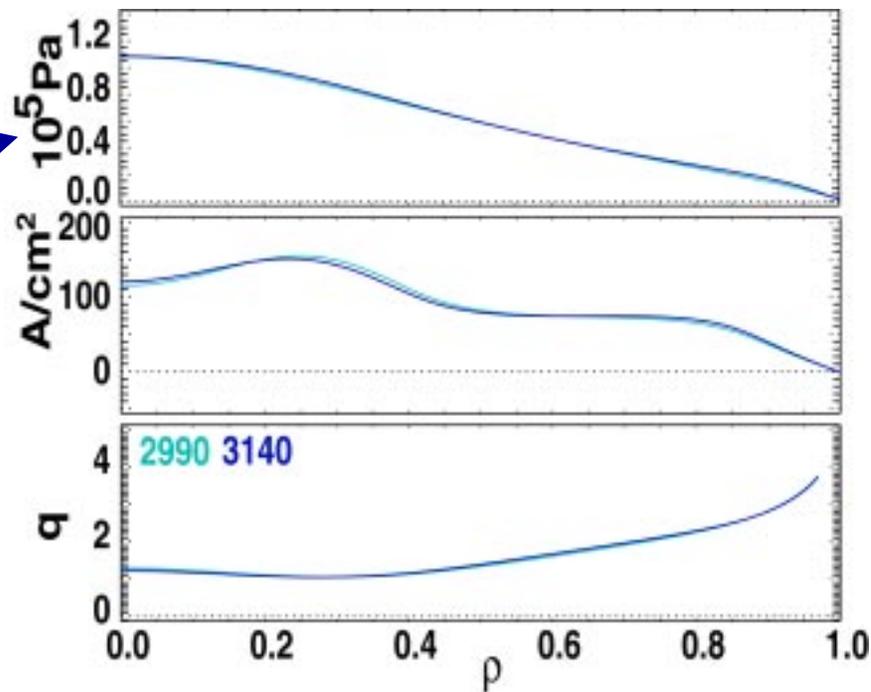
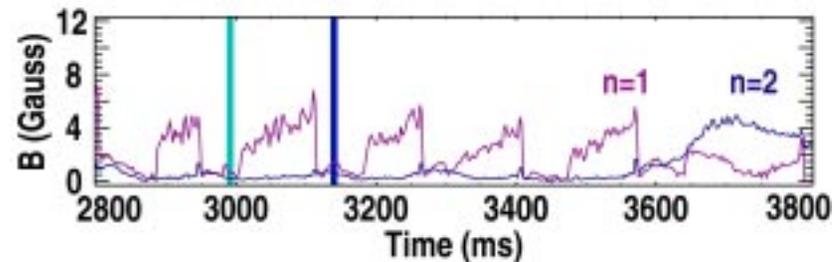
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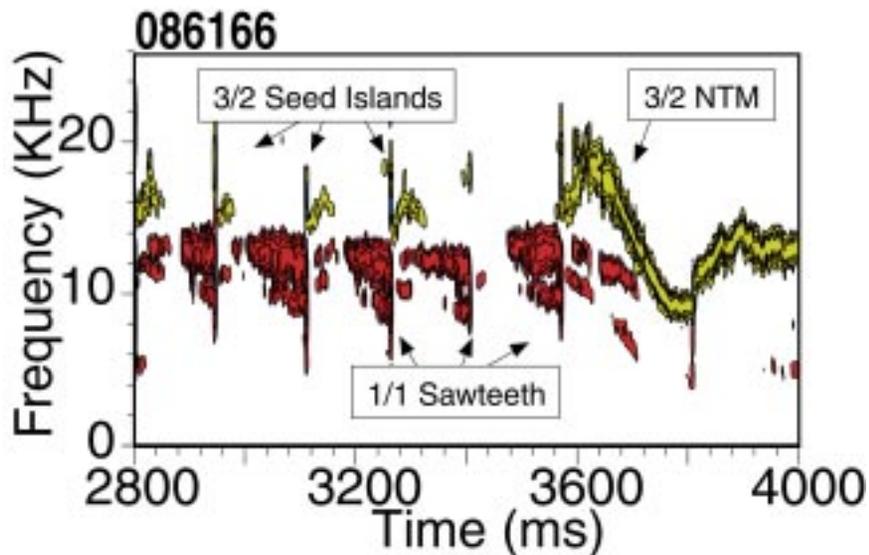
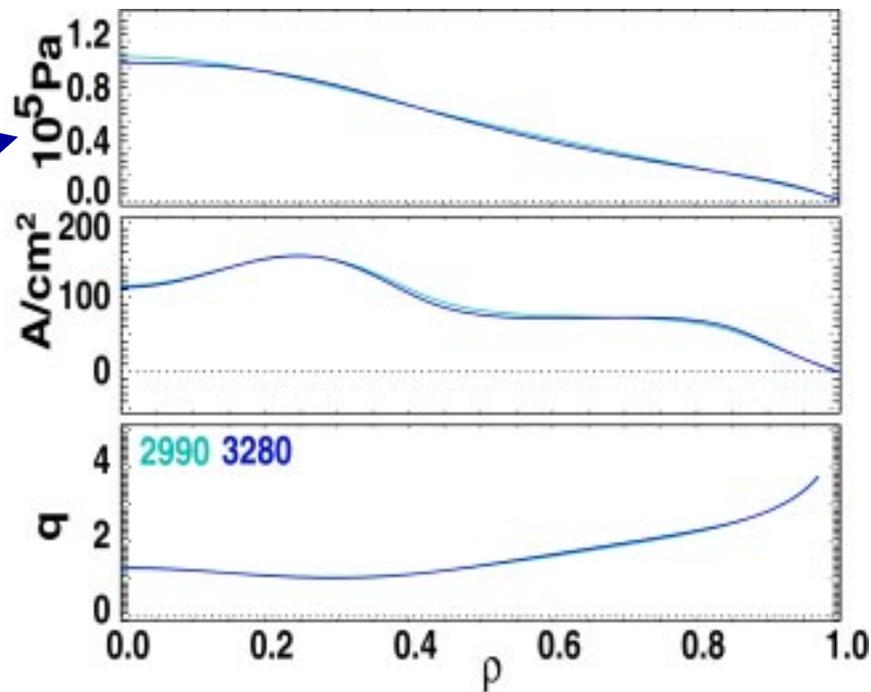
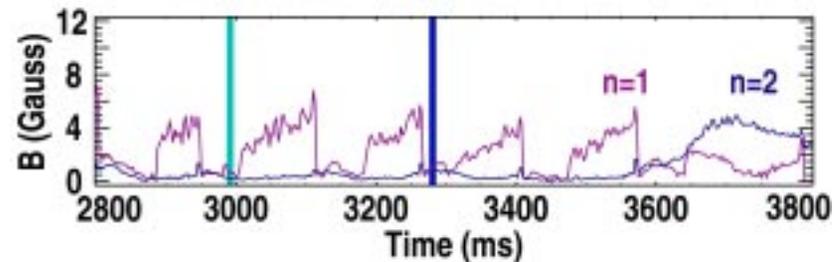
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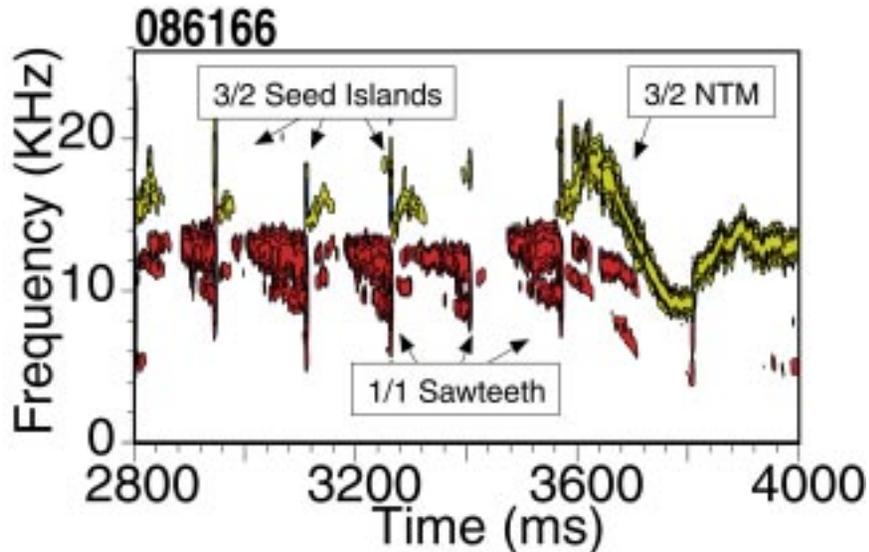
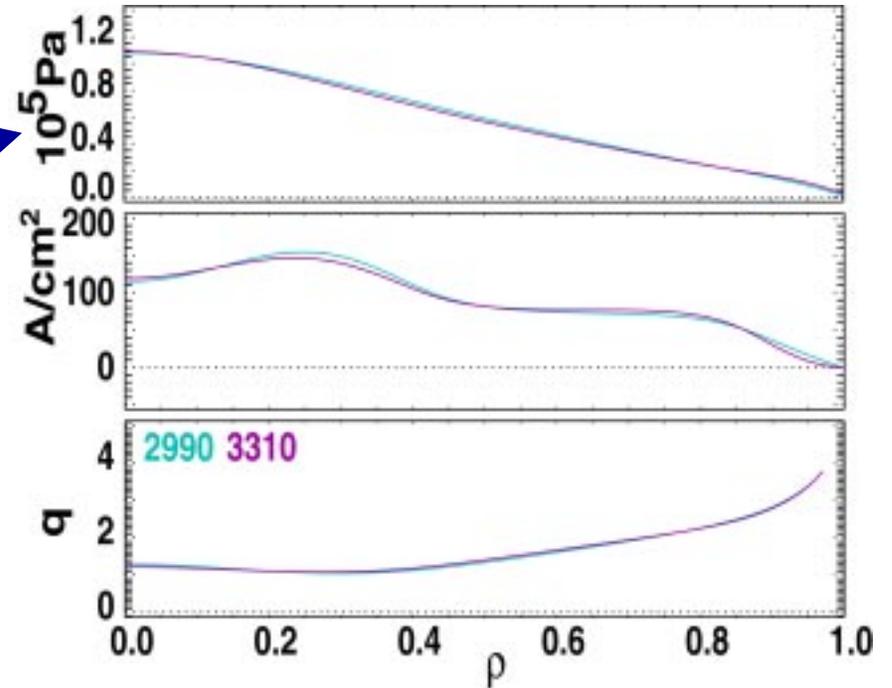
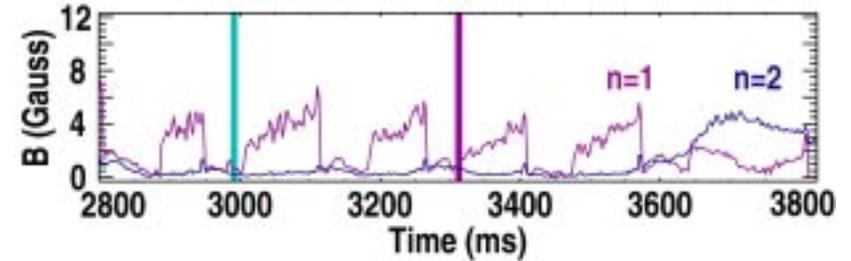
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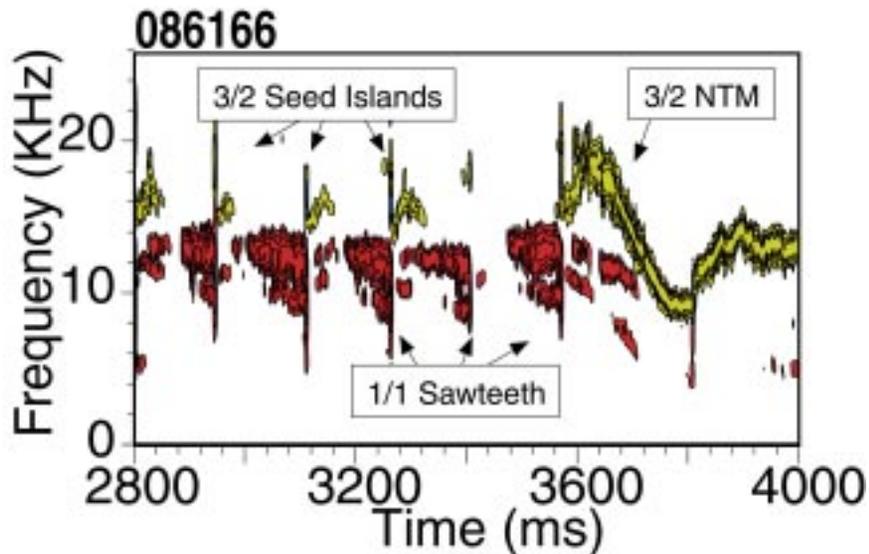
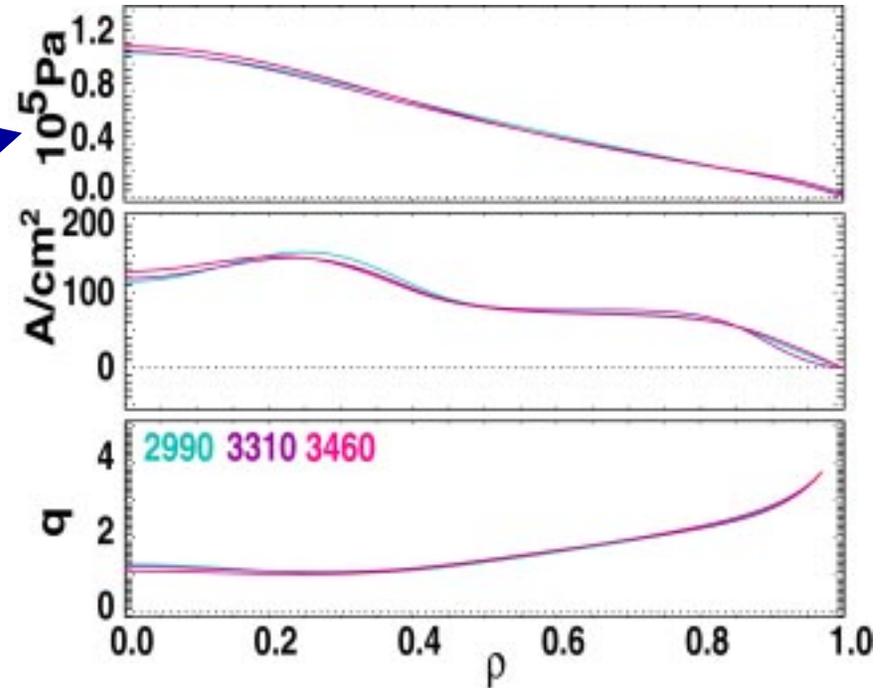
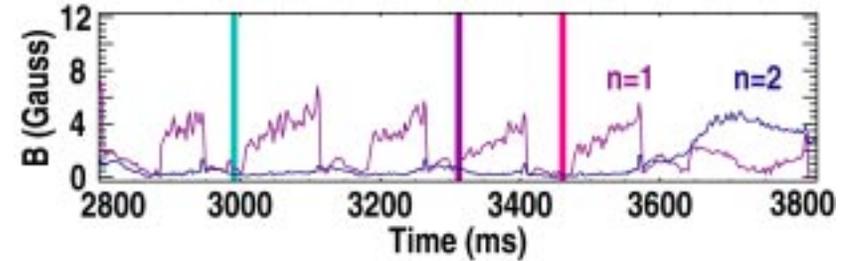
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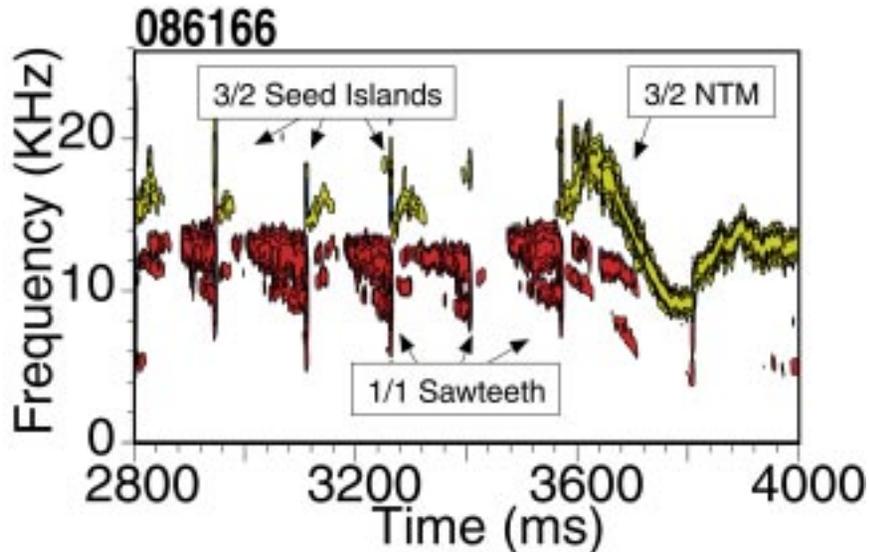
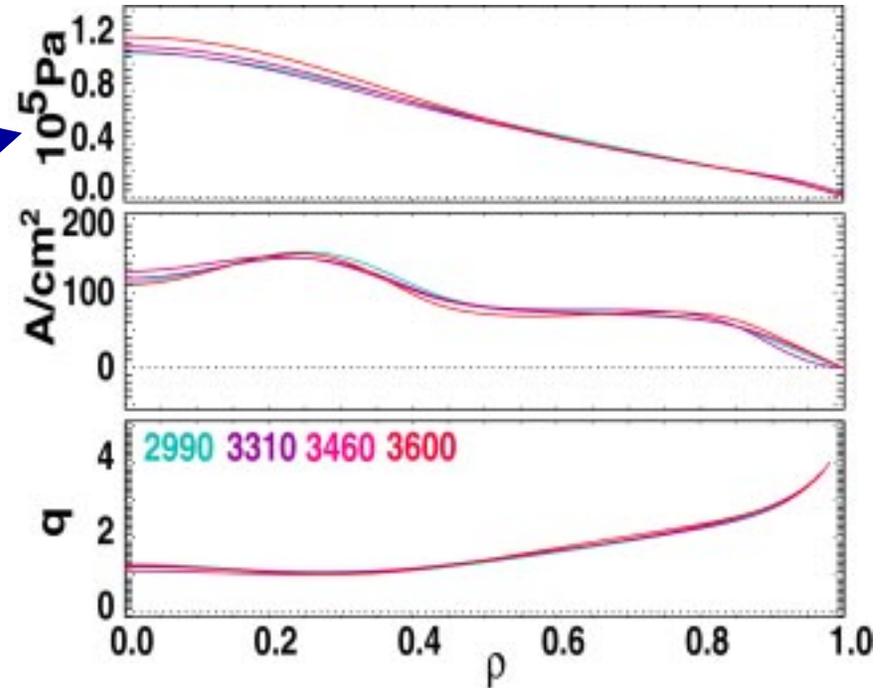
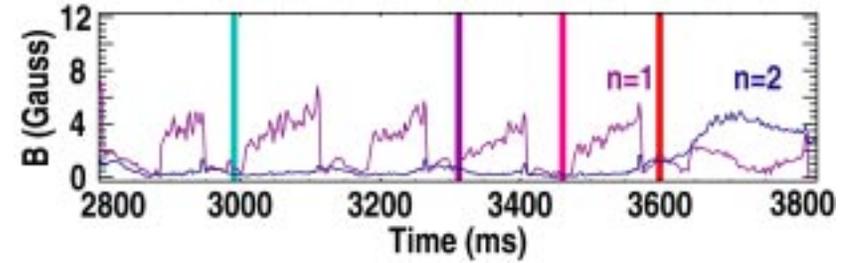
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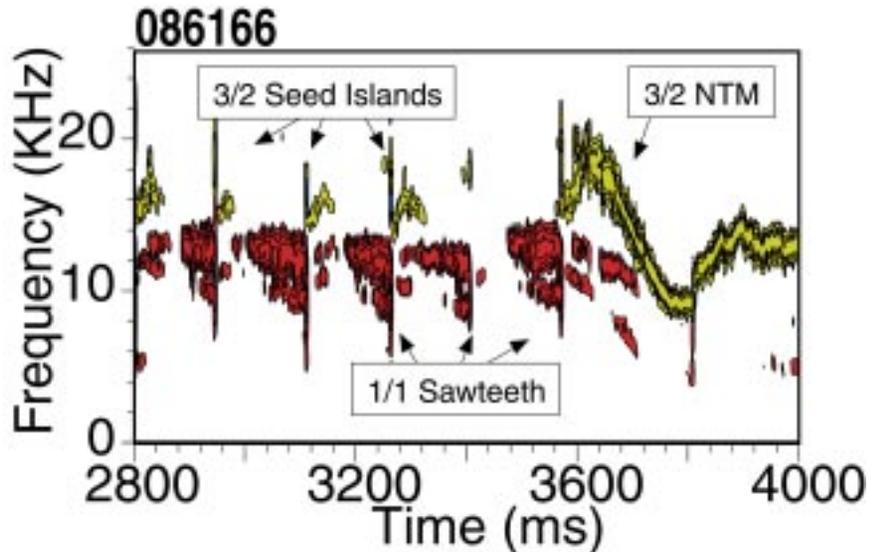
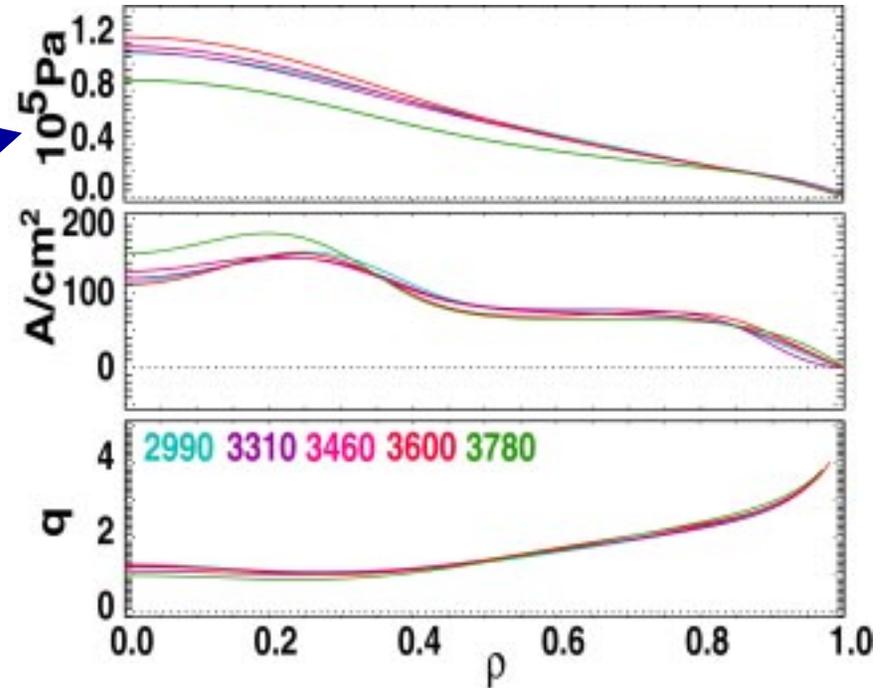
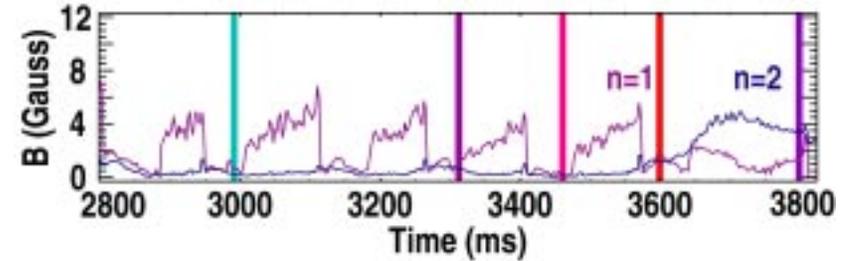
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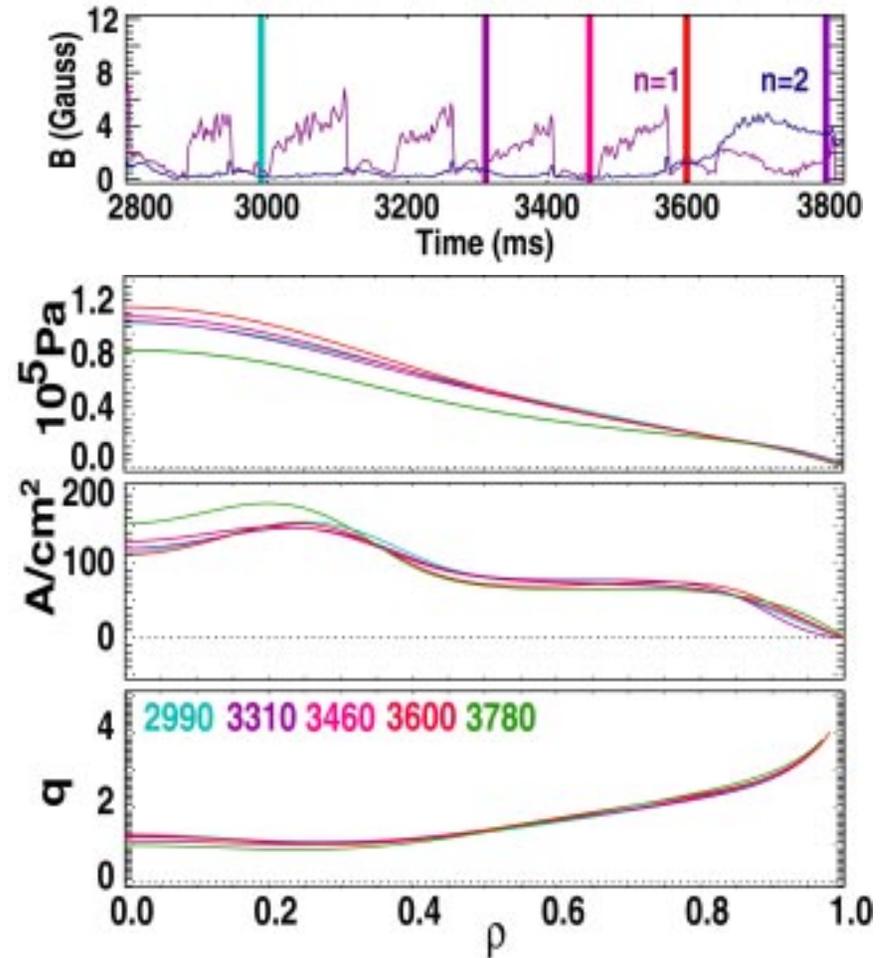
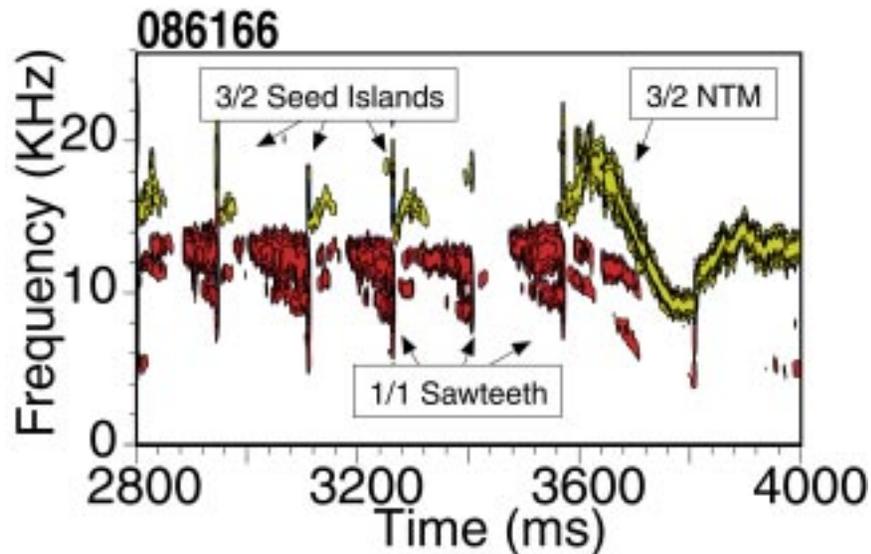
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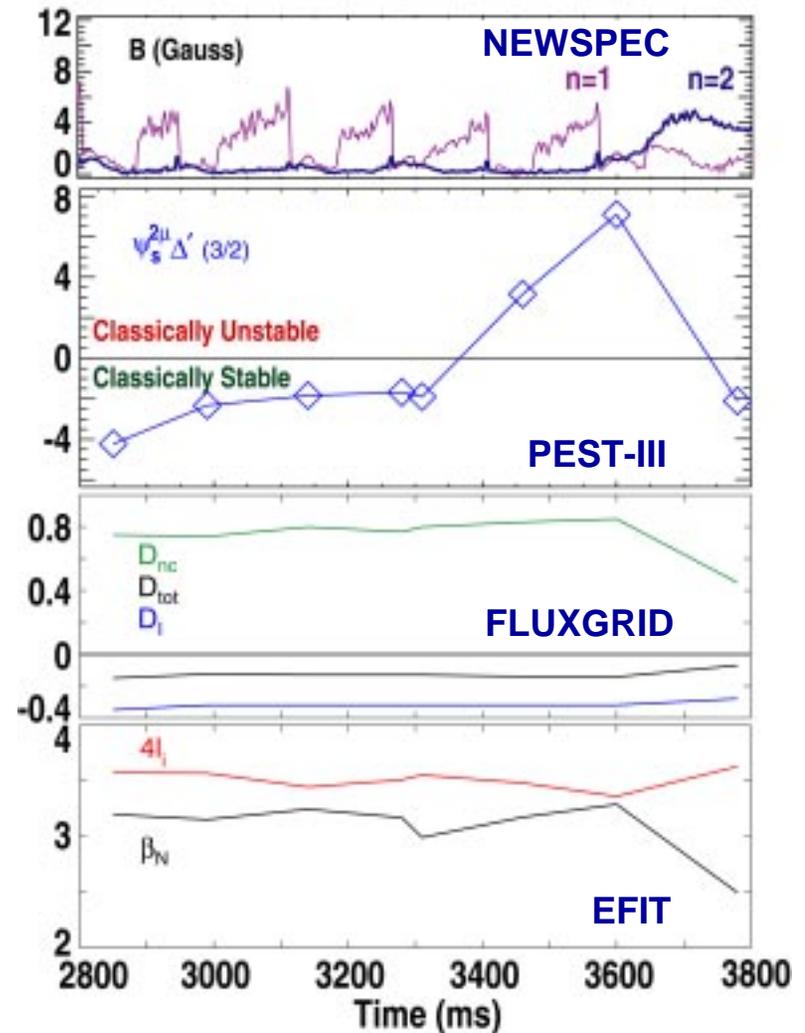
Point is to answer: why did the last sawtooth set off the 3/2 NTM while the several preceding similar sawteeth did not.



# Neoclassical Terms Remain Constant Between Sawtooth Periods, While $\Delta'$ Increases Sharply

Destabilization of seed island and transition to NTM state is driven primarily by change in  $\Delta'$

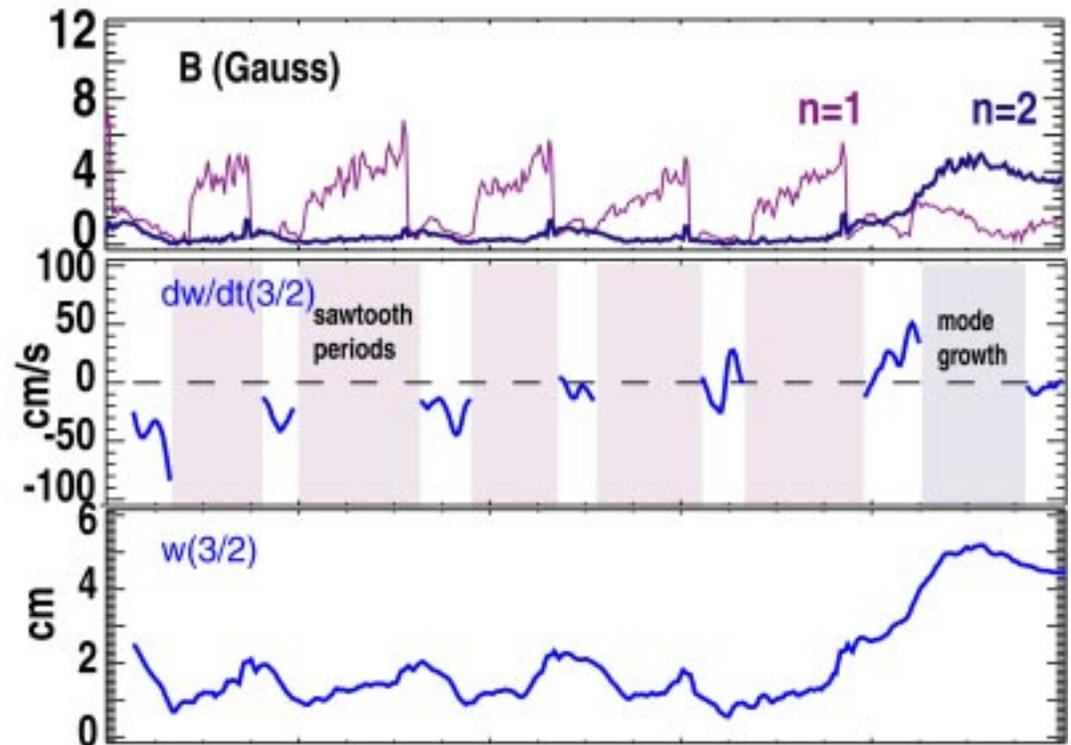
$\beta_N$  approaches no-wall limit at onset of 3/2 NTM —  $\Delta'$  pole is underlying mechanism for destabilization



# To Test This Proposition Island Evolution is Reconstructed From Experiment and Compared to Theory

$$w = \left( \frac{16rR_o |\tilde{B}_r|}{msB_{\phi o}} \right)^{1/2}$$
$$|\tilde{B}_r| = \frac{1}{2} \left( \frac{b}{r} \right)^{m+1} |\tilde{B}_\theta|$$

w from Magnetic Probe Signals used to compare dw/dt from theory and experiment

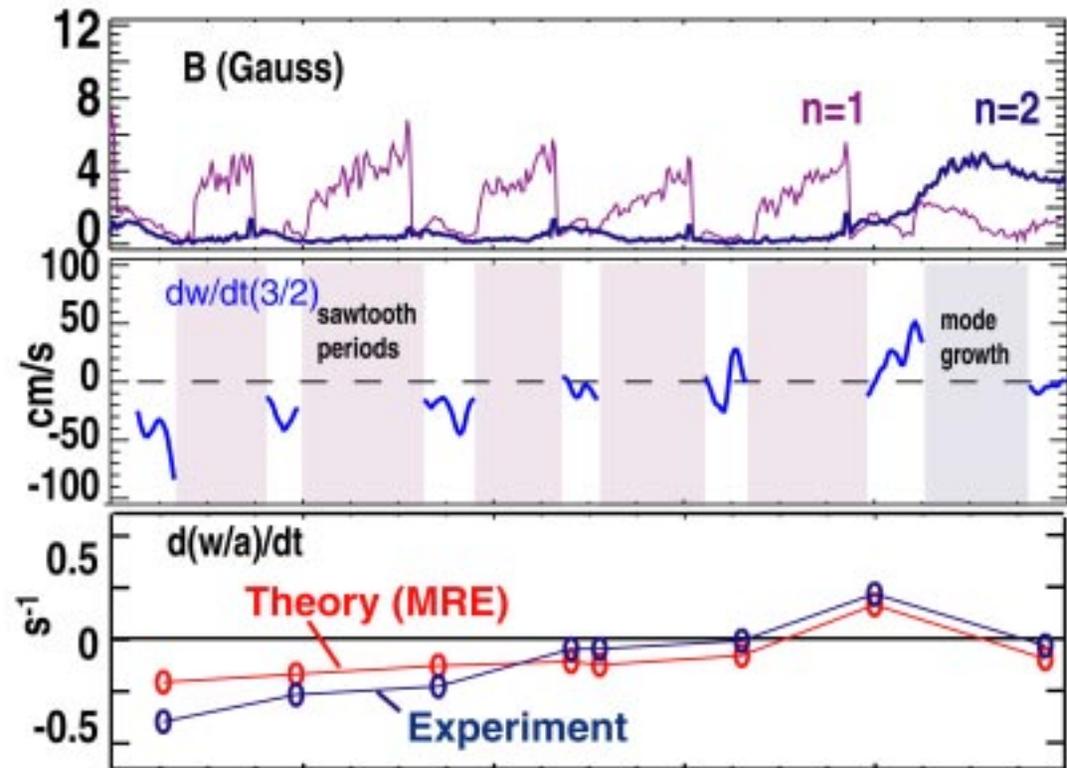


# dw/dt from Island Evolution Equation Agrees with dw/dt from Experimental Data

Island Evolution Equation gives right answer even without nonlinear coupling and with axisymmetric  $\Delta'$ .

$D_{pol}$  determined from  $\chi^2$  minimization agrees in sign with analytic value, but is smaller.

$$D_{pol} = -2.3e-5$$

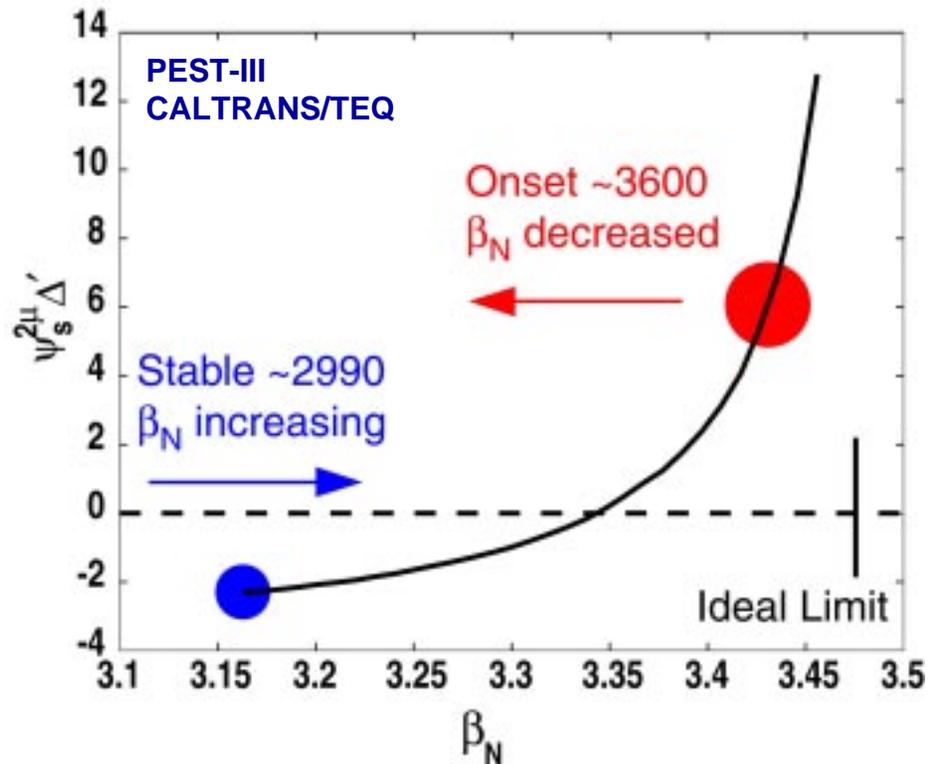


# Increase in Core Pressure Causes $\Delta'$ to Sharply Increase Due to Approach of Ideal Limit

Pressure profile at 2990 was gradually modified to approximate profile at 3600, showing transition.

Approach to  $n=2$  ideal limit increases  $3/2 \Delta'$ .

Pole causes rapid change in  $\Delta'(\beta)$  as  $\beta$  changes slightly

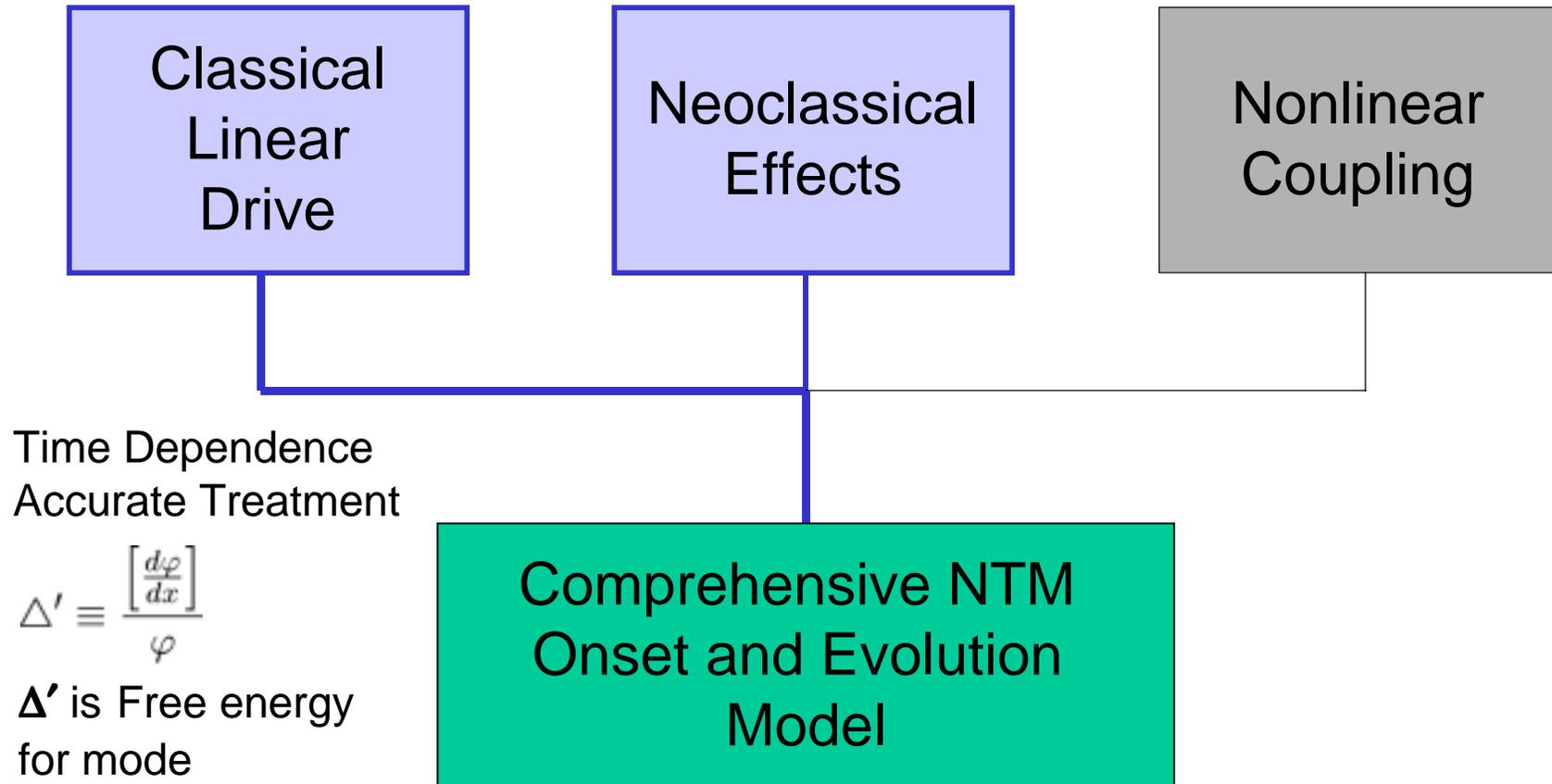


Nonlinear coupling between  $n=1$  and  $n=2$  modes not addressed by this model

How will this affect the stability and evolution?

# A Comprehensive Model of NTM Onset Emerges From a Combination of Theories

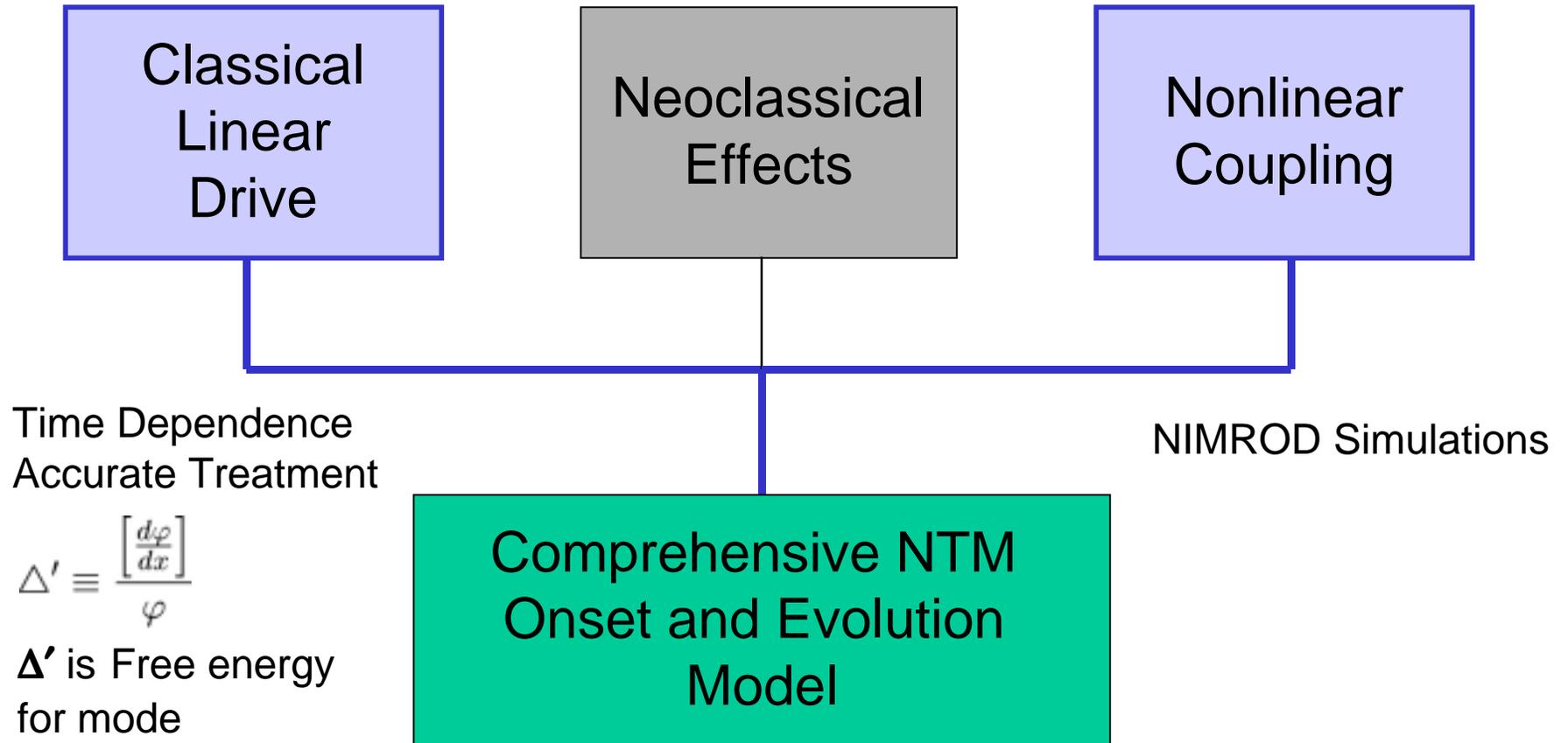
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All three components are necessary to explain the onset and evolution

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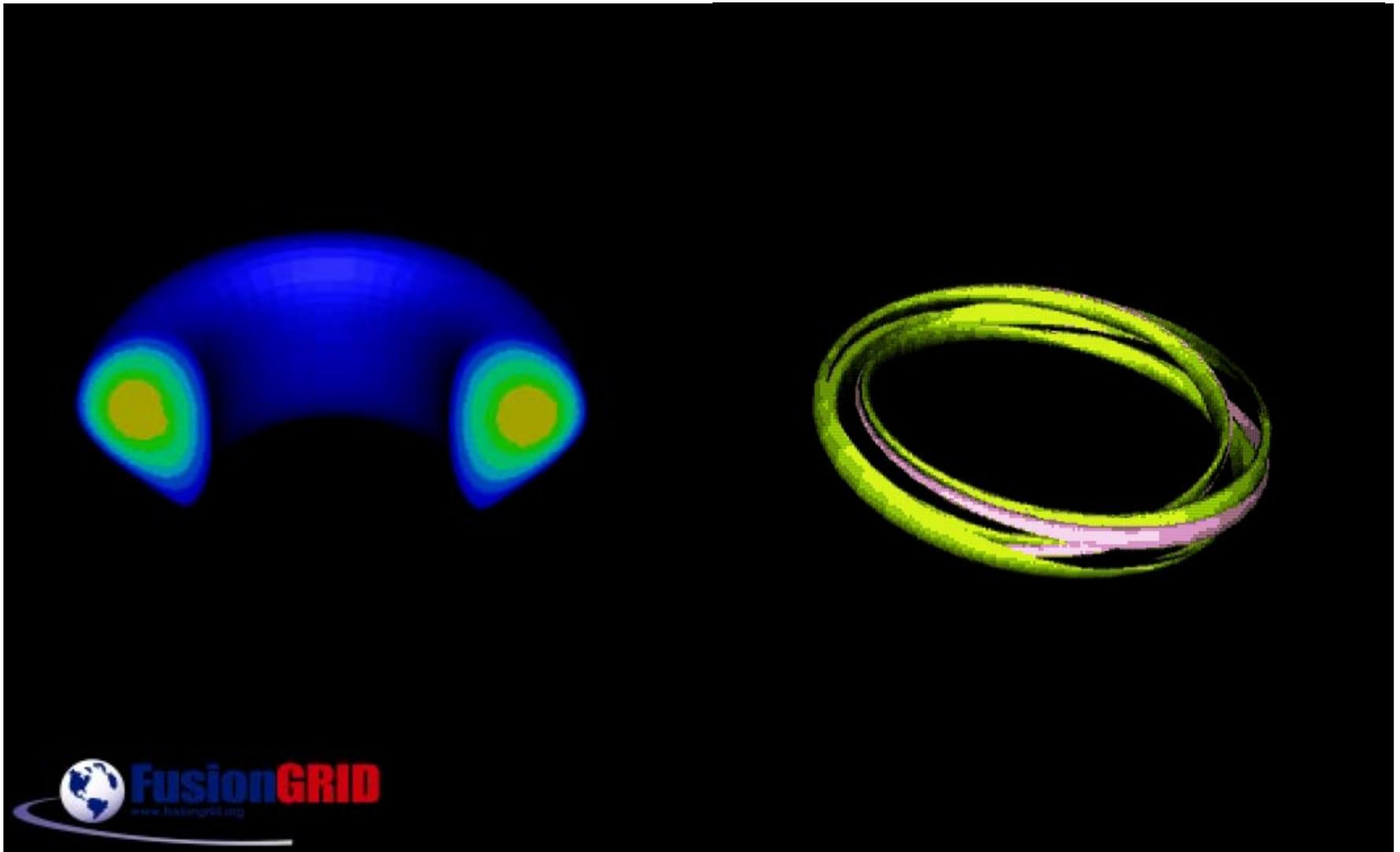
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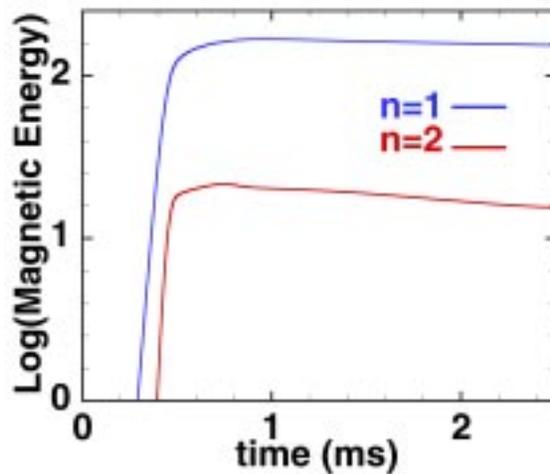
Studying the structure and nonlinear evolution of these modes with NIMROD can lead to new intuition and new physics

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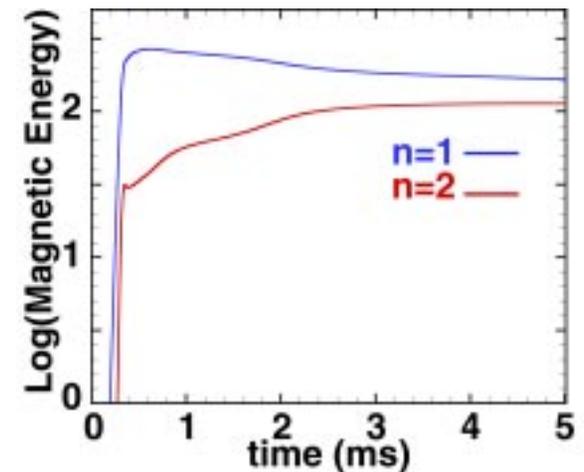
# NIMROD Simulations of two discharge times show unstable n=1 mode and driven n=2 mode, in agreement with experiment

$t_{\text{exp}}=2990$

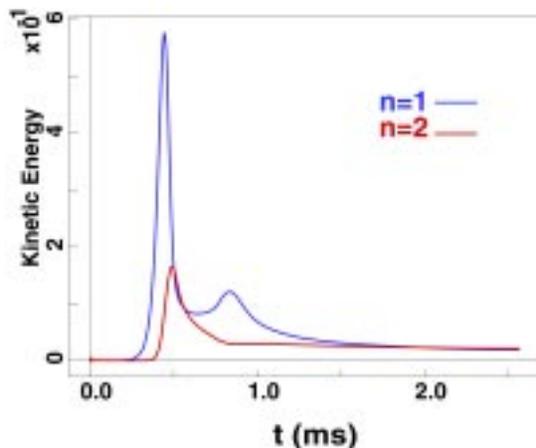


Stable  
n=2 decays  
after n=1  
drive begins  
to reduce

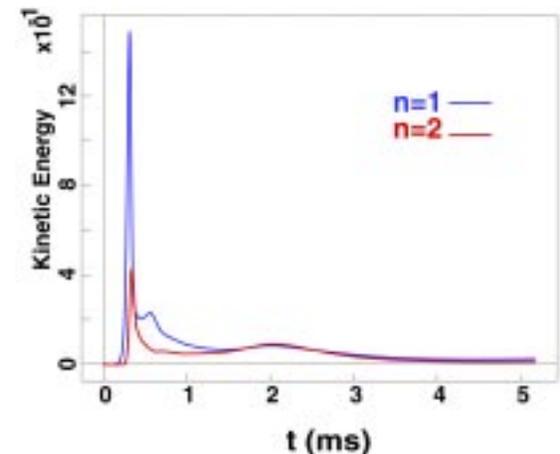
$t_{\text{exp}}=3600$



Unstable  
n=2 grows  
after n=1  
drive begins  
to reduce



$S=\tau_R/\tau_A=2.3e6$   
approaching  
realistic conditions



At later times, after saturation of  $n=1$ , the  $m=3$  component of  $n=2$  is dominant

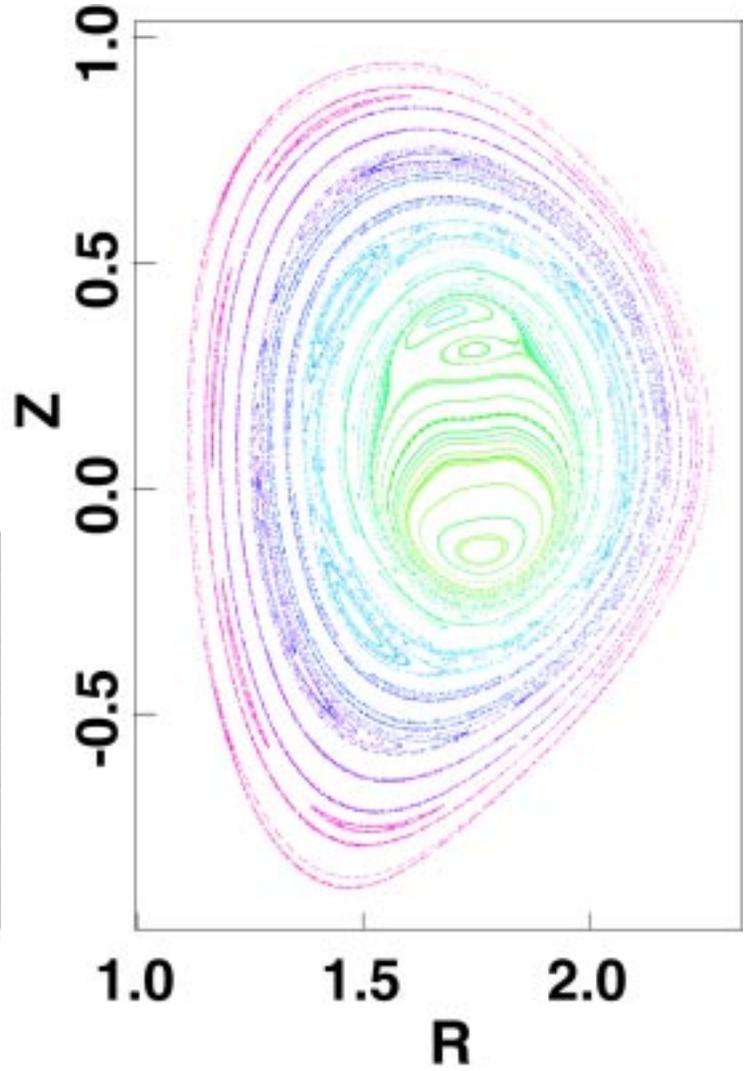
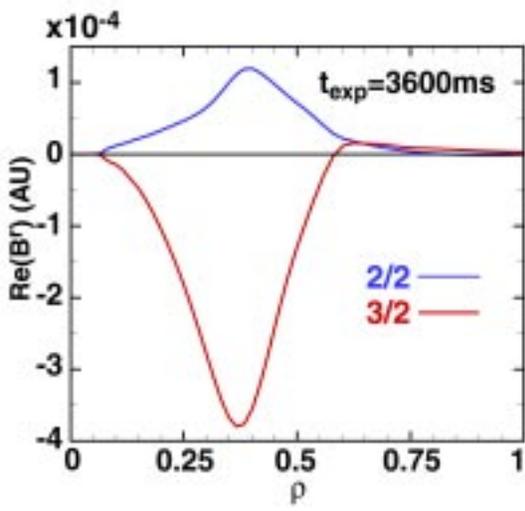
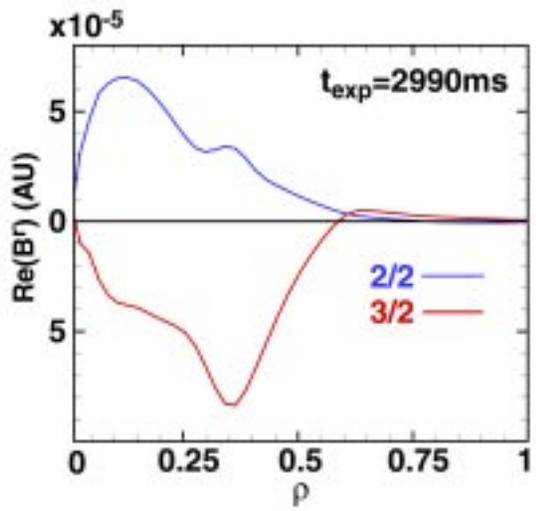
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$3/2$  decays in simulation of 2990ms

$3/2$  is larger and grows to saturation in simulation of 3600ms

Eigenfunctions show  $m=3$  to be dominant  $n=2$  component.

$m=1$  is dominant  $n=1$ .

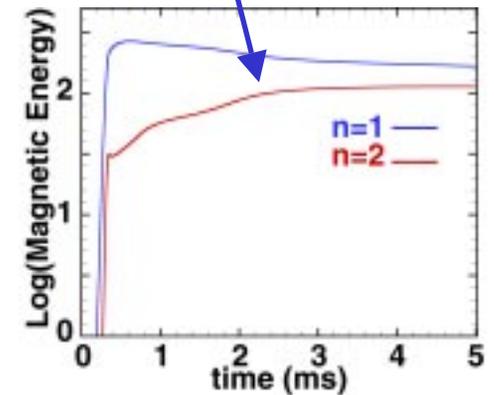
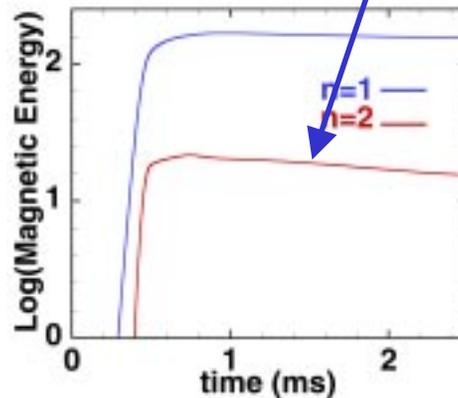
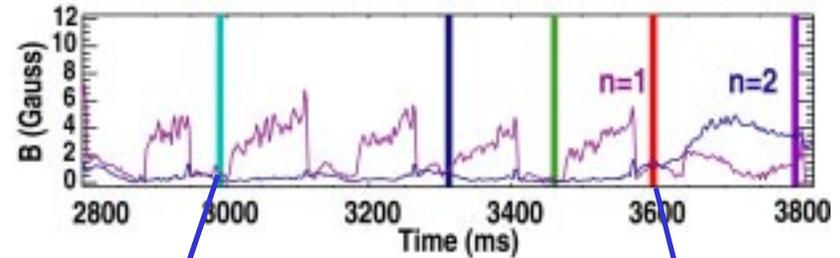


# Dynamics of NIMROD Simulations Indicate That Linear $\Delta'$ Drive Affects Islands Of Finite Width

$m/n=3/2$  is unstable for 3600ms, when  $n=1$  mode decays.

Nonlinear coupling effects do not prevent later seed island growth.

Equilibrium at 3600ms is closer to ideal limit and has larger linear drive.



The pole in  $\Delta'$  effects the stability of NTM seed islands

# DIII-D Experiment was Designed and Performed to Determine Effect of Poles in $\Delta'$ on Tearing Stability

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## **Experiment designed to isolate $\Delta'$ pole mechanism**

avoid other modes

vary  $d\beta_N/dt$  on approach to onset of 2/1

**Prediction was made that for spontaneous NTMs, evolution should depend on rate of approach to ideal boundary.**

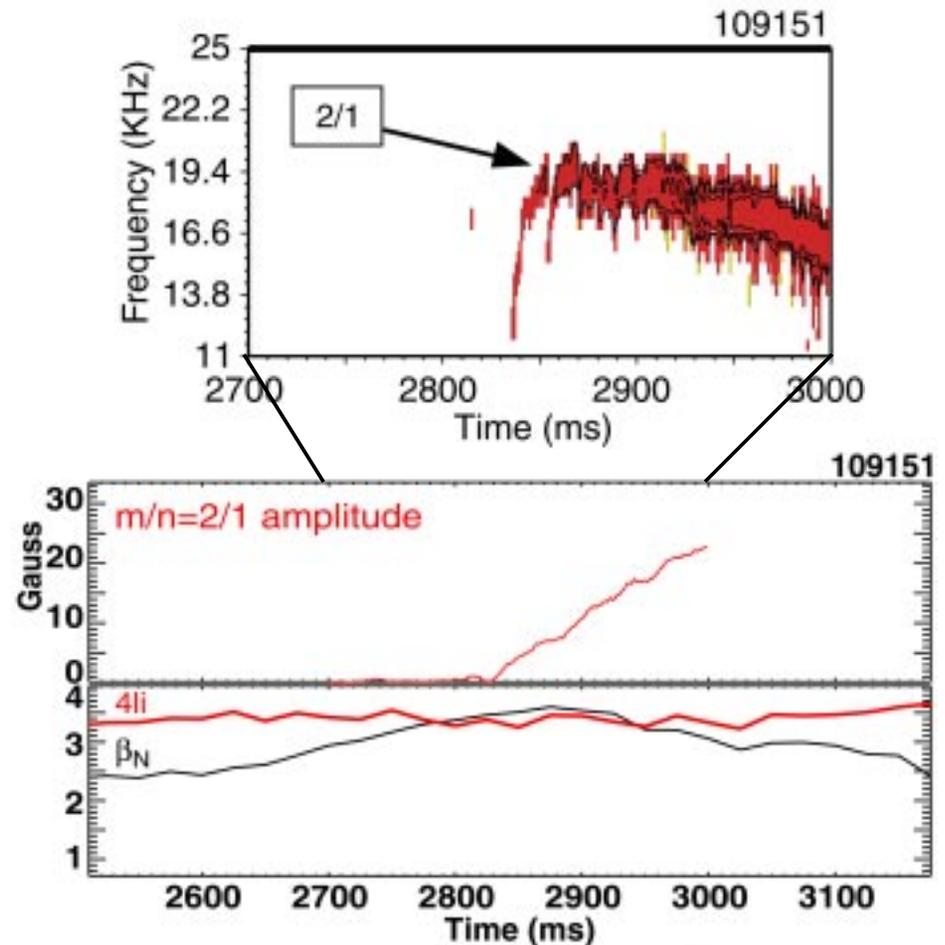
Measure  $\beta_N$  at point where  $w \sim w_d$  as a function of  $d\beta_N/dt$

Forced reconnection gives random  $w$  at random  $t$ , and should not show a correlated function like  $\Delta'(\beta)$

# Spontaneous/Seedless NTMs were Generated to Isolate Effect of $\Delta'$ Pole Onset Mechanism

Neutral beam injection applied at increasing rates up to  $\beta$  limit for 2/1 NTM onset.

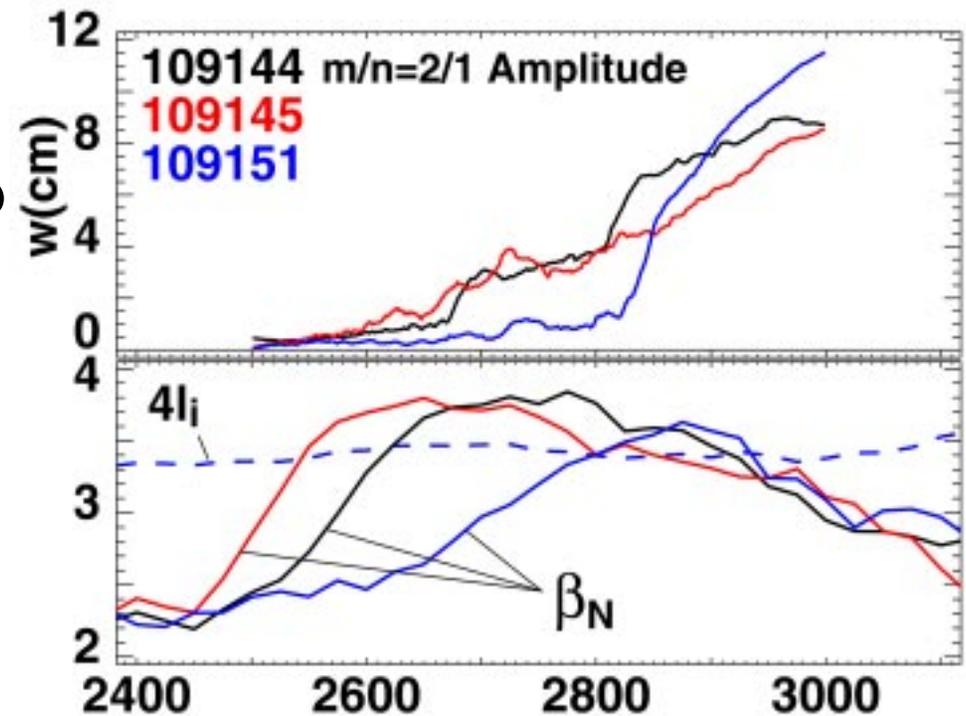
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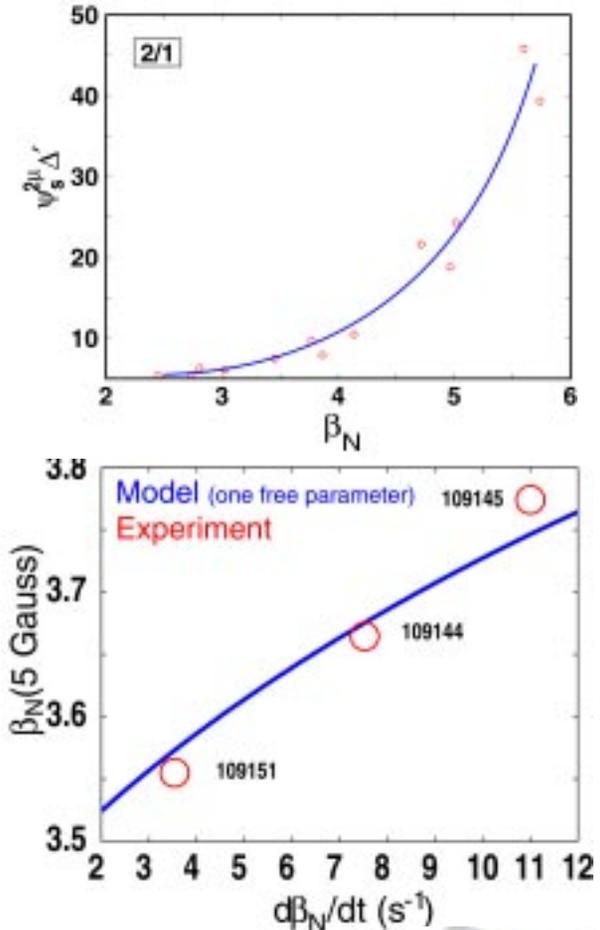
# Experimental Data Confirms New Theoretical Prediction from $\Delta'$ Pole Model

Model uses  $\beta_N(t)$  from experiment and  $\Delta'(\beta_N)$  in island evolution equation.

Pressure profiles modified in model equilibria and  $\Delta'$  at 2/1 surface calculated. Result is a function  $\Delta'(\beta_N)$ .

$D_{pol}$  is single constant free parameter fit to find  $\beta_N$  vs.  $d\beta_N/dt$  at mode onset.

Results support hypothesis that  $\Delta'$  is increasing rapidly in time, consistent with theoretical pole model.



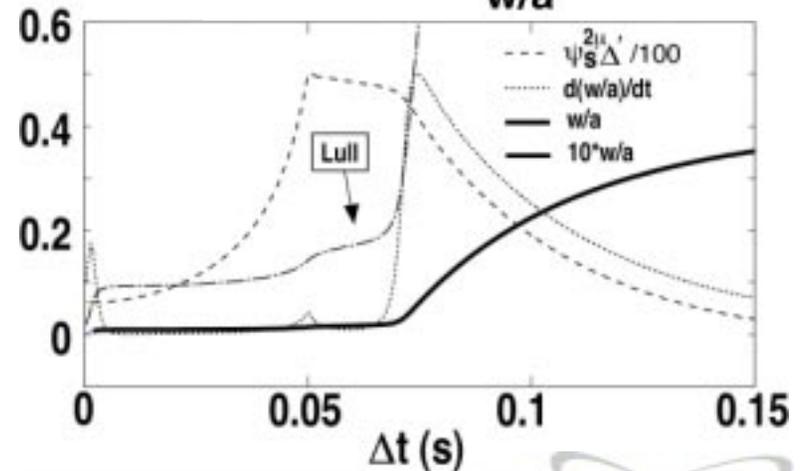
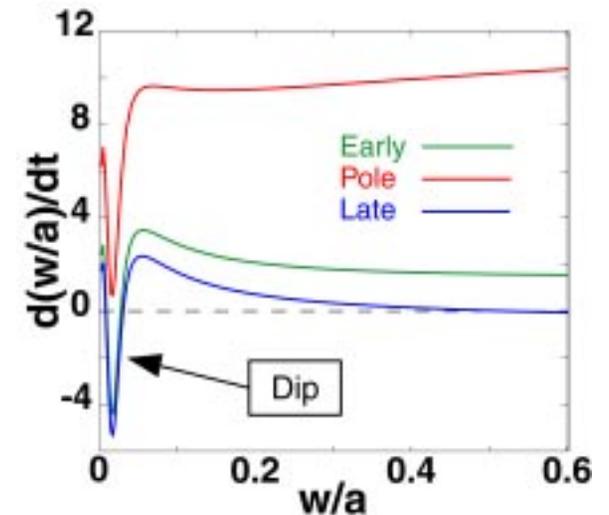
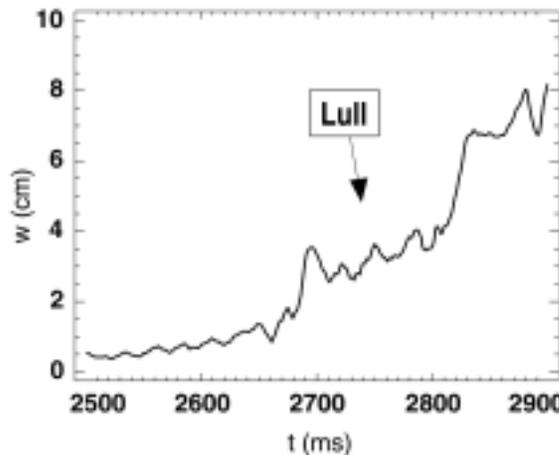
# Modeling of $\Delta'$ Pole Experiment Reproduces $dw/dt$ Lull Shortly After Onset

$D_{pol}$  term negligible at small island width. A model for  $D_{pol}$  is assumed which decays at  $w < w_b$ .

$$\frac{dw}{dt} = \frac{\eta^*}{k_0} \left( \Delta^* [\beta_N(t)] + \frac{w D_{tot}}{w_d^2 + w^2} + \frac{w D_{pol}}{w_b^4 + w^4} \right)$$

Resulting phase space plots have a Dip in growth rates.

$\beta_N(t)$  driving function reproduces Lull in growth



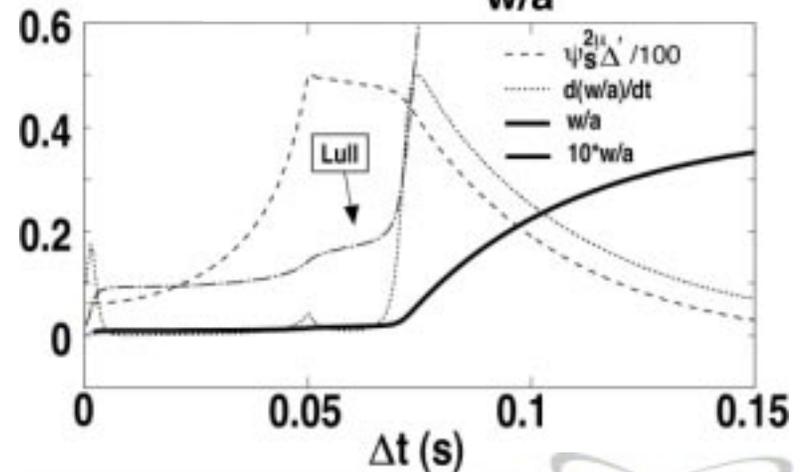
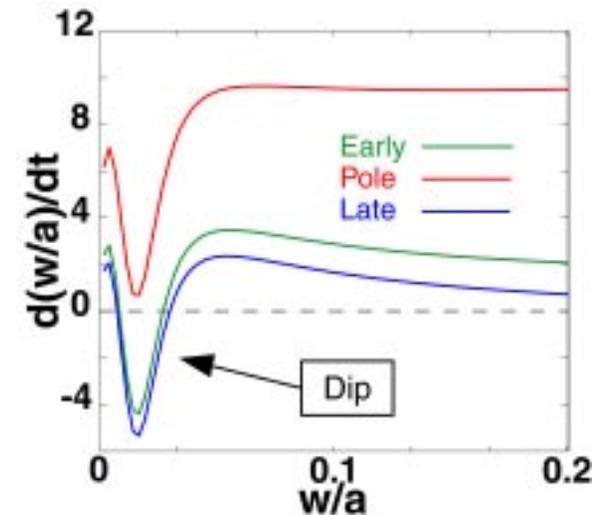
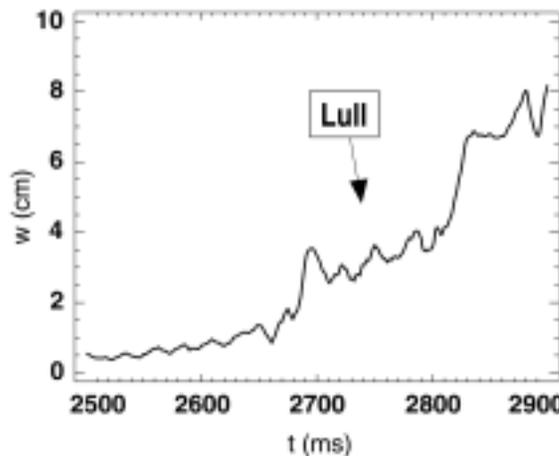
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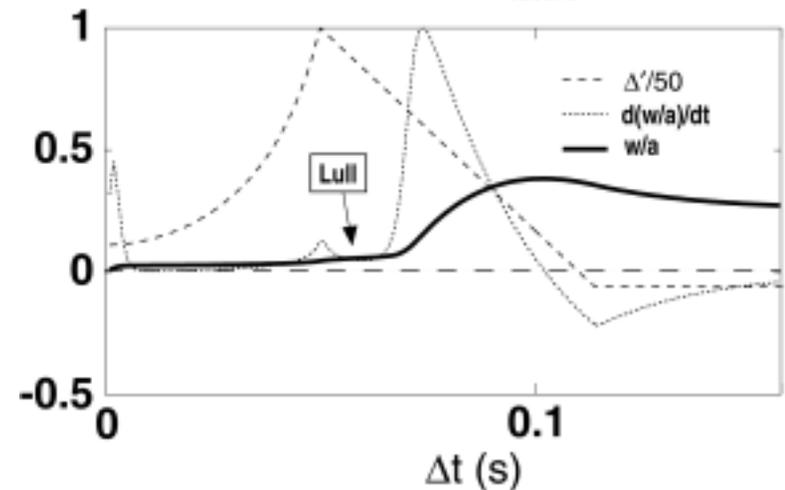
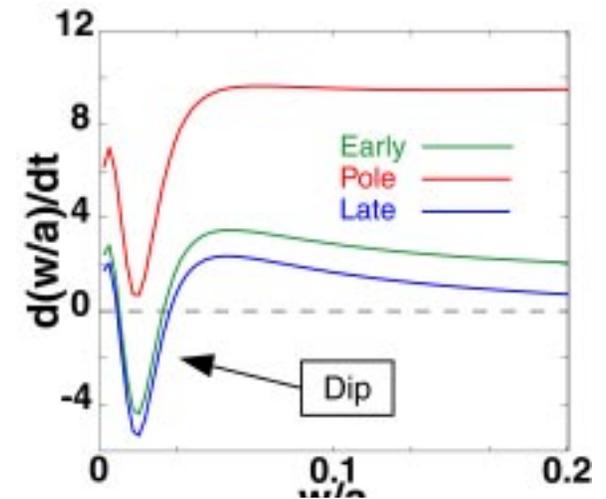
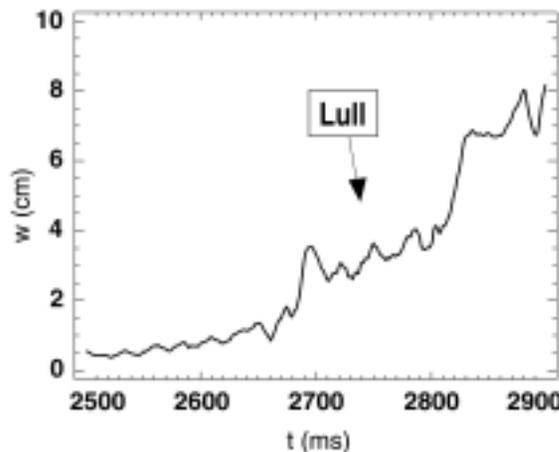
# Modeling of $\Delta'$ Pole Experiment Reproduces $dw/dt$ Lull Shortly After Onset

$D_{pol}$  term negligible at small island width. A model for  $D_{pol}$  is assumed which decays at  $w < w_b$ .

$$\frac{dw}{dt} = \frac{\eta^*}{k_0} \left( \Delta^* [\beta_N(t)] + \frac{w D_{tot}}{w_d^2 + w^2} + \frac{w D_{pol}}{w_b^4 + w^4} \right)$$

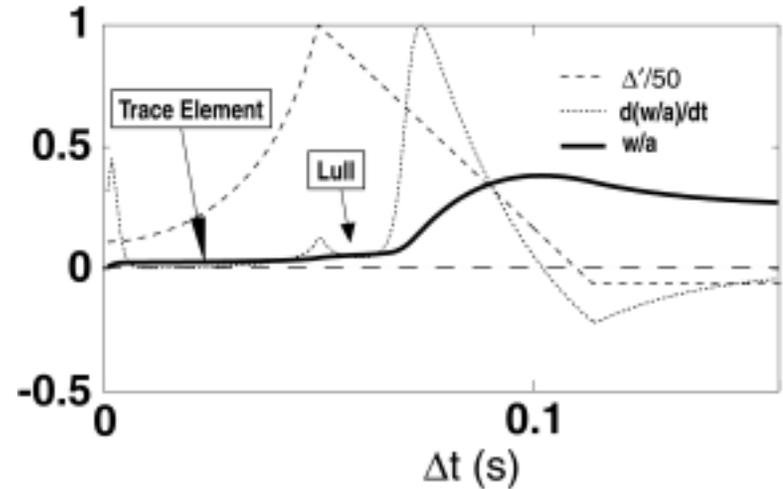
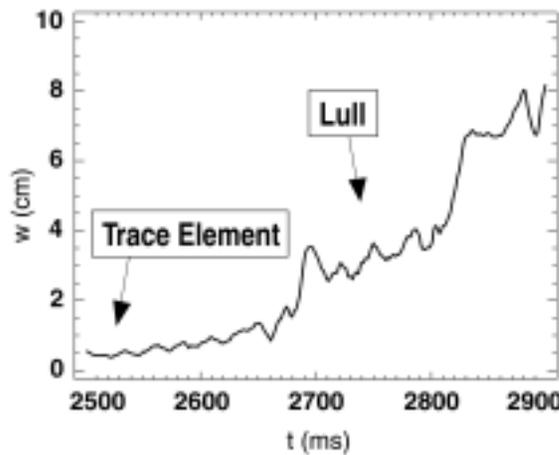
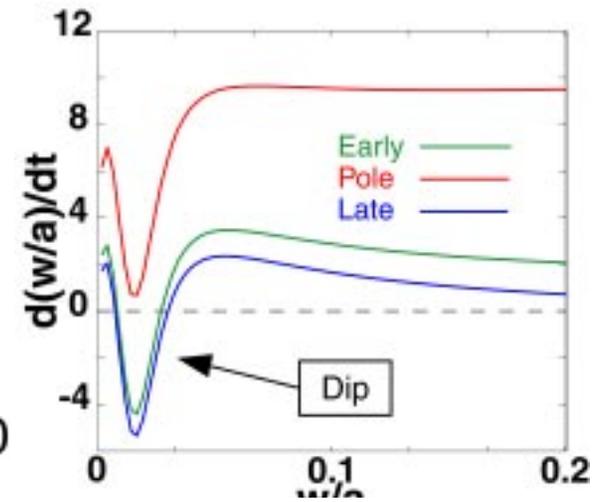
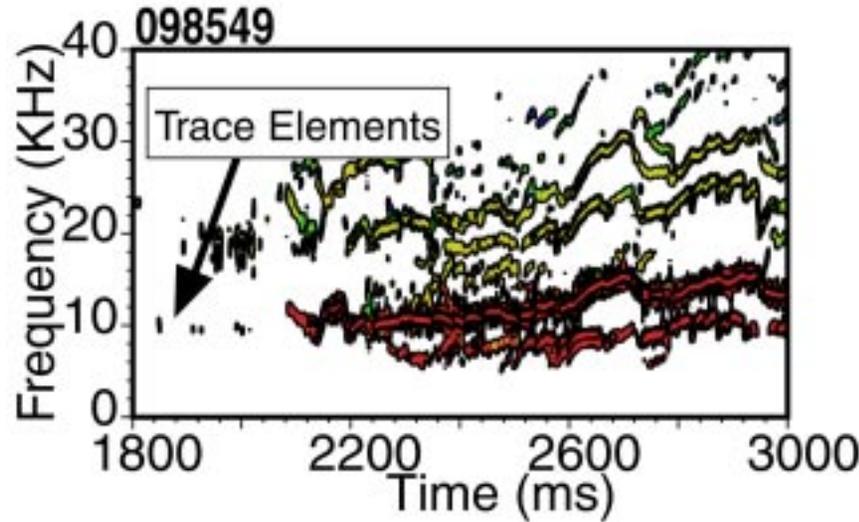
Resulting phase space plots have a Dip in growth rates.

$\beta_N(t)$  driving function reproduces Lull in growth



# Onset Model Reproduces Trace Elements and $dw/dt$ Lull Shortly After Onset

Model reproduces Lull in growth and Trace Elements



## Summary of Results

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- **Increasing  $\beta$  sharply increases  $\Delta'$  near ideal limit, due to approaching a pole, destabilizing NTMs**
  - In a sawtooth seeding a NTM case, eventual onset was caused by increased  $\Delta'$  due to approach of a pole
  - Nonlinear NIMROD simulations confirm that axisymmetric  $\Delta'$  is meaningful for nonlinearly coupled finite islands
- **DIII-D experiment confirmed effect of poles in  $\Delta'$  on NTM stability with varying rates of  $d\beta/dt$  causing spontaneous NTMs**
  - Data from early evolution are in agreement with prediction, both as function of  $d\beta_N/dt$  and detailed time evolution.

# Future Plans and Open Questions

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- **Predict the onset of spontaneous NTMs in the presence of an ECCD current peak**
  - Address the important physics model for  $D_{\text{ECCD}}$  and  $D_{\text{pol}}$  at  $w < w_b$
- **Can the lull phase and the trace elements be used as real-time indicators for avoidance of NTM transition**
  - Size of trace elements, slight  $\beta$  reduction during Lull phase
  - Experiment on DIII-D
  - Burning plasma projection
- **Seeded NTMs as ideal limit is approached, determine smaller threshold in burning plasma model**
  - Seeding in burning plasmas less sensitive to changes in  $\Delta'$ ?